

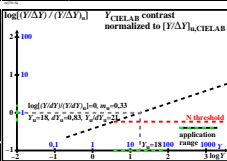
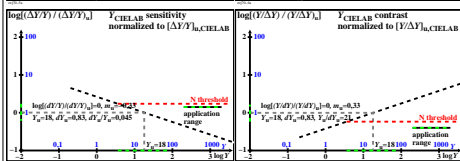
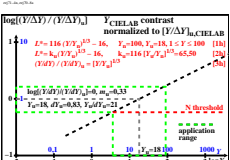
Lightness  $L^*$  and differences  $\Delta Y$  or  $dY$  in the colour space CIELAB

The lightness  $L^*$  is defined by the equation:  
 $L^* = 116(Y/25.38)^{0.425} - 16$ ,  $Y_a = 100, Y_a \cdot 18, 1 \leq Y \leq 100$  (1)

This CIELAB equation as function of relative tristimulus values is  
 $L^* = k_a(Y/25.38)^{0.425} - 16$ ,  $k_a = 116(Y_a/25.38)^{0.425} - 65.50$  (2)

The tristimulus values of difference  $dY$  is for  $dL^* = 1$   
 $dY = (3/116)(Y/25.38)^{2.25} = a(Y/25.38)^{2.25} = b(Y/25.38)^{2.25}$  (3)  
 $a = 0.557, b = 6.516$  (4)

Relative normalized differences are  $dY/dY_a$  and  $(Y/dY)/(Y/dY)_a$   
 $dY/dY_a = (Y/25.38)^{2.25} / (Y_a/25.38)^{2.25}$  (5)  
 $(Y/dY)/(Y/dY)_a = (Y/25.38)^{1.125} / (Y_a/25.38)^{1.125}$  (6)



Line-element examples for grey samples ( $0.25 \leq x = Y/Y_a \leq 5$ )

$F(x)$  is called the line-element function of  $f(x)$ .  
 The following relations are valid for  $x = Y/Y_a = 1/18$ :

$\frac{dF(x)}{dx} = f(x)$  (1)  
 $F(x) = \int \frac{f(x)}{x} dx$  (2)

Example for all normalized tristimulus values  $x = Y/Y_a$ ,  
 for example for  $Y_a = 3.6, Y_a = 18, Y_a = 90$ .

$\frac{d}{dx} [k_a(x)^{1/3} - 16] = \frac{1}{3} k_a(x)^{-2/3} / 3$  (3)  
 $k_a(x)^{1/3} + \text{const} = \int \frac{k_a(x)^{-2/3}}{3} dx$  (4)

