

## Hyperbolic response function of achromatic vision space $T^*_{HYP3X}$

nonlinear color terms	name and relationship with test field luminance $L$	notes
<b>threshold sum</b> $T^*_{HYP3X}$ $T^*_{HYP3}$	$T^*_{HYP3X} = A / (1 + A_2 / L^t); \quad X=1/L^t=L^{-t}$ $= A_1 / (1 + A_2 \cdot X); \quad dX/dL=-t \cdot L^{-t-1}$ $= A_1 \cdot [1 + A_2 \cdot X]^{-1}$	<i>T. Seim 2014:</i> exponent: $t = 0,8$ for presentation time: $t_p = 0,1\text{s}$ of Avramopoulos experiments 1989
<b>CIE luminance contrast sensitivity threshold</b> $L / dL$	$dT^*_{HYP3X} / dX = -A_1 \cdot A_2 \cdot [1 + A_2 \cdot X]^{-2}$ $dT^*_{HYP3X} / dL = dT^*_{HYP3X} / dX \cdot dX / dL$ $dT^*_{HYP3X} / dL = A_1 \cdot A_2 [1 + A_2 \cdot X]^{-2} t \cdot L^{-t-1}$ <i>for <math>dT^*_{HYP3X}=1</math>, and multiplication with <math>L</math>:</i> $L / dL = A_1 \cdot A_2 [1 + A_2 \cdot X]^{-2} t \cdot L^{-t}$ $= A_1 \cdot A_2 \cdot t \cdot / (L^t [1 + A_2 / L^t]^2)$	Hyperbolic function: $T^*_{\max} = A_1$ $T^*_{\text{average}} = 0,5 \cdot A_1$ $A_{2x} = A_2^{1/t}$
<b>CIE luminance difference threshold <math>dL</math></b>	$dL = L \cdot (L^t [1 + A_2 / L^t]) / (A_1 \cdot A_2 \cdot t)$ $= (L^t + A_2)^2 / (A_1 \cdot A_2 \cdot t \cdot L^{t-1})$	