

**Lightness L\* and differences Delta Y or dY in the colour space TUBJND**

The lightness L\* is defined by the equation:

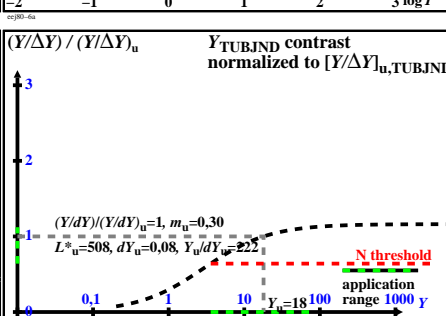
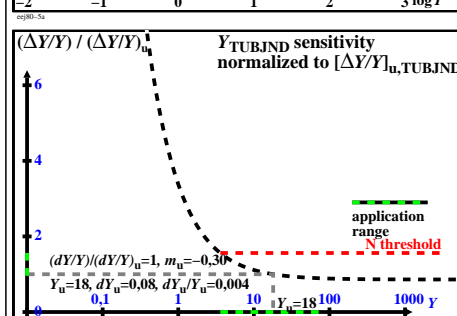
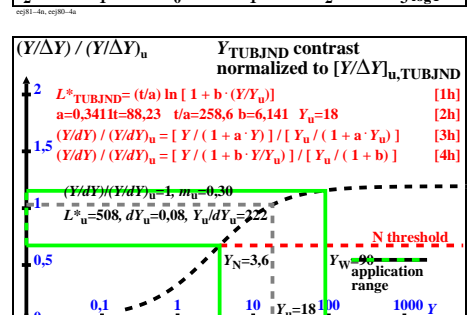
$$L^*_{TUBJND} = (t/a) \ln [1 + a \cdot Y] = (t/a) \ln [1 + b \cdot (Y/Y_u)]$$

a=0,3411 t=88,23 t/a=258,6 b=6,141 Y\_u=18

This equation is based on psychophysical BAM-research results  
 $dY = (s + q \cdot Y) / c$ , see Richter BAM-Forschungsbericht 115, 1985

There are different versions of these equations, all with equal content  
 $dY = (A_1 + A_2 \cdot Y) / A_0$ , see CIE 230; Eq. (A.7a)  
 $dY = (1 + a \cdot Y) / t = (1 + b \cdot (Y/Y_u)) / t$   
 $A_1 = s = 0,0170$   $A_2 = q = 0,0058$   $A_0 = c = 1,5$  (c=scaling constant)

The lightness L\* is called the line element of dY, see the equation

$$L^*_{TUBJND}(Y) = \int \frac{t \cdot dY}{1 + a \cdot Y} = (t/a) \ln [1 + a \cdot Y]$$


**Line-element examples for grey samples (0,2 ≤ x = Y/Y\_u ≤ 5)**

F(x) is called the line-element function of f(x).  
 The following relations are valid for x=Y/Y\_u=18:

$$\frac{d[F(x)]}{dx} = f(x)$$

$$F(x) = \int \frac{f'(x)}{f(x)} dx$$

Example for all normalized tristimulus values x=Y/Y\_u, for example for Y\_N=3,6, Y\_u=18, Y\_W=90.

$$\frac{d(t \ln(1+b \cdot x))}{dx} = \frac{tb}{1+b \cdot x}$$

$$t \ln(1+b \cdot x) = \int \frac{tb}{1+b \cdot x} dx$$
