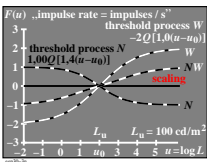


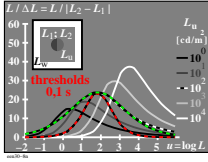
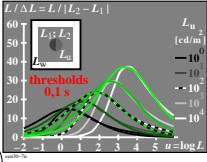
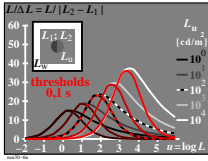
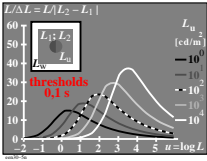
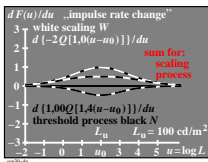
Weber-Fechner law in CIE 2002/03 for threshold colour difference of surface colours
 The Weber-Fechner law describes the lightness L^* , as an logarithmic function of L . The Stevens law describes the lightness $L_{200,20}$ as potential function of L .
 For $L_{200,20} = 1$ one obtains potential functions $L_{200,20} = a \cdot L^{0.425}$.
 The Weber-Fechner law is equivalent to the equation: $\Delta L_c = c \cdot L$.
 Integration leads to the logarithmic equation: $L_c = L \cdot \ln(L_c/L)$.
 Differentiation leads to the linear equation: $L_c = L \cdot (1 + \Delta L_c/L)$.
 The colour in offset is the standard contrast range is 25:1-100:3.
 Table 3: CIE relative values L^* , luminance L , and lightness L^* .

Colour (name)	Tri-stimulus value (x,y,z)	luminance (cd/m ²)	relative luminance L/L_u	CIE lightness L^*	relative lightness L^*/L_u^*
White W	0.3127, 0.3290, 0.3568	100	1.0000	100	1.0000
Black N	0.0381, 0.0441, 0.0481	0.02	0.0002	2	0.0200
Grey Z (paper)	0.1975, 0.2126, 0.2276	10	0.1000	10	0.1000
Black N	0.0381, 0.0441, 0.0481	0.02	0.0002	2	0.0200
White W	0.3127, 0.3290, 0.3568	100	1.0000	100	1.0000



Weber-Fechner law in CIE 2002/03 for threshold colour difference of surface colours and two ranges 0.2 ≤ L_c <= 1 and 1 < L_c <= 10
 The Weber-Fechner law describes the lightness L^* , as an logarithmic function of L . The Stevens law describes the lightness $L_{200,20}$ as potential function of L .
 For $L_{200,20} = 1$ one obtains potential functions $L_{200,20} = a \cdot L^{0.425}$.
 The Weber-Fechner law is equivalent to the linear equation: $\Delta L_c = c \cdot L$.
 Integration leads to the logarithmic equation: $L_c = L \cdot \ln(L_c/L)$.
 Differentiation leads to the linear equation: $L_c = L \cdot (1 + \Delta L_c/L)$.
 The colour in offset is the standard contrast range is 25:1-100:3.
 Table 4: CIE relative values L^* , luminance L , and lightness L^* .

Colour (name)	Tri-stimulus value (x,y,z)	luminance (cd/m ²)	relative luminance L/L_u	CIE lightness L^*	relative lightness L^*/L_u^*
White W	0.3127, 0.3290, 0.3568	100	1.0000	100	1.0000
Black N	0.0381, 0.0441, 0.0481	0.02	0.0002	2	0.0200
Grey Z (paper)	0.1975, 0.2126, 0.2276	10	0.1000	10	0.1000
Black N	0.0381, 0.0441, 0.0481	0.02	0.0002	2	0.0200
White W	0.3127, 0.3290, 0.3568	100	1.0000	100	1.0000



Colour-line element of Stiles (1946) with 'colour values' L_P, M_D, S_T
 three separate colour-response functions
 $F(L_P) = i \ln(1 + 9 \cdot L_P)$
 $F(M_D) = j \ln(1 + 9 \cdot M_D)$
 $F(S_T) = k \ln(1 + 9 \cdot S_T)$
Taylor-derivations:
 $\Delta F(L_P, M_D, S_T) = \frac{dF}{dL_P} \Delta L_P + \frac{dF}{dM_D} \Delta M_D + \frac{dF}{dS_T} \Delta S_T$
 $= \frac{9i}{1+9L_P} \Delta L_P + \frac{9j}{1+9M_D} \Delta M_D + \frac{9k}{1+9S_T} \Delta S_T$

Colour-line element of Vos&Walraven (1972) with 'colour values' L_P, M_D, S_T
 three separate colour-response functions
 $F(L_P) = -2 \sqrt{L_P}$
 $F(M_D) = -2 \sqrt{M_D}$
 $F(S_T) = -2 \sqrt{S_T}$
Taylor-derivations:
 $\Delta F(L_P, M_D, S_T) = \frac{dF}{dL_P} \Delta L_P + \frac{dF}{dM_D} \Delta M_D + \frac{dF}{dS_T} \Delta S_T$
 $\Delta F(L_P, M_D, S_T) = \frac{1}{\sqrt{L_P}} \Delta L_P + \frac{1}{\sqrt{M_D}} \Delta M_D + \frac{1}{\sqrt{S_T}} \Delta S_T$

'achromatic response'-description sub function $q[k(u-u_0)]$
 with $u = \log L$ ($L =$ luminance)
 $u_0 = \log L_u$ ($L_u =$ surround luminance)
 $q[k(u-u_0)] = 1 + 1/[1 + \sqrt{2} e^{k(u-u_0)}]$
sub function values:
 $q[k(u-u_0) \rightarrow +\infty] = 1$
 $q[k(u-u_0) = 0] = \sqrt{2}$
 $q[k(u-u_0) \rightarrow -\infty] = 2$

'achromatic response'-description function $Q_{1m}[k(u-u_0)]$
 with $u = \log L$ ($L =$ luminance)
 $u_0 = \log L_u$ ($L_u =$ surround luminance)
 $Q_{1m}[k(u-u_0)] = \frac{1}{\ln \sqrt{2}} \ln q[k(u-u_0)] - m$
function values with $l = m = 1$:
 $Q[k(u-u_0) \rightarrow +\infty] = -1$
 $Q[k(u-u_0) = 0] = 0$
 $Q[k(u-u_0) \rightarrow -\infty] = 1$

'achromatic response'-discrimination as function of relative light density $h = \ln H = k(u-u_0)$, $\ln =$ natural log.
 $Q' = \frac{dQ}{dh} = \frac{d}{dh} [1 + 1/(1 + \sqrt{2} H)] / (1/\ln \sqrt{2})$
 $= -\sqrt{2} / [\ln \sqrt{2} (1 + \sqrt{2} H)(2 + \sqrt{2} H)]$
function values:
 $Q'[k(u-u_0) \rightarrow +\infty] = 0$
 $Q'[k(u-u_0) = 0] = -0,5$
 $Q'[k(u-u_0) \rightarrow -\infty] = 0$

luminance discrimination possibility $L/\Delta L$ as function of H
 with: $L = 10^u$, $H = e^{-h} = 10^{-\log e k(u-u_0)}$
 $dL/d u = \ln 10 \cdot L$, $dH/d u = k \cdot H$
 $\frac{L}{\Delta L}$ follows: $L/\Delta L = [kH/(dH \ln 10)]$
 $\frac{L}{\Delta L} = \text{const } H / [(1 + \sqrt{2} H)(2 + \sqrt{2} H)]$
sub function values:
 $Q'[k(u-u_0) \rightarrow +\infty] = 0$
 $Q'[k(u-u_0) = 0] = \text{maximum}$
 $Q'[k(u-u_0) \rightarrow -\infty] = 0$

double line element of Richter (1987) for the lighting technology with the luminance $L = f(L_P, M_D, S_T)$
 $F(L) = \int_{-\infty}^L (L/\Delta L) dL$ (relative L, M, S^2)
 $F(L) = i Q(H)$ ($u = u_0$)
 $F(H) = i Q(H) = \int i Q(H) dH$ ($u = u_0$)
 with: $k=1,4$ $k=1$ $i=1$ $\tilde{i}=2,0$
 $u = \log L$ $u_0 = \log L_u$ $\tilde{u} = \log L_u$
 $H = e^{k(u-u_0)}$ $\tilde{H} = e^{k(u-u_0)}$ $\tilde{H} = e^{k(u-u_0)}$

double line element of Richter (1987) for the lighting technology with the luminance $L = f(L_P, M_D, S_T)$
 $F(L) = \int_{-\infty}^L (L/\Delta L) dL$ (relative L, M, S^2)
 $F(L) = i Q(H)$ ($u = u_0$)
 $Q(H) = [\ln(1 + 1/(1 + \sqrt{2} H))] / (\ln \sqrt{2} - 1)$
Taylor-derivations:
 $\Delta F(L) = \frac{dF}{dL} \Delta L = i \frac{dQ}{dH} \Delta H$
 $= -i \sqrt{2} \Delta H / [\ln \sqrt{2} (1 + \sqrt{2} H)(2 + \sqrt{2} H)]$

see similar files of the whole serie: http://farbe.li.u-berlin.de/een3/een310n1.txt /ps; only vector graphic VG; start output see similar files: http://farbe.li.u-berlin.de/een3/een3.htm

TUB registration: 20230701-een3/een310n1.txt /ps application for evaluation and measurement of display or print output TUB material: code=thadta