

line element of Stiles
(1946) with „color values” P, D, T
three separate color signal functions
 $F(P) = c_i \log(1+9P)$
 $F(D) = c_j \log(1+9D)$
 $F(T) = c_k \log(1+9T)$

Taylor-derivations ($c=1/(n \ln 10)$):
 $\Delta F(P, D, T) = \frac{dF}{dP} \Delta P + \frac{dF}{dD} \Delta D + \frac{dF}{dT} \Delta T$
 $= \frac{9c_i}{1+9P} \Delta P + \frac{9c_j}{1+9D} \Delta D + \frac{9c_k}{1+9T} \Delta T$

line element of Vos & Walraven
(1972) with „color values” P, D, T
three separate color signal functions
 $F(P) = -2i \sqrt{P}$
 $F(D) = -2j \sqrt{D}$
 $F(T) = -2k \sqrt{T}$

Taylor-derivations:
 $\Delta F(P, D, T) = \frac{dF}{dP} \Delta P + \frac{dF}{dD} \Delta D + \frac{dF}{dT} \Delta T$
 $\Delta F(P, D, T) = \frac{1}{\sqrt{P}} \Delta P + \frac{1}{\sqrt{D}} \Delta D + \frac{1}{\sqrt{T}} \Delta T$

functions $q\{n x_r\}$ for „achromatic signal”-description

with $x_r = \log L_r = \log L / L_b$
(L_b = background luminance)

$q\{n x_r\} = 1 + 1/[1 + \sqrt{2} \cdot 10^{n x_r}]$
function values (with $n = k \log e$):
 $q\{n x_r \rightarrow +\infty\} = 1$
 $q\{n x_r = 0\} = \sqrt{2}$
 $q\{n x_r \rightarrow -\infty\} = 2$

„achromatic signal” sensitivity
as function of relative luminance
 $g = \log H = n x_r$

$Q' = \frac{d}{dH} \{ \log[1 + 1/(1 + \sqrt{2}H)] \} / \log \sqrt{2}$
 $= -\sqrt{2} / \{ \log \sqrt{2} [1 + (1 + \sqrt{2}H)(2 + \sqrt{2}H)] \}$
function values:
 $Q'\{n x_r \rightarrow +\infty\} = 0$
 $Q'\{n x_r = 0\} = -0,5$
 $Q'\{n x_r \rightarrow -\infty\} = 0$

double line element of Richter
(2006) for the lighting technic with
relative luminance $L_r = F(L, M, S)$

luminance signal function $F(L_r)$
 $F(L_r) = i Q(H) \quad (x_r < 0)$
 $F(L_r) = i Q(H) \quad (x_r \geq 0)$
with: $n = 1,4 \quad \bar{n} = c \quad i = 1 \quad i = -2$
 $x_r = \log L_r \quad H = 10^{n x_r} \quad \bar{H} = 10^{\bar{n} x_r}$

„achromatic signal”-description
functions $Q_{lm}\{n x_r\}$

with $x_r = \log L_r$
(L_r = relative luminance)

$Q_{lm}\{n x_r\} = \frac{1}{\log \sqrt{2}} \log q\{n x_r\} - m$
function values with $l = m = 1$:
 $Q\{n x_r \rightarrow +\infty\} = 1$
 $Q\{n x_r = 0\} = 0$
 $Q\{n x_r \rightarrow -\infty\} = -1$

relative luminance sensitivity
 $L_r / \Delta L_r$ as function of H

$L_r = 10^x H = 10^{n x_r} \quad c = \ln 10$
 $dL_r/dx = c L_r \quad dH/dx = c n H$
it follows: $L_r / \Delta L_r = [n H / (dH c)]$
 $L_r / dL_r = \text{const} H / [(1 + \sqrt{2}H)(2 + \sqrt{2}H)]$
 $Q'\{n x_r \rightarrow +\infty\} = 0$
 $Q'\{n x_r = 0\} = \text{maximum}$
 $Q'\{n x_r \rightarrow -\infty\} = 0$

double line element of Richter
(2006) for the lighting technic with
relative luminance $L_r = F(L, M, S)$

luminance signal function $F(L_r)$
 $F(L_r) = i Q(H) \quad H = 10^{n x_r}$
 $Q[\log \{1 + 1/(1 + \sqrt{2}H)\}] / \log \sqrt{2} - 1$
Taylor-derivations:
 $\Delta F(L_r) = \frac{dF}{dL_r} \Delta L_r = i \frac{dQ}{dH} \Delta H$
 $= -i \sqrt{2} \Delta H / \{ \log \sqrt{2} [1 + (1 + \sqrt{2}H)(2 + \sqrt{2}H)] \}$

