

Line element of Stiles (1946) with „cone values“  $L, M, S$  separate colour response functions

$$F(L) = i \ln(1+9L)$$

$$F(M) = j \ln(1+9M)$$

$$F(S) = k \ln(1+9S)$$

Taylor-derivations:

$$\Delta F(L, M, S) = \frac{dF}{dL} \Delta L + \frac{dF}{dM} \Delta M + \frac{dF}{dS} \Delta S$$

$$= \frac{9i}{1+9L} \Delta L + \frac{9j}{1+9M} \Delta M + \frac{9k}{1+9S} \Delta S$$

feb20-1N

Line element of Vos&Walraven (1972) with „cone values“  $L, M, S$  separate colour response functions

$$F(L) = -2i\sqrt{L}$$

$$F(M) = -2j\sqrt{M}$$

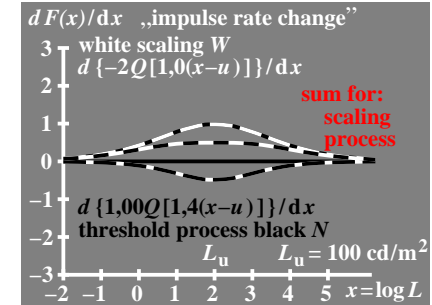
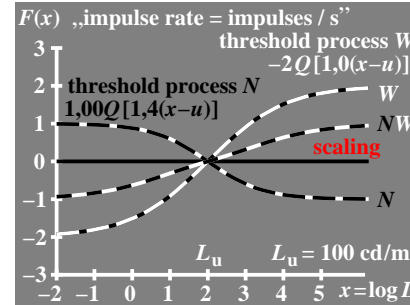
$$F(S) = -2k\sqrt{S}$$

Taylor-derivations:

$$\Delta F(L, M, S) = \frac{dF}{dL} \Delta L + \frac{dF}{dM} \Delta M + \frac{dF}{dS} \Delta S$$

$$\Delta F(L, M, S) = \frac{i}{\sqrt{L}} \Delta L + \frac{j}{\sqrt{M}} \Delta M + \frac{k}{\sqrt{S}} \Delta S$$

feb20-2N



functions  $q[k(x-u)]$  „achromatic signal“-description with  $x = \log L$  ( $L$  = luminance)  $u = \log L_u$  ( $L_u$  = surround luminan.)

$$q[k(x-u)] = 1 + 1/[1 + \sqrt{2}e^{k(x-u)}]$$

function values:

$$q[k(x-u) \rightarrow +\infty] = 1$$

$$q[k(x-u) = 0] = \sqrt{2}$$

$$q[k(x-u) \rightarrow -\infty] = 2$$

feb20-3N

„achromatic signal“-description functions  $Q_{lm}[k(x-u)]$  with  $x = \log L$  ( $L$  = luminance)  $u = \log L_u$  ( $L_u$  = surround luminan.)

$$Q_{lm}[k(x-u)] = \frac{l}{\ln \sqrt{2}} \ln q[k(x-u)] - m$$

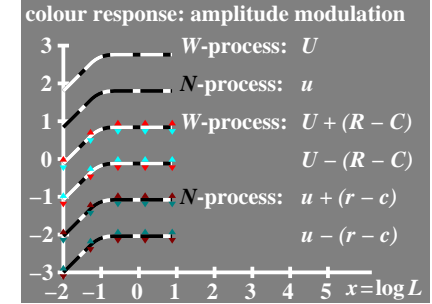
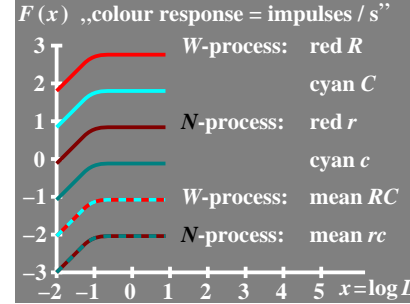
function values with  $l = m = 1$ :

$$Q[k(x-u) \rightarrow +\infty] = 1$$

$$Q[k(x-u) = 0] = 0$$

$$Q[k(x-u) \rightarrow -\infty] = -1$$

feb20-4N



„achromatic signal“-discrimination as function of relative light density  $h = \ln H = k(x-u)$   $\ln$  = natural log.

$$Q' = \frac{d}{dH} [\ln\{1 + 1/(1 + \sqrt{2}H)\}] / \ln \sqrt{2}$$

$$= -\sqrt{2} / [\ln \sqrt{2} (1 + \sqrt{2}H)(2 + \sqrt{2}H)]$$

function values:

$$Q'[k(x-u) \rightarrow +\infty] = 0$$

$$Q'[k(x-u) = 0] = -0,5$$

$$Q'[k(x-u) \rightarrow -\infty] = 0$$

feb20-5N

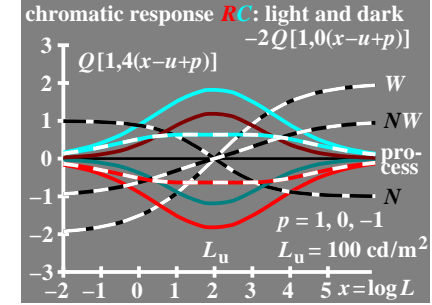
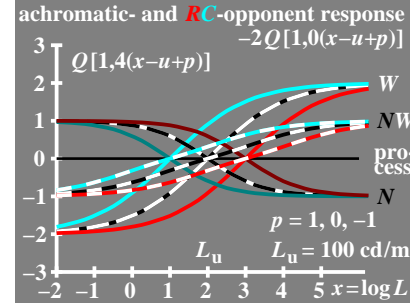
luminance discrimination possibility  $L/\Delta L$  as function of  $H$  with:  $L = 10^x H = e^{h} = 10^{\log e k(x-u)}$

$$\frac{dL}{dx} = \ln 10 L \quad \frac{dH}{dx} = k H$$

it follows:  $L/\Delta L = [kH / (dH \ln 10)]$

$$\frac{L}{dL} = \text{const } H / [(1 + \sqrt{2}H)(2 + \sqrt{2}H)]$$

feb20-6N



double line element of Richter (1987) for the lighting technic with luminance  $L = F(L, M, S)$

luminance signal function  $F(L)$

$$F(L) = iQ(H) = \begin{cases} i Q(\bar{H}) & (x < u) \\ \bar{i} Q(\bar{H}) & (x \geq u) \end{cases}$$

with:  $k=1,4 \quad \bar{k}=1 \quad \bar{i}=1 \quad \bar{i}=-2$

$$x = \log L \quad u = \log L_u$$

$$H = e^{k(x-u)}, \bar{H} = e^{\bar{k}(x-u)}$$

feb20-7N

double line element of Richter (1987) for the lighting technic with luminance  $L = F(L, M, S)$

luminance signal function  $F(L)$

$$F(L) = iQ(H) \quad H = e^{k(x-u)}$$

$$Q[\ln\{1 + 1/(1 + \sqrt{2}H)\}] / \ln \sqrt{2} - 1$$

Taylor-derivations:

$$\Delta F(L) = \frac{dF}{dL} \Delta L = i \frac{dQ}{dH} \Delta H$$

$$= -i\sqrt{2} \Delta H / [\ln \sqrt{2} (1 + \sqrt{2}H)(2 + \sqrt{2}H)]$$

feb20-8N

