

Lightness L* and differences ΔY or dY in the colour space TUBJND

The lightness L* is defined by the equation:

$$L^*_{TUBJND} = (t/a) \ln(1+a \cdot Y) = (t/a) \ln(1+b \cdot (Y/Y_u))$$

a=0.3411 t=88.23 u/a=258.6 b=6.141 Y_u=18 [1] [2]

This equation is based on psychophysical BAM-research results

$$dY = (s + q \cdot Y) / c$$

see Richter BAM-Forschungsbericht 115, 1985 [3]

There are different versions of this equations, all with equal content

$$dY = (A_1 + A_2 \cdot Y) / A_0$$

see CIE 230; Eq. (A.7a) [4]

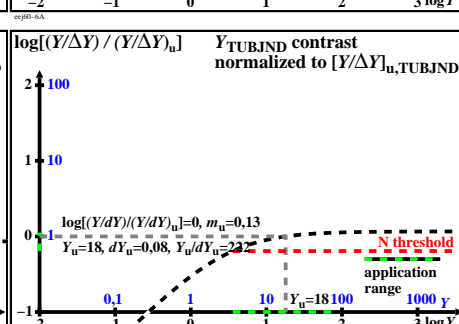
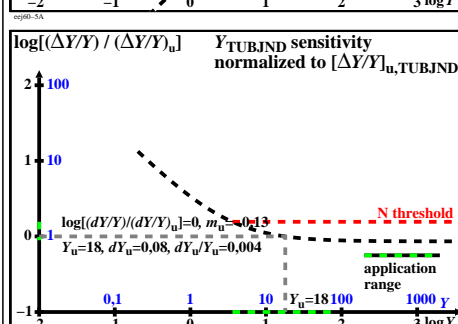
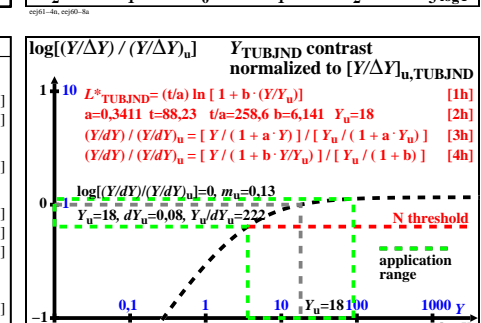
$$dY = (1 + a \cdot Y) / t = (1 + b \cdot (Y/Y_u)) / t$$

A_1=s=0.0170 A_2=q=0.0058 A_0=c=1.5 (c=scaling constant) [5] [6]

The lightness L* is called the line element of dY, see the equation

$$L^*_{TUBJND}(Y) = \int \frac{t \cdot dY}{1+a \cdot Y} = (t/a) \ln(1+a \cdot Y)$$

[7]



Line-element examples for grey samples (0.2 ≤ x = Y/Y_u ≤ 5)

F(x) is called the line-element function of f(x).

The following relations are valid for x=Y/Y_u=1/18:

$$\frac{d[F(x)]}{dx} = f(x)$$

[1]

$$F(x) = \int \frac{f'(x)}{f(x)} dx$$

[2]

Example for all normalized tristimulus values x=Y/Y_u, for example for Y_N=3.6, Y_u=18, Y_W=90.

$$\frac{d(t \ln(1+b \cdot x))}{dx} = \frac{tb}{1+b \cdot x}$$

[3]

$$t \ln(1+b \cdot x) = \int \frac{tb}{1+b \cdot x} dx$$

[4]

