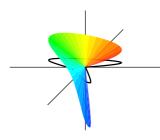
1

Output Linearization Methods for Displays, Printers, and Offset Print

White paper for a standard document (technical report or other) for discussion, 2013-04, see 59 pages 1,3 MB http://130.149.60.45/~farbmetrik/OUTLIN13_01.PDF



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see: http://www.li.tu-berlin.de

At the 2011 CIE Division 8 meeting in South Africa CIE Division 8 decided the

Reportership CIE R8-09 Output Linearization Methods for Displays and Printers

Terms of Reference

Make a report on proposals for the application of output linearization methods. The report may cover the device and elementary hue output of displays and printers.

Reporter: Klaus Richter (DE), email: klaus.richter@mac.com, Internet: Berlin University of Technology (TUB): http://130.149.60.45/~farbmetrik

In 2012 a publication **Colour and Colour Vision - Elementary colours in colour image technology** has applied output linearization methods for the sRGB display output, the offset print output on different papers, and the laser printer output. Some colorimetric results of this publication are included in this report

The paper "Colour and Colour Vision" is available in different versions for monitor, offset, and printer output, and in German, English and other languages, for example French, Spanish, and Italian (intended), see http://130.149.60.45/~farbmetrik/color

For the newest version of this document on output linearization see http://130.149.60.45/~farbmetrik/outlin

1 Scope

A digital file with 9x9x9 *rgb* equally spaced input data is used to produce 729 colours on a colour display. The digital file format may be *PostScript* (PS) or *Portable document* (PDF). Within the different file formats the 9 step colour scales are defined by 9 digital values between 0 and 1, for example by 0, 1/8, 2/8 to 8/8 in RGB coordinates. The first output is measured and by the linearization method (LM) of this Technical Report, a visually equally spaced output is produced in relative CIELAB units, for example between the white display and a 48 step hue circle of maximum device chroma for these hues.

This Technical Report produces tables $rgb \rightarrow rgb'^*$ (dash-star coordinates, compare ISO/IEC 15775) for output in device space and also tables $rgb \rightarrow rgb'^*$ according to CIE R1-47:2009 for the device independent elementary hue output. The output is linearized for the eight viewing conditions defined in ISO 9241-306 for eight ambient light reflections on the display.

There are tables of output values and graphs for the first and linearized output. This method produces a linear relationship between the linear digital input data and the output data on a visual relative CIELAB scale in any hue plane. The method is applicable for systems that do not have colour management or as a linearization method for devices that could be used as a setup_state for colour management. The aim of this method is to produce equal CIELAB spacing. The equal spacing of the steps achieved in the linearization method may be adapted to various purposes. The accuracy of this method is expected to be within ΔE^*_{ab} =1 of CIELAB. However, the standard deviation of ΔE^*_{ab} of colour output on different positions of the display, or on the printer, or in offset print is for example between ΔE^*_{ab} =0,5 (photo printer) and ΔE^*_{ab} =5 (laser printer). For real output the accuracy is therefore device-dependent and in many cases larger than ΔE^*_{ab} =1.

NOTE 1: This Technical Report applies the Technical Report ISO/IEC TR 19797 for output linearization of printer to displays and to the eight luminance reflections L_r between 0 and 40% according to ISO 9241-306, Annex D. Similar as for printers this Technical Report could be used as a setup_state for colour management. In addition the affine transformation of Fig. 25 on page 36 is a colour management strategy. It is intended that for example the user can choose one mode of eight for the whole display output similar as in ISO 9241-306.

NOTE 2: The effectivity of the cylindrical and relative triangle coding in hue planes is by a factor 10 more effective compared to the fixed 8-bit coding in the range -128 and 127 for a^* and b^* of CIELAB and 0 and 100 for L^* of CIELAB. The ten times higher effectivity and accuracy of coding is based on data for the *sRGB* color space. CIE 168 shows that the *sRGB* gamut fills 20% of this CIELAB coding gamut. For the standard luminance reflection $L_r = 2,5\%$ in the office the *sRGB* gamut fills only 50% of the standard *sRGB* gamut in the dark room.

2 Conformance

A paragraph.

3 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies

CIE 15:2008, Colorimetry

CIE 17.4:1983, International lighting vocabulary, 4th ed. (Joint publication IEC/CIE)

CIE 168:2005: Criteria for the Evaluation of Extended-Gamut Colour Encoding

CIE R1-47:2009, Hue angles of elementary colours, see for download under REPORTS http://div1.cie.co.at

DIN 33872-1 to 6:2010, Information technology - Office machines - Method of specifying relative colour reproduction with YES/NO criteria, see for download of test charts http://www.ps.bam.de/33872E

ISO EN DIN 9241-306:2008, Ergonomics of human system interaction – Part 306: Field Assessment methods for electronic visual displays

ISO 11664-4:2008(E)/CIE S 014-4/E:2007: Joint ISO/CIE Standard: CIE Colorimetry — Part 4: 1976 L*a*b* Colour Space (CIELAB)

ISO 15076-1:2005, Image technology colour management -- Architecture, profile format and data structure -- Part 1: Based on ICC.1:2004-10

ISO/IEC 15775:1999, Information Technology – Office machines – Method of specifying image reproduction of colour copying machines by analog test charts – Realization and application

ISO/IEC 15775/Amd.1, Information technology – Office machines – Machines for colour image reproduction – Method of specifying image reproduction of colour copying machines by analog test charts – Realization and application – Amendment 1

ISO/IEC TR 19797:2004, Information technology – Office machines – Machines for colour image reproduction – Device output for 16-step colour scales, output linearization method (LM) and specification of the reproduction properties

ISO/IEC TR 24705:2005, Information technology – Office machines – Machines for colour image reproduction – Method of specifying image reproduction of colour devices by digital and analog test charts, see for download of test charts http://www.ps.bam.de/24705TE

SS 019100:1997, Colour notation system, and SS 019102:2004, NCS ATLAS (NCS Colour atlas)

4 Terms and definitions

3.1

3

Colorimetric data Three colour data with a defined and simple relation to the standard CIELAB data $LAB^* = L^*$, a^* , b^* or $LCH^* = L^*$, C^*_{ab} , h_{ab}

NOTE 1: There is a family of colorimetric *standard* CIELAB data *LAB**, of colorimetric *adapted* data *LAB**_{*a*}, and of colorimetric *relative* data *lab**, compare table C.1.

NOTE 2: The family of the colorimetric *standard* CIELAB data *LAB** has two equivalent versions *LAB*LAB** = *L**, *a**, *b** and *LAB*LCH**= *L**, *C**_{*ab*}, h_{ab} , compare table C.1.

NOTE 3: The family of the colorimetric *adapted* CIELAB data LAB_a^* has two equivalent versions $LAB_a^* LAB_a^* = L_a^*$, a_a^* , b_a^* and $LAB_a^* LCH_a^* = L_a^*$, C_{ab}^* , h_{ab} , compare table C.1.

NOTE 4: The family of the colorimetric *adapted* data LAB_a^* has a defined and simple relation to the standard CIELAB data LAB^* . The adapted lightness L^*_a is identical to the standard lightness L^* , compare table C.1. In some applications corresponding colour values are necessary which then use the index a, for example the tristimulus values X_a , Y_a , Z_a of the chromaticity values x_a and y_a . For example in Fig. 8 on page 12 the colorimetric *adapted* data LAB^*_a are calculated from the colorimetric *standard* CIELAB data LAB^* and shown as colour samples.

NOTE 5: The family of the colorimetric *relative* data *lab* has many equivalent versions, for example

 $lab*lab* = l^*$, a^*_{a} , b^*_{a} , $lab*lch^* = l^*$, c^* , h^* , $lab*ncu^* = n^*$, c^* , u^* , and $lab*cmy^*_e = c^*_e$, m^*_e , y^*_e , compare Table B.1.The colorimetric *relative* data *lab** have a defined and simple relation to the colorimetric *adapted* CIELAB data *LAB**_a. For example in Fig C.2 the colorimetric relative data *l**, *c**, *h** are calculated from the adapted CIELAB data L^*_a , C^*_{ab} , and h_{ab} , and are shown as colour samples.

NOTE 6: The colorimetric data LAB^* , LAB^*_a , and lab^* are listed together with the names and abbreviations in table E.1. Additional coordinates, for example colour deepness d^* , brilliantness i^* , and whiteness w^* are not defined in table E.1. The linear relationship, for example between these coordinates and $lab^*rgb^*_e$ is shown in the paper "Colorimetric supplement to DIN 33872-1 to -6 [1] and in Annex C.

3.2

colorimetric space CIELAB

three-dimensional space for the geometrical representation of colorimetric data with rectangle or cylindrical standard or adapted CIELAB coordinates.

NOTE 1: The colorimetric data may be of the type *rectangle*, for example $LAB^*LAB^* = LAB^*$, $LAB^*_aLAB^*_a = LAB^*_a$ or of the type cylindric, for example $LAB^*LCH^* = LCH^*$, $LAB^*_aLCH^*_a = LCH^*_a$

3.3

Colorimetric isometric data

relative CIELAB data *lab*tab** or *lab*tch**, for which the calculated colorimetric differences correspond to a high degree with the visual differences.

3.4

Colorimetric isometric space

Three-dimensional space for the geometrical representation of the relative CIELAB data *lab*tab** or *lab*tch*, where the differences in the space correlate to a high degree with the visual differences of a device system.

NOTE 1: This space is to a high degree isometric in the sense of perception and shows a high degree of visual uniformity.

NOTE 2: If the coordinates *lab*t**, *lab*c**, and *lab*h** are used, then the three-dimensional visual representation of the 16step colour series between White W and Black N and the six chromatic colours is a double cone, which is called a Natural Colour Connection Space NCCS

NOTE 3: For any device system the colorimetric data lab^*t^* in the range 0 to 1 are used for the vertical axis, and the colorimetric data lab^*c^* in the range 0 to 1 are used for the horizontal axis. For the 16-step colour series equal visual differences correspond to equal geometric differences.

NOTE 4: Fig. A.3 and A.4 shows colour samples in the colorimetric isometric space of the type cylindrical with the coordinates *tch**.

3.5

Device system colours

Output colours of a device system which are dependent on the hard and software properties including the viewing illumination.

NOTE 1: Examples are reflective colours on a printer, the light colours of a monitor or the projected colours of data projectors.

3.6

Normal colour vision

Vision perception, which can be determined by a colour vision test, and which corresponds to the CIE-2 degree observer according to CIE 15 or DIN 5033.

NOTE: The normal colour vision of an observer is for example tested according to DIN 6160 by the Anomaloscope of *Nagel* or with *Ishihara* test charts.

3.7

Colour difference

Amount of the perceived difference between two colours.

NOTE: The colour difference ΔE^*_{ab} between two colours is calculated according to ISO 11664-4 with the CIELAB colour difference formula.

3.8

Relative colour difference

Amount of the perceived difference of at least three colours A, B, and C.

NOTE 1: The colorimetric specification of the relative colour differences is given by comparison of the relative colour difference between A-B and B-C.

NOTE 2: In the standard series DIN 33872 the relative colour difference of 3-, 5-, 9-, 16-, and 17-step colour series is evaluated visually and/or specified by colorimetry.

3.9

Colour image

visual presentation of colours in a two dimensional arrangement.

NOTE: For example the data of a colour image are defined by 960 times 640 pixels as *rgb* or CIELAB data within a digital test chart.

3.10

Colour image reproduction

Visual evaluation or colorimetric specification of the reproduction of a colour image.

NOTE: For the reproduction for example the rgb-data in a digital file are used for the output.

3.11

Relative colour image reproduction

Reproduction of a colour image for which the hue of any colour and the relative colour differences of the arrangement remain constant.

NOTE 1: Equally spaced 17-step colour series in a hue triangle, for example between Black and White, Chromatic and White and Chromatic and Black remain equally spaced by visual evaluation for any output system.

NOTE 2: The relative colour differences of colour images are only slightly dependent by the chromaticity of the illumination compared to large colour data differences of single samples in the office environment. For the office illumination see ISO 8995 and DIN V 18599-4.

NOTE 3: For monitors and data projectors the relative colour differences of colour images are highly dependent on the reflections of the office illumination on the monitor surface and the projection screen, see DIN EN ISO 9241-306. This standard describes methods for output linearization depending on the reflection properties.

3.12

Colour order system

Three-dimensional order of colours by visual and/or colorimetric criteria.

NOTE 1: Examples for the order according to visual criteria are the colour order systems *Natural Colour System (NCS)*, *Ostwald, Munsell* and the *Optical Society of America (OSA)*, compare [1].

NOTE 2: Examples for the order according to colorimetric criteria are the colour order systems according to DIN 6164-1 and the *RAL Design System* with a regular cylindric order in the CIELAB colour space for the CIE standard illuminant D65 and the 10 degree observer, compare [1].

5 Symbols (and abbreviated terms)

PS PDF	PostScript Portable Document Format
ORS18 TLS00 TLS18	Offset Reflektive System with lightness $L_a^* = 18$ for Black N Television Light System with lightness $L_a^* = 0$ for Black N Television Light System with lightness $L_a^* = 18$ for Black N (standard for offset and displays)
RYGCBM _d	Device (d) colours (Colours of the device hue hexagon): Red (R_d), Yellow (Y_d), Green (G_d), Cyan blue (C_d), Blue (B_d), and Magenta (M_d)
RYGBCBM _e	Elementary (e) colours (Colours of the elementary hue hexagon): Red (R_e), Yellow (Y_e), Green (G_e), Cyan blue (C_e), Blue (B_e), and Magenta (M_e)
D65	Daylight with correlated colour temperature 6500° Kelvin (CIE 15: standard illuminant)

6 Start and linearized output of RGB displays for standard luminance contrast

6.1 Output of a 16 step device colour circle and definition of elementary colours

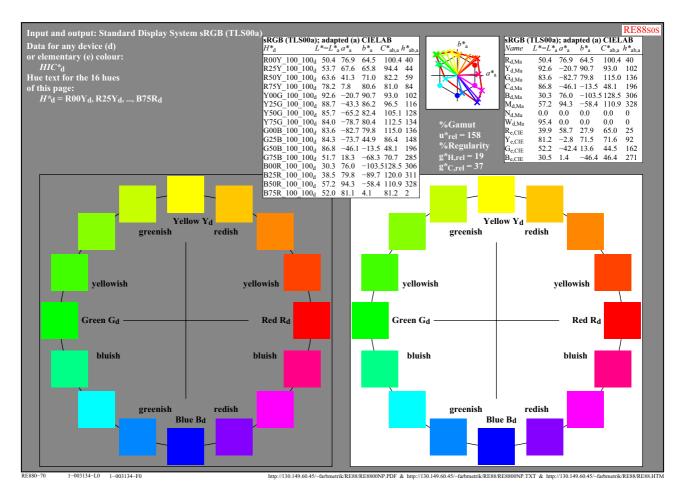


Fig. 1 - Hue circle with 16 colour steps and with device (d) colours

Fig. 1 shows a 16 step hue circle of device (d) colours. The four colours Red R_d , Yellow Y_d , Green G_d und Blue B_d are produced by the rgb_d data $(1, 0, 0)_d$, $(1, 1, 0)_d$, $(0, 1, 0)_d$, and $(0, 0, 1)_d$. The CIELAB data L^* , a^* , b^* , C^*_{ab} and h_{ab} are given in the right table. The hue angles $h_{ab,d}$ 40, 102, 136, 306 belong to the output colours on the standard sRGB display. For comparison the elementary hue angles $h_{ab,d}$ of the CIE test colours 9 to 12 of CIE 13.3 are given. These four colours with the elementary hue angles $h_{ab,d} = 25$, 92, 162, and 271 represent the CIE elementary hue angles according to R1-47. The standard deviation of the hue angle is +/-4 for R_e , Y_e , and G_e , and +/-8 for B_e .

Fig. 1 includes a special colour code HIC_{d}^{*} , for example HIC_{d}^{*} =R00Y_100_100_d for device red. According to DIN 33872-1 the three colour coordinates HIC_{d}^{*} are called hue text H^{*} , Brilliance I^{*} and Chroma C^{*} . Brilliance I^{*} is equal to 100 times the relative brilliance i^{*} and Chroma C^{*} is equal to 100 times of the relative chroma c^{*} .

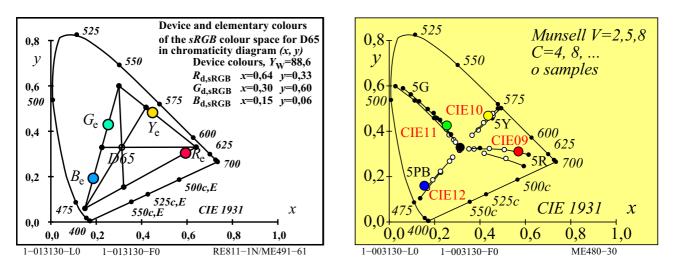
In addition the CIELAB data L^* , a^* , b^* , C^*_{ab} and h_{ab} are given. For many real applications for black N and white W there is a small difference compared to the ideal values ($a^*_N=0$, $b^*_N=0$) and ($a^*_W=0$, $b^*_W=0$). Then some "adaptation" (index a) is necessary for a useful calculation of the hue angles. For the standard (ideal) sRGB device the coordinates L^*a^* , b^* , C^*_{ab} , h_{ab} and ($L^*a^*b^*C^*_{ab}h_{ab}$)_a are identical, compare Fig. 9 on page 13 and Annex B on page 52.

Usually for the values $rgb_{\rm d}$ (index _ unspecified) the device blue is produced and this colour appears reddish blue. The sRGB hue angle is $h_{\rm ab,d}$ = 305. However the elementary hue angle is $h_{\rm ab,e}$ =272.

Achromatic colours, intermediate colours	Chromatic colours, Elementary colours	Chromatic colours, Device colours
five achromatic colours:	"Neither-nor"-colours	TV, Print (PR), Photo (PH)
N black (French noir)	four elementary (e) colours:	six device (d) colours:
$D dark grey$ $Z central grey$ $H light grey$ $W white$ $two intermediate \ colours:$ $C_{e} = G50B_{e} \ green-blue$ $M_{e} = B50R_{e} \ blue-red$	$R = R_e \text{ red}$ $neither \text{ yellowish nor bluish}$ $G = G_e \text{ green}$ $neither \text{ yellowish nor bluish}$ $B = B_e \text{ blue}$ $neither \text{ greenish nor reddish}$ $J = Y_e \text{ yellow (French jaune)}$ $neither \text{ greenish nor reddish}$	$C = C_{d}$ cyan blue (cyan) $M = M_{d}$ magenta red (magenta) $Y = Y_{d}$ yellow $O = R_{d}$ orange red (red) $L = G_{d}$ leaf green (green) $V = B_{d}$ violet blue (blue)

Table 1 - Device colours and elementary colours with visual criteria

Table 1 shows the device colours (index d) and the elementary colours (index e) and the visual criteria for the elementary colours. ISO/IEC 15775 uses for example the letters O, L and V instead of R_d , G_d , and B_d which indicate the difference to the letters R, G, and B. However, in this paper we prefer to use the index **d** or **e** to distinguish between device end elementary colours or hues.



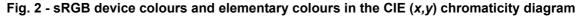


Fig. 2 shows the six device colours (black balls) and the four elementary colours which can be produced from these device colours in the CIE chromaticity diagram (left). The four CIE test colours no. 9 to 12 which represent the elementary hues (compare the following) are shown together with the samples of the hues 5R, 5Y, 5G and 5PB of the *Munsell* colour order system for the three *Values* V=2,5, and 8 (approximately $L^*=20$, 50, 80 in CIELAB) (right).

6.2 ISO request to the CIE for an elementary RGB system and work results within the CIE

Conclusion 31/2007 ISO TC159/SG4/WG2 Ergonomics – Visual Display Requirements

ISO TC159/SG4/WG realizes that the colour spaces CIELAB and CIELUV of *CIE Division 1* will soon become ISO/CIE standards. In applications we use these CIE colour spaces and *device-dependent* relative RGB colour spaces. For users of visual display systems a *device-independent* RGB colour space is useful. This produces via software the elementary hues Red, Green and Blue for the RGB data 100, 010 and 001 and equally spaced output in CIE colour spaces for equally spaced RGB input. We recommend that *CIE Division 1* study the colorimetric definition of such a space, which can be used in visual display applications.

Remark: We have realized that an example colour space of this type is published in CIE X030:2006, p. 139–144. unanimous vote (Finland, Germany, Japan, Korea, Netherlands, Schweden, USA) SE380-1

Fig. 3 - Conclusion of ISO TC159/WG4/SC2 for a device-independent RGB colour space

Fig. 3 shows a conclusion of ISO TC159 which includes a request of the ISO committee "Visual Display Requirements" for the definition of the elementary hues by CIE Division 1 "Colour and Vision". Different ISO committees have problems with the application of colour in ISO International Standards and Technical Reports. CIE Division 1 is the appropriate body to study the colour problems and to produce guidance.

At the CIE meeting in Stockholm, June 2008, *CIE Division 1* decided to establish the CIE Reportership R1–47 **Hue Anles of Elementary Colours** by *Thorstein Seim (Norway)* in response to the request of ISO TC 159 **Visual Display Requirements** and to present the result at the next CIE meeting in Budapest 2009.

The report **CIE R1–47:2009 Hue Angles of Elementary Colours** lists in chapter 3.6 the average CIELAB hue angles 26, 92, 166, and 270 of *Miescher, NCS, and the CIE*.

CIE R1-47 recommends to use the CIELAB hue angles 25, 92, 162 and 271 of the CIE test colours no. 9 to 12 according to CIE 13.3 for the four elementary colours R_e , Y_e , G_e , and B_e .

For free download of CIE R1–47 see the CIE Division 1 web site http://cie.co.at *under MINUTES & REPORTS*

SE380-3

Fig. 4 - Decision of CIE Division 1 and Report CIE R1-47 with definition of elementary hue angles

Fig. 4 shows the decision and answer of CIE Division 1 on the request of ISO TC159. The four CIELAB hue angles $h_{ab,e} = 25$, 92, 162 and 271 of the CIE test colours no. 9 to 12 according to CIE 13.3 are proposed for the four elementary colours R_e , Y_e , G_e , and B_e . This is the CIE basis to define the device-independent rgb_e coordinates which produce the visual elementary hues. The report includes the standard deviation of the elementary hue angles. For R_e , Y_e , and G_e the values $h_{ab,e}$ =+/-4, and for B_e the value $h_{ab,e}$ =+/-8 is given. However, for example the standard sRGB colour space produces $h_{ab,d}$ =305 and an example printer of a leading printer company h_{ab} =260. Both hue angles are outside the visual range $h_{ab,e}$ =271+/-8, and in addition the shift is in the display case towards the reddish and in the printer case towards the greenish side. Therefore, if the proposal $h_{ab,e}$ =271+/-8 of CIE R1-47 is reached on most devices, this will be a large improvement for users.

One must consider that there are hundreds of *RGB* colour spaces, including he ISO standard spaces *sRGB*, *RIM RGB*, *ROM RGB*, *Adobe RGB*, *ECI RGB*. All are device specific and not related to the visual elementary hue definition of CIE R1-47.

6.3 Output of the elementary colour circle

The output of the elementary colour circle on a standard sRGB display needs hue shifts, compare Fig. 32 on page 43. For example the three rgb_d values (0 0 1)_d (d=device) produce the hue angle $h_{ab,d}$ =305 and the three rgb_e values (0 0 1)_e (e=elemntary) produce the hue angle $h_{ab,e}$ =271. For a 16 step device and elementary hue circle the hue angles $h_{ab,d}$ and $h_{ab,e}$ are given in the tables of Fig. 1 and 4 respectively. For example for the device hue Y00G_d and the elementary hue Y00G_e the hue angles are $h_{ab,d}$ =102 and $h_{ab,e}$ =92. The device hue angle $h_{ab,d}$ =102 produces a greenish yellow compared to the elementary hue angle $h_{ab,e}$ =92 with the standard deviation +/-4. The colour code Y00G_100_100_e belongs to the rgb values rgb_e =(1 1 0)_e. The first value Y00G_e is called the hue text, the following two values are 100 times the relative brilliance *i** and the relative chroma *c**. One can use the capital letters *I** = 100 *i** and *C** = 100*c**. There are two equations which allow to transform betweenalues of rgb^* and *c** and *i** for both the device and the elementary colours:

$$c^* = max (rgb^*) - min (rgb^*)$$

$$i^* = max (rgb^*)$$

Example: For a greyish red with rgb*=(0,75, 0,50, 0,25) it is valid $c^*=0,5$ and $i^*=0,75$ (compare also Fig. 14 on page 18).

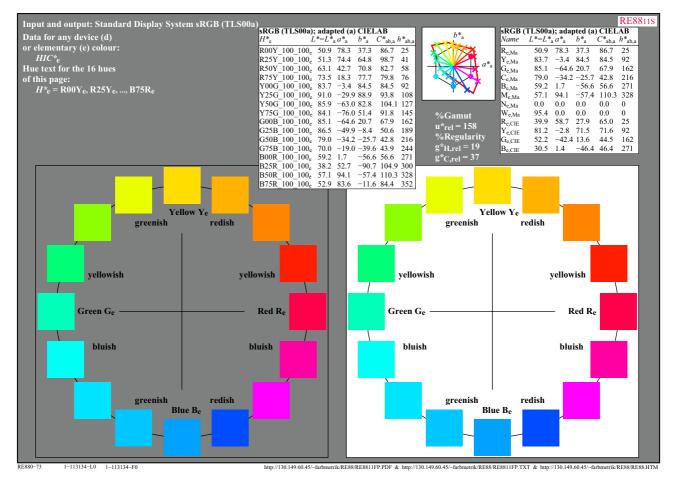


Fig. 5 - 16 step hue circle of elementary (e) colours

Fig. 5 shows a 16 step hue circle which shall produce the elementary colours R_e , Y_e , G_e , and B_e according to the criteria given in the figure. There may be a small visual difference on the grey and white background. One may realize that Yellow $Y_e=Y00G_e$ is darker compared to the next greenish step $Y25G_e$. This is a special property of the sRGB systems and not of standard offset. Y_e is the additive mixture of approximately the lighter colour $Y25G_e$ and the much darker colour $R75Y_e$. Therefore $Y_e=Y00G_e$ appears darker compared to $Y25G_e$.

6.4 ISO/IEC request to the CIE for a human visual RGB system and work results within CIE

Resolution Busan 18/2009 of ISO/IEC JTC1/SC28 "Office Equipment" SC28 Review of the AWG recommendation on jn28n1280 (DIN 33872-1 to 6)

The German proposal included the concept of a human visual RGB. SC28 recognizes the importance of correct understanding of the human visual system and the potential importance and application of this understanding to office equipment and office systems. SC28 welcomes the German plan to continue development of the human visual RGB within *CIE Division 1 and Division 8*.

In addition SC28 welcomes a new proposal from Germany in the future based on this CIE human visual RGB work, potentially in relation to AWG/PWG5 NWI-9

(Office colour space).

unanimous vote (Austria, China, Germany, Japan, Korea, USA)

SE380-5

Fig. 6 - Resolution on a human visual RGB of ISO/IEC JTC1/SC28 Office Equipment

Fig. 6 shows the Resolution *Busan* 18/2008 of ISO/IEC JTC1/SC28 *Office Equipment*. An English translation of the German Standard series DIN 33872-1 to 6, see http://www.ps.bam.de/33872E, has been discussed in SC28. According to Fig. 7 further ISO processing in SC28 has been stopped until a human visual RGB system is developed within CIE Division 1 and 8.

The German standard series DIN 33872-1 to -6 is addressed to many applications of different specialized ISO committees, for example TC 42 (Photography), TC 130 (Graphic Technology), TC 159 (Displays, compare Fig. 3 on page 8), and ISO TC 171 (Document Management). Only CIE Division 1 has the broader view and is in addition the appropriate International Standard Body for "Colour and Vision". Therefore it is a German wish to proceed in this area by a CIE Technical Report which in addition may be applied in different ISO committees.

At the CIE meeting in South Africa, June 2011, *CIE Division 1* decided to establish the Reportership CIE R1–57 Border between Luminous and Blackish Colours by *Thorstein Seim (Norway)* in response to the resolution 18/2009 of ISO/IEC JTC1/SC28.

in response to the resolution 18/2009 of ISO/IEC JTC1/SC28.

In addition CIE Division 8 decided to establish the Reportership

CIE R8–09 Output Linearization Methods for Displays and Printers by *Klaus Richter (Germany)* in response to the same resolution 18/2009 of ISO/IEC JTC1/SC28.

Both reports CIE R1-57 and CIE R8-09 have relations and may appear during 2013 at the CIE web site.

Possible Result: Definition of a *device-independent visual RGB*^{*}_e system as response to the request of SC28. All surface colours define a hue circle of maximum chroma located within the CIE (x,y) chromaticity diagram. CIELAB chroma C^*_{ab} and lightness L^* of this circle as function of hue h_{ab} serves as reference points of a *device-independent visual RGB*^{*}_e system (compare the reference C^*_{ab} , L^* hue circle of the *NCS* system). SE380-7

Fig. 7 - Present Work in CIE Division 1 and 8 to solve the request of ISO/IEC JTC1/SC28

Fig. 7 indicates that a larger step towards a human visual and device-independent RGB_{e}^{*} system may be reached in 2013 with the two proposed Reportership Reports CIE R1-57 and CIE R8-09.

A enlarged summary of this report here is intended to become the Reportership report CIE R8-09.

In. Fig. 6 SC28 has asked Germany to produce the output according to a human visual RGB. This paper and the Reportership report CIE8-09 seem to be a step in this direction. In addition this report allows to realize a lot of the user wishes according to DIN 33872-1 to -6

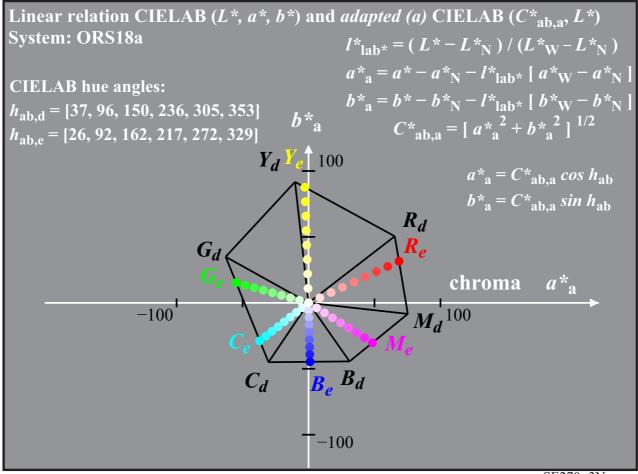
6.5 Standard documents which include input and output linearization and device colours Table 2 - Overview of ISO and DIN documents based on CIE visual and colorimetric differences

Input	Output	Input and outp	out media and	Technical Repo	ort	Method & Test:					
I		Input media				Application	(TR) or Standa		Linearization		
_	_	_		– Basis			ISO/IEC TR 24	4705	{DIN 33866-1 DIN 33872-1		
analog	analog	linearized ISO/ ISO/IEC-test cl		Haro	dcopy	Copier	ISO/IEC 15775		DIN 33866-2 JIS X 6933		
analog	digital	ISO/IEC-test cl	nart (hardcopy)	File		Scanner	ISO/IEC TR 24	4705	DIN 33866-4		
digital	analog	ISO/IEC-test cł	art (File)	∫Hardcopy		Printer	ISO/IEC TR 24	4705	DIN 33866-3 DIN 33872-2,4		
uigitui			luit (1 lie)	lSoftcopy		Display	ISO/IEC TR 24 ISO 9241-306	4705	DIN 33866-5 DIN 33872-2,4		
						le from an ISO/IEC-original scene:					
		n 16 equidistant				-					
			<u>^</u>	es fron					or printer output:		
ISO/IEC	C-input li	nearisation me			ISO/IEC-output linearisation method						
Input	Output	Application	Technical Rep (TR) or Stand	oort ard	Input	Output media	Application	oplication Technical Report (TR) or Standard			
Original scene	ISO/IEC Image	- Reference Image	ISO/IEC 1577 ISO/IEC TR 2		ISO/IEC File	- Hardcopy	Printer	ISC	/IEC TR 19797		
+ CIE- colours	File	File			ISO/IEC File	- Softcopy	Display		9241–306 ewing conditions		
						Softcopy	Display		E R8-09: 2013		
					ISO/IEC File	- Hardcopy	offset		ice space +		
					1 110	L Hardcopy	Printer	visu	ice-independent al RGB*eo space		
		1_000000_I	SE200-7N								

1-000000-L SE200-7N

Table 2 shows many International and National Standards and Technical Reports of ISO, IEC, DIN, and JIS. The common basis is the input or output evaluation or colorimetric specification based on CIE colorimetry. It may be the only standard document overview which is highly based on CIE colorimetry in this application field. Most of the standard documents are directed to only one application, for example copiers, scanners, printers, or displays. However there are multifunctional devices (a copier may be at the same time a scanner and a printer) which need in addition separate evaluations or specifications.

Table 2 shows that the intended Report CIE R8-09:2013 includes for the first time the three *devices display, offset, and printer* in **one** standard document. According to the terms of references of R8-09 (see page 1) not only the device-dependent colour output and also in addition the **device-independent** elementary colour output is included.



SE270-3N

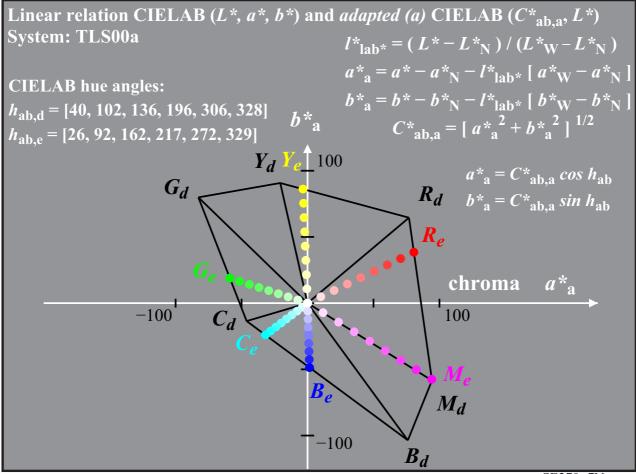
Fig. 8 - Device and elementary colours of standard offset according to ISO/IEC 15775

Fig. 8 shows the device colours $RYGCBM_d$ of standard offset according to ISO/IEC 15775 and the elementary colours $RYGB_e$ which are produced in standard offset for the four elementary hue angles $h_{ab,e} = 25$, 92, 162, and 271. In addition the mean hue angles $h_{ab,Ce} = 217 = 162+(271-162)/2$ and $h_{ab,Me} = 329 = 271+(397-271)/2$ are given for C_e and M_e

Fig. 8 shows some equation to calculate the CIELAB coordinates with the index a (= adapted). If the CIELAB coordinates of black $N(a_N^*, b_N^*)$ and white $W(a_W^*, b_W^*)$ are all zero (which is not true for standard offset) then the coordinates with the index *a* are identical to the coordinates without index. In any case the adapted coordinates (index a) have the values 0 for both the black *N* and white *W*. For the calculation of the hue angle this property is necessary.

If the CIELAB (*a*^{*}, *b*^{*}) coordinates of black *N* and *W* are known one can transfer to the adapted coordinates and backwards.

Many CIE data, for example *x*, *y*, *X*, *Y*, *Z*, *L*^{*}, C_{ab}^* , h_{ab} of the six standard chromatic colours RGB_d and CMY_d and black *N* and white *W* are given in Annex B on page 52 for the offset system ORS18 and the television systems TLS00 and TLS18. The system called TLS00 is identical to the standard display system sRGB. The system TLS18 has the lightness $L_N^*=18$ for black *N*. This lightness corresponds to the CIE tristimulus value *Y*=2,5.



SE270-7N

Fig. 9 - Device and elementary colours of the standard sRGB display according to IEC 61966-2-1

Fig. 9 shows the device colours $RYGCBM_d$ of the standard sRGB display according to IEC 61966-2-1. The elementary colours $RYGB_e$ have the four elementary hue angles $h_{ab,e} = 25$, 92, 162, and 271. In addition the colours C_e and M_e are shown for the hue angles $h_{ab,Ce} = 217 = 162+(271-162)/2$ and $h_{ab,Me} = 329 = 271+(397-271)/2$.

Fig. 9 shows some equations to calculate the CIELAB coordinates with the index a (= adapted), similar as Fig. 8. The standard sRGB device produces the colours B_d and M_d with a high chroma. This is the case in a dark room without reflection on the display. In offices with a standard luminance reflection of L_r =2,5% (CIE tristimulus value Y=2,5 compared to the white reference) the chroma $C^*_{ab,a}$ decreases by about 10% and is still much larger compared to the chroma $C^*_{ab,a}$ of standard offset ORS18a, compare Fig. 8 on page 12.

The different chroma of standard offset ORS18a and the standard display sRGB indicate that a colorimetric reproduction with the same $L^*C^*_{ab}h_{ab}$ values on the display and in print is not possible

A comparison of Fig. 8 on page 12 and Fig. 9 shows similar chroma $C_{ab,a}$ for the elementary blue B_e . However, the lightness L^* on the screen is larger. Both values $(L^*C^*_{ab,a})_e$ are needed for the comparison and the reproduction.

6.6 Colour double cone and basics of output linearization

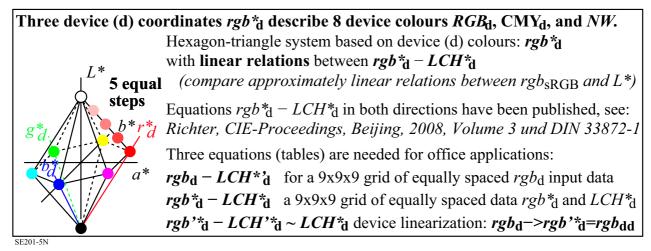
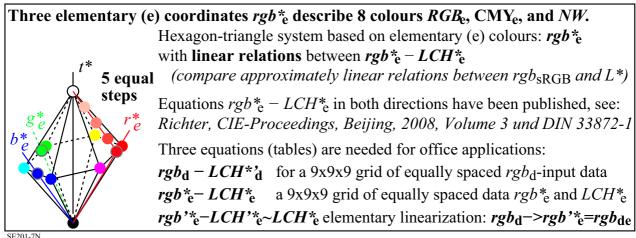


Fig. 10 - Six chromatic device colours RGB_d and CMY_d, and black N, and white W

Fig. 10 shows the device coordinates rgb_{d}^{*} which can describe six chromatic device colours RYG_{d} and CMY_{d} , and the achromatic colours black N and white W. They are all located on the border of a three dimensional colour cone with a hexagon basis. Usually display systems use additive mixture of a most chromatic primary, for example red R_d, with different amounts of the opponent colour C_d to produce for example the five step scale between red $R_{\rm d}$ and white W.

It is the goal to define both equally spaced rgb_{d}^{*} coordinates, in this case $rgb_{d} = (1,00\ 0,00\ 0,00)_{d}$ (1,00 0,25 0,25)_d, (1,00 0,50 0,50)_d, (1,00 0,75 0,75)_d, and (1,00 1,00 1,00)_d, and equally spaced relative CIELAB coordinates $tcu_{d}^{*} = (0,50 \ 1,00 \ \text{R00Y})_{d}$, $(0,625 \ 0,75 \ \text{R00Y})_{d}$, $(0,75 \ 0,50 \ \text{R00Y})_{d}$, $(0,875 \ 0,25 \ \text{R00Y})_{d}$, and $(1,00 \ \text{R00Y})_{d}$, $(0,100 \ \text{R0W})_{d}$, $(0,100 \ \text{R$ 0,00 R00Y)_d. The coordinates tcu^*_{d} are called device triangle lightness t^*_{d} , device relative chroma c^*_{d} , and device hue text u_{d}^{*} (=R00Y_d) according to DIN 33872-1. For the 5 step colour series between red R_{e} and white W there is by definition a linear relation between the coordinates rgb*_d and LCH*_d. Therefore for any rgb*_d value the LCH*_d values can be calculated in both directions, if the LCH*_d data for the colours of maximum chroma are given. In applications instead of 6 steps 48 steps of a chromatic circle are used.



SE201-7N

Fig. 11 - Six chromatic elementary colours RGB_e and CMY_{e} , and black N, and white W

Fig. 11 shows the elementary coordinates rgb*e which can describe six chromatic elementary colours RGBe and CMY_{e} , and the achromatic colours black N and white W. The equations are similar compared to Fig. 10. The coordinates star-dash (*') and dash-star ('*) are defined in ISO/IEC 15775 and will be applied in clause 7.4 on page 26. The real data LCH'*_e may have a colour difference $\Delta E^*_{ab} \sim 1$ compared to the intended data LCH*_e.

Table 3 - Coordinates rgb*e	and CIELAB (L*a*b*C*abhab)	e of a 16 step hue circle and mixture colours
-----------------------------	----------------------------	---

<i>rgb</i> [*] _e and Cl according to				• • •			<i>rgb</i> [*] _e and Cl according to				• • •		
16 step elemen	tary hu	e circle w	ith hues	$: h_{ab,a,e} =$	25.4, 92	.3, 162.2, 271.7	3 colours of th	e elemei	ntary huo	es <i>RYGB</i>	e: h _{ab,a,e} =	= 25.4, 9	2.3, 162.2, 271.7
Code	L* _{a,e}	a* _{a,e}	b* _{a,e}	C* _{ab,a,e}	h _{ab,e}	rgb*e	Code	L* _{a,e}	a* _{a,e}	b* _{a,e}	C* _{ab,a,e}	h _{ab,e}	rgb* _e
$R\theta\theta Y_{\rm e} = R_{\rm e}$	50.9	78.1	37.1	86.4	25.4	1.00 0.00 0.00	$R\theta\theta Y_{e} = R_{e}$	50.9	78.1	37.1	86.4	25.4	1.00 0.00 0.00
R25Y _e	52.2	71.9	65.2	97.1	42.1	1.00 0.25 0.00	θ , 5 $R_{\rm e}$ + θ , 5 $N_{\rm e}$	25.4	39.0	18.5	43.2	25.4	0.50 0.00 0.00
R50Y _e	63.1	42.7	70.7	82.6	58.8	1.00 0.50 0.00	$0.5R_{e} + 0.5W_{e}$		39.0	18.5	43.2	25.4	1.00 0.50 0.50
<i>R75Y</i> _e	72.7	19.7	76.7	79.2	75.5	1.00 0.75 0.00							
$Y \theta \theta G_{e} = Y_{e}$	83.6	-3.4	84.2	84.3	92.3	1.00 1.00 0.00	$Y \theta \theta G_{e} = Y_{e}$	83.6	-3.4	84.2	84.3	92.3	1.00 1.00 0.00
<i>Y25G</i> e	90.8	-31.8	88.5	94.0	109.7	0.75 1.00 0.00	$\theta, 5Y_{e} + \theta, 5N_{e}$	41.8	-1.7	42.1	42.1	92.3	0.50 0.50 0.00
Y50G _e	85.9	-63.0	82.7	104.0	127.2	0.50 1.00 0.00	$0,5Y_{e} + 0,5W_{e}$	89.5	-1.7	42.1	42.1	92.3	1.00 1.00 0.50
<i>Y75G</i> _e	84.1	-76.6	54.1	93.8	144.7	0.25 1.00 0.00							
$G\theta\theta B_{\rm e} = G_{\rm e}$	85.1	-64.2	20.5	67.4	162.2	0.00 1.00 0.00	$G\theta\theta B_{\rm e} = G_{\rm e}$	85.1	-64.2	20.5	67.4	162.2	0.00 1.00 0.00
G25B _e	87.1	-49.5	-8.4	50.2	189.6	0.00 1.00 0.50	θ ,5 $G_{\rm e}$ + θ ,5 $N_{\rm e}$	42.5	-32.1	10.2	33.7	162.2	0.00 0.50 0.00
G50B _e	79.1	-33.9	-25.6	42.5	217.0	0.00 1.00 1.00	$\theta, 5G_{e} + \theta, 5W_{e}$	90.2	-32.1	10.2	33.7	162.2	0.50 1.00 0.50
G75B _e	70.1	-18.8	-39.1	43.4	244.2	0.00 0.50 1.00							
$B00R_{\rm e} = B_{\rm e}$	59.3	1.7	-56.0	56.1	271.7	0.00 0.00 1.00	$B00R_{e} = B_{e}$	59.3	1.7	-56.0	56.1	271.7	0.00 0.00 1.00
B25R _e	38.3	52.5	-90.3	104.4	300.1	0.50 0.00 1.00	$0,5B_{e} + 0,5N_{e}$	29.6	0.8	-28.0	28.0	271.7	0.00 0.00 0.50
B50R _e	57.3	94.2	-57.4	110.4	328.6	1.00 0.00 1.00	$0,5B_{e} + 0,5W_{e}$	77.4	0.8	-28.0	28.0	271.7	0.50 0.50 1.00
$B75R_{\rm e}$	52.5	82.3	-4.2	82.4	357.0	1.00 0.00 0.50							
5 step equidist	ant grey	scale: L	* _e = 0.0,	23.8, 47.7	, 71.5, 95	5.4	5 step equidist	ant grey	scale: L	* _e = 0.0,	23.8, 47.7	, 71.5, 9	5.4
Code	L* _{a,e}	a* _{a,e}	b* _{a,e}	C* _{ab,a,e}	h _{ab,e}	rgb* _e	Code	L* _{a,e}	a*a,e	b* _{a,e}	C* _{ab,a,e}	h _{ab.e}	rgb* _e
$N000W_{e} = N_{e}$	0.0	0.0	0.0	0.0	0.0	0.00 0.00 0.00	$N000W_{e} = N_{e}$		0.0	0.0	0.0	0.0	0.00 0.00 0.00
N025We	23.8	0.0	0.0	0.0	325.3	0.25 0.25 0.25	N025We	23.8	0.0	0.0	0.0	325.3	0.25 0.25 0.25
N050We	47.7	0.0	0.0	0.0	325.1	0.50 0.50 0.50	N050W	47.7	0.0	0.0	0.0	325.1	0.50 0.50 0.50
N075W	71.4	0.0	0.0	0.0	325.1	0.75 0.75 0.75	N075W	71.4	0.0	0.0	0.0	325.1	0.75 0.75 0.75
$N100W_{\rm e} = W_{\rm e}$	95.4	0.0	0.0	0.0	0.0	1.00 1.00 1.00	$N100W_{\rm e} = W_{\rm e}$		0.0	0.0	0.0	0.0	1.00 1.00 1.00
SE300-3N		*100 0	danted	=not ad	anted		SE300-4N		*1.0	dantad	-mot od		

SE300-3N, LAB*la0, adapted=not adapted

SE300-4N, LAB*la0, adapted=not adapted

Table 3 shows the coordinates rgb_{e}^{*} and the corresponding CIELAB data $(L^*a^*b^*C^*{}_{ab}h_{ab})_{e}$ for the standard sRGB colour space. On the left side the data are given for a 16 step elementary hue circle and on the right side for mixture colours between the most chromatic colours and black *N* and white *W*. On both sides a 5 step grey scale is added. For the normalization of the data for white *W* the standard L^*_{W} data of the standard offset paper according to ISO/IEC 15775 are used (Y=88,6, L*=95,4).

It is very essential to understand the goal of this report which uses the term output linearization. For output linearization a regular double cone forms the colour space with a circular instead of the hexagon basis, and with the coordinates tcu^* to be defined. The next two figures will include some example data and the definitions of this coordinates which can be calculated either from the data rgb^*_e or $(L^*C^*_{ab}h_{ab})_e$.

Table 3 shows the data $L_{a,e}^* = L_e^*$ for the 16 step hue circle. The largest value $L_e^*=90.8$ is reached for Y25G_e and the lowest value $L_e^*=38.3$ for B25R_e. The coordinate triangle lightness t_e^* for the (most chromatic) colour circle in Table 3 is defined as

 $t_{e}^{*} = 0.5 (L_{e}^{*} / L_{e,M}^{*})$ (=0.5 for $L_{e}^{*} = L_{e,M}^{*}$)

For the achromatic colour series the triangle lightness t_e^* is equal to the relative lightness

$$t_{e}^{*} = (L^{*} - L_{N}^{*}) / (L_{W}^{*} - L_{N}^{*})$$

Relative chroma c* is defined as relative CIELAB chroma C*ab compared to the chroma C*ab.M

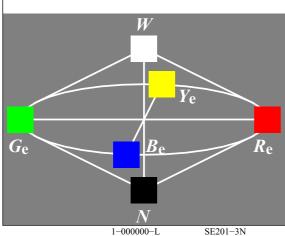
$$c_{e}^{*} = C_{ab,e}^{*} / C_{ab,e,M}^{*}$$
 (=1 for $C_{ab,e}^{*} = C_{ab,e,M}^{*}$)

Therefore the most chromatic colour circle of Table 3 (left) has the coordinates $t_e^*=0.5$ and $c_e^*=1$ for any hue.

What is Output Linearization? (For the elemetary hues, see CIE R1-47:2009.) The colour space of a double cone includes 6 colours. The six colours can be the device-dependend device colours (index d): $(R, Y, G, B, N, W)_d$ or the device-independend elementary colours (index e): $(R, Y, G, B, N, W)_e$. Elementary red appears neither yellowish nor bluish. The hue angle is $h_{ab,e} = 26$.

For example for red R_e there are colorimetric data $(L^*, C^*_{ab}, h_{ab})_e$ and corresponding data rgb_e in the sRGB colour space according to IEC 61966-2-1. Some corresponding data are shown in the figure for the colours RYW_d and RYW_e .

 $rgb_{W} = (1 \ 1 \ 1)_{W}$ (*L**, *C**_{ab}, *h*_{ab})_W = (95, 0, -)_W



 $rgb_{d,Yd} = (1\ 1\ 0)_{d,Yd}$ $(L^*, C^*_{ab}, h_{ab})_{Yd} = (93, 93, 103)_{Yd}$ $rgb_{e,Ye} = (1\ 1\ 0)_{e,Ye} = (1\ 0,86\ 0)_{de,Ye}$ $(L^*, C^*_{ab}, h_{ab})_{Ye} = (84, 85, 92)_{Ye}$ **Output Linearization** (proposed CIE R8–09) produces for the mean data rgb of R_e and Wthe mean data (L^*, C^*_{ab}, h_{ab}) . Similar for $rgb_e = (1\ 0,5\ 0)_e$ the mean hue angle $h_{ab,e} = 59 = 26 + (92 - 26)/2$ is produced. $rgb_{d,Rd} = (1\ 0\ 0)_{d,Rd}$ $(L^*, C^*_{ab}, h_{ab})_{Rd} = (50, 100, 40)_{Rd}$ $rgb_{e,Re} = (1\ 0\ 0)_{e,Re} = (1\ 0\ 0,26)_{de,Re}$ $(L^*, C^*_{ab}, h_{ab})_{Re} = (50, 87, 26)_{Re}$



Fig. 12 tries to answer the question: What is output linearization? With Fig. 10 on page 14 it was possible to understand the transfer from the coordinates $L^*C^*_{ab}h_{ab}$ to the double cone coordinates tce^* with a circular basis. For a mean grey and the most chromatic colours the value of the triangle lightness is t^*_e =0,5. For the circle the relative chroma is c^*_e =1. Both the device colours and the elementary colours are located on this circle. However, they have different CIELAB hue angles, for example $h_{ab,Yd}$ = 103 and $h_{ab,Ye}$ = 92.

Fig. 12 shows that there is a linear calculation of the intended CIELAB hue angles. For example the coordinates $rgb_e = (1\ 0.5\ 0)_e$ which belong to the hue (R50Y)_e are in the middle between the data for red and yellow. It is intended that the data $rgb_e = (1\ 0.5\ 0)_e$ produce the CIELAB hue angle in the middle between the hue angles of red R_e and yellow Y_e.

The next figure will give more example data how to transfer between the different coordinates. The user friendly coordinates are based on the request of ISO TC 159 "Visual Display Requirements" (compare Fig. 3 on page 8).

At the same time a further step seem to be reached towards a human visual RGB_{e}^{*} colour space. This development of the CIE Division 1 was requested by ISO/IEC JTC1/SC28 (Fig. 6 on page 10).

6.7 Colour in daily life and definition of user friendly relative colour coordinates

Design, architecture, art, industrial products	Colour Information Technology
Measured for CIE standard illuminant D65	Measured for CIE illuminants D65 and D50
colour order system; name and coordinates:	Device system name and coordinates:
<i>RAL Design System (CIELAB)</i>	Printer system (illuminants D50 or D65):
<i>L*C*</i> _{ab} <i>h</i> _{ab} , lightness, chroma, hue angle	<i>cmy</i> _d , content of "cyan, magenta, yellow"
<i>Munsell Colour System</i>	Display system (standard illuminant D65):
<i>VCH</i> , lightness (Value), Chroma, Hue text	rgb _d /sRGB _d , content of "red, green, blue"
<i>Natural Colour System (NCS)</i> <i>ncu</i> [*] _e : relative blackness, relative chroma relative elementary hue text	No user friendly colour coordinates Nearly no connection to colour order systems

Aim: define user friendly connection

New: Interpretation of the *rgb* colour data in the range 0 to 1 as elementary colour data rgb_e^*

Linear relations between relative and absolute coordinates $lab_{d}^{*} - LAB_{d}^{*}$ and $lab_{e}^{*} - LAB_{e}^{*}$ $rgb_{d}^{*} - (L^{*}a^{*}b^{*}C_{ab}^{*}h_{ab})_{d}$ and $rgb_{e}^{*} - (L^{*}a^{*}b^{*}C_{ab}^{*}h_{ab})_{e}$ (CIELAB) $rgb_{d}^{*} - cmy_{d}, rgb_{d}^{*} - cmy_{d}^{*}$ and $rgb_{e}^{*} - cmy_{e}, rgb_{e}^{*} - cmy_{e}^{*}$ ("1-minus"-relation) $rgb_{d}^{*} - nce_{d}^{*}, rgb_{d}^{*} - ncu_{d}^{*}$ and $rgb_{e}^{*} - nce_{e}^{*}, rgb_{e}^{*} - ncu_{e}^{*}$ relative coordinates lab_{e}^{*} : elementary redness r_{e}^{*} , greenness g_{e}^{*} , blueness b_{e}^{*} , blackness n_{e}^{*} chroma c_{d}^{*} , elementary hue e_{e}^{*} , elementary hue text u_{e}^{*}

SE251-3

Fig. 13 - Application of colour in daily life or in colour information technology (IT)

Fig. 13 shows colour coordinates used in daily life in the field of colour order systems, for example the CIELAB coordinates $L^*C^*_{ab}h_{ab}$. There are coordinates used in information technology, for example rgb_d of the sRGB colour space. There seems to be nearly no user friendly colour coordinates in information technology, for example those requested by ISO TC159 Ergonomics - Visual display requirements. The coordinates rgb_e of Fig. 13 and the coordinates cmy^*_e used in offset printing seem to fill this gap. Both are connected by the so called 1-Minus-Relation (1MR) which is based on the three equations

 $c_{e}^{*} = 1 - r_{e}^{*}$ $m_{e}^{*} = 1 - g_{e}^{*}$ $y_{e}^{*} = 1 - b_{e}^{*}$

It is one main goal of this paper to define more user friendly coordinates for image technology and a user friendly connection to CIELAB and other colorimetric systems based on CIE colour measurement and colour appearance.

Usually the colour considered here are presented either on a white display surround or on a white paper. This presentation mode is called surface colour mode in CIE colorimetry. The standard illuminance on the white paper is 500 lux in offices. For the white standard offset paper with the standard reflection of 88,6% this produces the luminance L=142 cd/m². The same luminance is possible on many modern sRGB or other devices. There are many real device arrangements where it is hard to answer the question if the output of a test chart is produced by the reflection of light on paper or by the emission of light on a screen.

So we may have surface colour mode either by the reflection of light or by the emission of light. Both are in many cases physically (by measurement) and visually equivalent. In addition there are screen technologies which produce the colours by both the emitting of light in a dark environment, and the reflection of light in sunshine

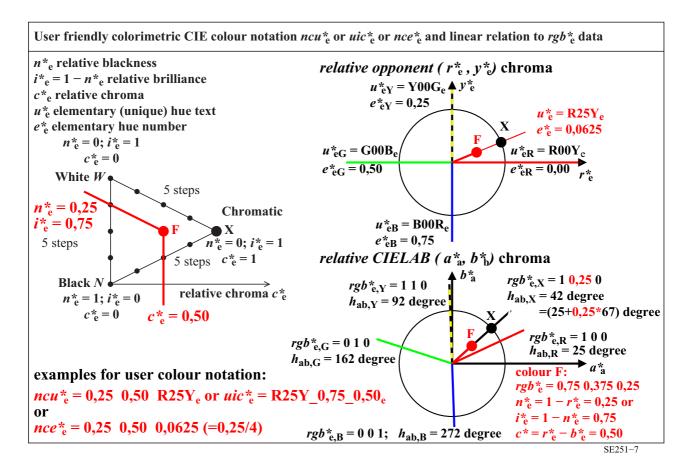


Fig. 14 - User friendly colorimetric CIE colour notations *ncu**_e, *uic**_e or *nce**_e

Fig. 14 shows user friendly colorimetric CIE colour notations ncu^*_{e} , uic^*_{e} , and nce^*_{e} . Some examples show the transfer between the many possible data sets rgb^*_{e} , ncu^*_{e} , uic^*_{e} , and nce^*_{e} . The CIELAB hue angles for the four elementary colours $RYGB_{e}$ are given. Instead of the CIELAB coordinates (a^*_{a}, b^*_{a}) and the CIELAB hue angle h_{ab} the relative opponent coordinates (r^*_{e}, y^*_{e}) and the relative elementary hue e^*_{e} in the range between 0 to 1 may be used.

On the front cover of the book "Colour and Colour Vision", see the next figure the coordinates rgb_{e}^{*} and HIC_{e}^{*} are given above and below the samples

It is valid

I*=100 i* and

 $C^* = 100 \ c^*$

Then in Fig. 14 the colour notation

*uic**_e = R25Y_0,75_0,50_e

changes to (without any comma)

HIC^{*}_e = R25Y_075_050_e

Annex C on page 55 shows these and additional coordinates and their relations.

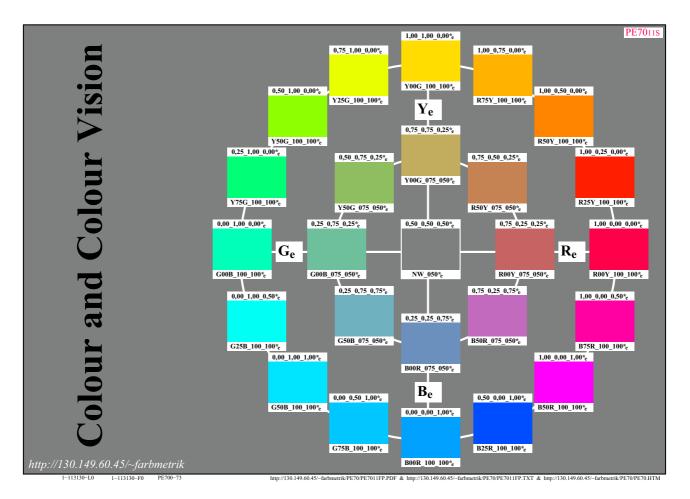


Fig. 15 - Elementary colour circle with 16 samples and colorimetric coordinates rgb*e and HIC*e

Fig. 15 shows the 16 step elementary colour circle together with the CIE colorimetric coordinates rgb_{e}^{*} on the top and HIC_{e}^{*} on the bottom. This colour circle is on the top cover of a book and available in offset print. The inner circle has half the CIELAB chroma C_{ab}^{*} of the outer circle. The grey is in CIELAB lightness L^{*} in the middle between the lightness L_{N}^{*} of black *N* and the lightness L_{W}^{*} of white *W*.

The four elementary colours shall have the CIELAB hue angles $h_{ab,e}$ = 26, 92, 162, and 271. The visual test shall clearly show that for example R25Y_e appears yellowish and B75R_e appears bluish.

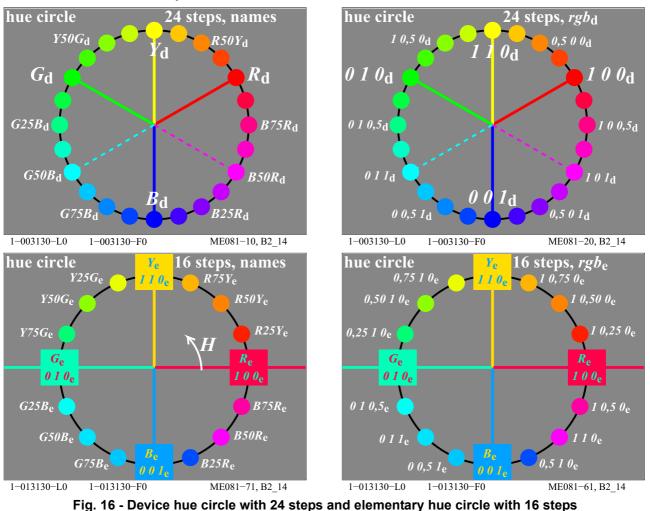
Output linearization has been used to produce this colour circle on displays, as printer output and offset output.

For the linearized elementary output of the 25 samples and for the standard sRGB display the calculations show an average colour difference $\Delta E^*_{ab,e} = 0,4$ for the outer circle and of $\Delta E^*_{abe} = 0,7$ for the inner circle. The largest difference appears for the sample Y50G_050_050_e.

The calculated data are available as tables on the page 52 (page 19 of second series) of the file output http://130.149.60.45/~farbmetrik/RE69/RE69L0FP.PDF

Measurement of the linearized elementary output for the 25 samples, and for the offset output on glossy paper shows an average colour difference of ΔE^*_{ab} = 3,0 between the intended and the measured output, compare page 52 (page 19 of the second series) of the file output http://130.149.60.45/~farbmetrik/SE03/SE03L0FP.PDF

Both file outputs show many additional data and figures, for example the device display colours on page 8 and the data rgb_{de} and $(L^*a^*b^*C^*_{ab,a})_e$ for the 360 hue angles $h_{ab,e}$ between zero and 360 in steps of $\Delta h_{ab,e}$ =1.



6.8 Device and Elementary colour circles

Fig. 16 shows two device hue circles with 24 steps on the top. The hue text H_d^* is given on the left side, and the

 rgb_{d} data are given on the right side.

Fig. 16 shows two elementary hue circles with 16 steps on the bottom. The hue text H_e^* is given on the left side, and the *rgb*_e data are given on the right side.

A comparison of the device and elementary hue circle (top and bottom) shows an increase of the hue angle range from 60 to 90 for the sectors R_e to Y_e and Y_e to G_e . This is the lighter side of the colour circle.

At the same time there is a decrease of the hue angle range form 120 to 90 for the ranges between G_d via C_d to B_d , and B_d via M_d to R_d . This is the darker side of the colour circle.

This change is used in the NCS colour system and is appropriate for applications by at least two reasons

- The CIELAB chroma of surface colours is for the darker side between G_e via B_e to R_e roughly half compared to the lighter side. Therefore the ratio colour difference/hue angle difference $\Delta E^*_{ab}/\Delta h_{ab}$ is roughly half for the darker side. Therefore it is appropriate to reduce the hue angle range from 120 to 90 for the darker side and to increase the hue angle range form 60 to 90 for the lighter side.

- in many applications, for example house and wall paintings, clothes and advertising, the lighter colour side is much more important compared to the darker colour side. Therefore the elementary (e) hue scaling by rgb_{e}^{*} is more appropriate compared to the present device (d) colour scaling by rgb_{d}^{*} .

7 Equivalent relative coordinates rgb and cmyk for digital and analog colours

7.1 Test chart output with 1080 colours on a displays with different software

By CIE colorimetry and according to the *PostScript Reference Manual* there are many equivalent relative coordinates *rgb* and *cmyk* to describe colours in digital files and the (analog or visual) surface or display colours

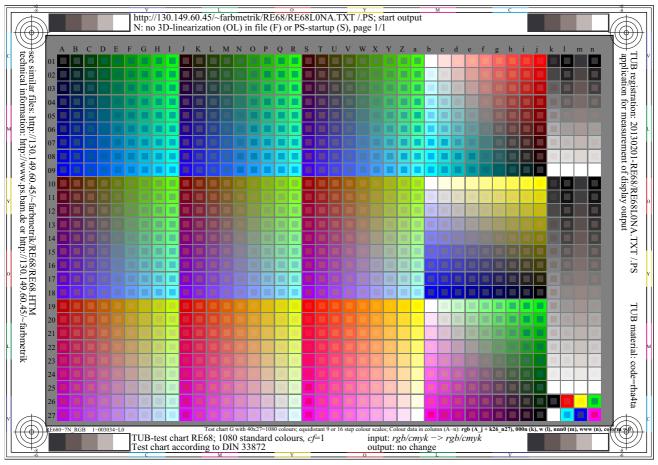


Fig. 17 - Standard colour test chart with 1080 colours defined by rgb and equivalent data

Fig. 17 shows a standard colour test chart with 1080 colours. The left 729 (=9x9x9) colours (columns A to a and rows 01 to 27) show a standard grid (Grid G) which is often used for output colour measurement.

The following 243 (=3x9x9) colours (columns b to j, and rows 01 to 27) show opponent colour planes $R_d - C_d$, $Y_d - B_d$, and $G_d - M_d$ with three times the achromatic series in the diagonal.

At least there are 9 step grey scales (columns k to n, rows 01 to 09) and 16 step grey scales (columns k to n, rows 10 to 25) and the six most chromatic device colours and black and white (columns k to n, rows 26 and 27).

There are two equivalent definitions for chromatic colours by two PostScript operators:

- r g b setrgbcolor
- c m y 0 setcmykcolor

The output looks usually different and the difference is device-dependent.

The values of *rgb* and *cmyk* are in the range 0 to 1, otherwise a negative value is set to zero, and for values larger 1 the value is set to one. There is the so called 1-Minus-Relation (1MR) between *rgb* and *cymk* which is given by

c = 1 - r m = 1 - g y = 1 - b k = 0.

If the lowest value w = min (r g b) which is called the white value w of the three is larger than zero then the

following relation is equivalent: c = 1 - r - wm = 1 - g - wk = w. y = 1 - b - w

There are four equivalent definitions for grey (achromatic) colours with r=g=b=w by the PS operators w w w setrabcolor

1-w 1-w 1-w 0 setcmykcolor 0 0 0 w setcmykcolor w setgray

These definitions are used in the four rows k to n. The output looks usually different and is device-dependent.

http://130.149.60.45/~farbmetrik/RE68/RE68L0NA.TXT /.PS; start output N: no 3D-linearization (OL) in file (F) or PS-startup (S), page 1/1 C D E GHIJKLMNOPQRSTUVWXYZab A в eee similar files: http://130.149.60.45/-farbmetrik/RE68/RE68.HTM technical information: http://www.ps.bam.de or http://130.149.60.45/~farbmetrik TUB registration: 20130201-RE68/RE68L0NA.TXT/.PS - application for measurement of display output 06 07 12 13 14 15 16 17 18 19 20 TUB material: code=rha4ta 22 23 24 25 TUB-test chart RE68; 1080 standard colours, cf=1 input: rgb/cmyk -> rgb/cmyk output: no change

7.2 Screen shot of the display output with the software Adobe FrameMaker

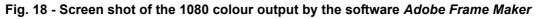


Fig. 18 shows a screen shot of the output of the 1080 standard colours defined by the four PS operators:

- r g b setrgbcolor
- c m y 0 setcmykcolor (always in addition as the inner square with half of the diameter for any colour)
- -000 n setcmykcolor
- w setgray

with corresponding values defined by the 1-Minus-Relation. The output is equal with Adobe Frame Maker.

Therefore the display output of Fig. 18 (a screen shot produces a *tiff*-file) is equal. The printer output of Fig. 18 (based on the PDF-file created by the software Adobe Frame Maker) shows up to four different colour outputs for the four equivalent PS operators.

The software Adobe Frame Maker produces for the four PS operators

Test chart according to DIN 33872

- equal output on the screen as intended for the four equivalent PS operators by CIE colorimetry,
- and a PDF file for later print if requested.

The software *Adobe Reader* produces with this PDF-file (which includes the four PS-operators) - **different device-dependent output on the screen and in print** for the four equivalent PS operators.

It is obvious that a device-independent CIE standard is needed. At present many of the devices produce for values around $cmy_d = (0,45\ 0,32\ 0,32)$ a mean grey and **not** for $cmy_e = cmy_d = (0,5\ 0,5\ 0,5)$. There is a historic basis for the strange cmy_d values. A special offset process has produces for the values $cmy_d = (0,45\ 0,32\ 0,32)$ a mean grey. However, by many reasons grey shall now be produced by the black colorant *N* (*K*) only, if the device has a black colorant (and for example the three colours *CMY*).

Note: The software *Preview* of the *Mac* operating system OSX up to Version 10.2 includes the 1-Minus-Relation and has produces equal colour output for equivalent colour definitions. Since Version 10.3 the output is different.

Note: In addition the software *Preview* of the *Mac* operating system OSX changes any PS file to a PDF file by a double click on the PS file. Therefore output linearization is possible with the software of the *Mac* operating system OSX without additional software, for example the software *Adobe Distiller* on a *Mac* or on a Windows operating system.

5 steps of grey series black – white (N _d – W _d)	Colour space, colour space coordinates and PostScript operator calculations according to ISO/IEC 15775:1999-12											
Linear mixture between				re	lative	CIE	LAB					
black and white	lab*w*d	lab*l)00n*	t _d =000	0n*d	lab*e	cmy0 [°]	*d=cm	<i>y0*</i> d	lab*r	gb*d=	<i>rgb*</i> d
in CIELAB colour space	setgray	000n	* _d set	cmyk	color	cmyl)* _d set	tcmyk	color	rgb*d	setrg	bcolor
$1,00N_{d}+0,00W_{d}$ (Black N_{d}) $0,75N_{d}+0,25W_{d}$ $0,50N_{d}+0,50W_{d}$	0,00 0,25 0,50	0,00	0,00	0,00	0,75	0,75	0,75	0,75	0,00	0,00 0,25 0,50	0,25	0,25
$0,30N_{d}+0,30W_{d}$ $0,25N_{d}+0,75W_{d}$ $0,00N_{d}+1,00W_{d}$ (white W_{d})	0,30 0,75 1,00	0,00	0,00	0,00	0,25	0,25	0,25	0,25	0,00	0,30 0,75 1,00	0,75	0,75

5 steps of grey series black – white (N _d – W _d)	Colour space, colour space coordinates and PostScript operator calculations according to ISO/IEC 15775:1999-12								
Linear mixture between black and white in CIELAB colour space	$LAB*LAB*_{d} = LAB*_{d}$			adapteo LAB*L LAB*a,	relative CIELAB lab*ncu* _d = ncu* _d ncu* _d setcolor				
$ \begin{array}{c} 1,00N_{\rm d} +0,00W_{\rm d} \ ({\rm Black} \ N_{\rm d}) \\ 0,75N_{\rm d} +0,25W_{\rm d} \\ 0,50N_{\rm d} +0,50W_{\rm d} \\ 0,25N_{\rm d} +0,75W_{\rm d} \\ 0,00N_{\rm d} +1,00W_{\rm d} \ ({\rm white} \ W_{\rm d}) \end{array} $	18,01 37,35 56,70 76,05 95,41	0,50 0,10 -0,10 -0,50 -0,98	2,10 -3,40	18,01 37,35 56,70 76,05 95,41	$0,00 \\ 0,00 \\ 0,00 \\ 0,00 \\ 0,00 \\ 0,00$	$\begin{array}{c} 0,00\\ 0,00\\ 0,00\\ 0,00\\ 0,00\\ 0,00 \end{array}$	0,75 0,50 0,25	0,00 0,00 0,00	R00Y _d R00Y _d R00Y _d R00Y _d R00Y _d

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5 steps of colour series cyan blue – white (C _d – W _d)	Colour space, colour space coordinates and PostScript operator calculations according to ISO/IEC 15775:1999-12								
Linear mixture between cyan blue and white in CIELAB colour space	Standard CIELAB LAB*LAB*d = LAB*d LAB*d setcolor	relative CIELAB lab*cmy0*d = cmy0*d cmy0*d setcmykcolor	relative CIELAB lab*rgb*d = rgb*d rgb*d setrgbcolor						
$ \begin{array}{c} 1,00C_{\rm d}+0,00W_{\rm d} \mbox{ (cyan blue } C_{\rm d}) \\ 0,75C_{\rm d}+0,25W_{\rm d} \\ 0,50C_{\rm d}+0,50W_{\rm d} \\ 0,25C_{\rm d}+0,75W_{\rm d} \\ 0,00C_{\rm d}+1,00W_{\rm d} \mbox{ (white } W_{\rm d}) \end{array} $	58,62 -30,62 -42,74 67,82 -23,21 -30,86 77,02 -15,80 -18,98 86,21 -8,39 -7,11 95,41 -0,98 4,76	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$						

Table 5 - Equivalent PS operators for cyan blue colours C by CIE colorimetry and PostScript

SE250-5

Table 4 and Table 5 show equivalent PS operators for grey colour series between black *N* and white *W*, and for a 5 step colour series between cyan blue C_d and white *W*. The output with the four standard PS operators shall be the same by CIE colorimetry and the *PostScript* programming language, see *PostScript* reference manual.

7.3 PostScript code which includes the 1-Minus-Relation

Table 6 - PostScript programming code which includes the 1-Minus-Relation

```
Frame File PostScript Code for 1-Minus-Relation (1MR) to setrgbcolor
and line 05 to 07 for change of setgray to setrgbcolor
and line 09 to 13 for change of setcmykcolor to setrgbcolor
01 %!PS-Adobe-3.0 EPSF-3.0, 1MR for change to setrgbcolor
02 /1MR-0000 {%BEG procedure 1MR-0000
03 %1MR-Transform of setgray and setcmykcolor to FFM setrgbcolor
04
05 /setgray {%BEG procedure setgray to setrgbcolor
06
             dup dup FFM setrgbcolor
07
            } def %END procedure setgray to setrgbcolor
08
09 /setcmykcolor {%BEG procedure setcmykcolor to setrgbcolor
10 /FFM k exch def /FFM y exch def /FFM m exch def /FFM c exch def
11 FFM k 0 eq {1 FFM c sub 1 FFM m sub 1 FFM y sub FFM setrgbcolor}
12
              {1 FFM k sub dup dup FFM setrgbcolor} ifelse
13
                  } def %END procedure setcmykcolor to setrgbcolor
14
15 } def %END procedure 1MR-0000
16 %%Trailer %END 1-Minus-Relation (1MR) to setrgbcolor
Remarks:
The FF PS code includes: /FFM setrgbcolor {setrgbcolor} bind def
Then setgray and setcmykcolor is changed to standard setrgbcolor
SE341-3N
```

Table 6 includes some *PostScript* program code which transfers the three PS operators and their values - *w* setgray

- c m y 0 setcyykcolor

- 0 0 0 k setcmykcolor

towards the usually used PS operator r g b setrgbcolor with the values r g b according to the 1-Minus-Relation.

A user with some technical knowledge and for example the software *Adobe Distiller* can apply the 1-Minus-Relation. A user can download the file text 1MR: http://130.149.60.45/~farbmetrik/SE34/SE341-3N.TXT.

The user can copy the PS program text to the "Startup" directory or the "In" directory of the software *Adobe Distiller*. After a new start of the software *Adobe Distiller* the "*Startup code 1MR*" will change the three PS operators and their values in the intended direction and the output looks equal for equivalent colour definitions.

This method is used within many black and white PS printers which change the three PS operators to the *rgb* PS operator and produce an equal output for the equivalent colour definitions similar as *Adobe Frame Maker*.

However, many colour PS printers produce different colours in the output similar as *Adobe Reader* and often different depending on the version.

Alternative methods are the copy of the file text 1MR at the beginning of a PS file. Then for example the software Mac Preview uses the file text 1MR by a double click of the file to produce a PDF file with the intended change.

The most important application here is the copy of PS code together with the 1080 measurement data of a device at the beginning of a file. The use of the measurement data in the appropriate PS code changes all colour data in the intended direction.

For example this procedure produces a device linearization for the device or the elementary colour output.

7.4 PostScript Frame File code with output linearization method (FF_LM) Table 7 - Frame File Postscript code (FF_PS) with three loops

```
Frame File PostScript Code (FF PS) with three loops (important parts)
and line 05 (%line 139) to include different transfer PS codes
and line 20 (%line 239) to include the PS code of an ISO or DIN test file
01 %!PS-Adobe-3.0 EPSF-3.0 SE34LMFF.PS 20110801
02 %%BoundingBox: 0 0 842 595
03
04 %line169 %BEG INCLUDE TRANSFER PS CODES
05
06 %END INCLUDE TRANSFERS PS CODES
07 %%EndProlog
08 gsave
09
10 colorm10f 1 colorm20f {/colormf exch def %colorm10f,colorm20f
11 gsave
12
13 xcolor10f 1 xcolor20f {/xcolorf exch def %xcolor10f,xcolor20f
14 gsave
15
16 xchart10f 1 xchart20f {/xchartf exch def %xchart10f,xchart20f
17 gsave
18
19 %line 239 %BEG INCLUDE TEST FILE PS CODE
20
21 %END INCLUDE TEST FILE PS CODE
22
23 68 MM 1.5 MM moveto
24 (http://130.149.60.45/~farbmetrik/SE34/SE34LMFF.PDF) showde
25
26 showpage
27 grestore
28
29 } for %end for xchartf=xchart10f,xchart20f
30 grestore
31 } for %end for xcolorf=xcolor10f,xcolor20f
32 grestore
34 } for %end for colormf=colorm10f,colorm20f
35 %%Trailer
Remarks:
The outer loop 10 to 34 is without and with a Linearization Method
colormf=0 or 1 without and with Frame File Linearization Method (FF LM)
The middle loop 13 to 31 is for the amount of Room Reflections
xcolorf=0 to 7 for 8 display luminance reflections
The inner loop 16 to 29 is for the amount of ISO test pages
xchartf=0 to 11 for 1 to 12 ISO and DIN test file pages
Inclusion of TRANSFER PS CODE, for example 1MR, DEH, at line 05
Inclusion of TEST FILE PS CODE, for example ME16 of ISO 9241–306
```

SE340-7N

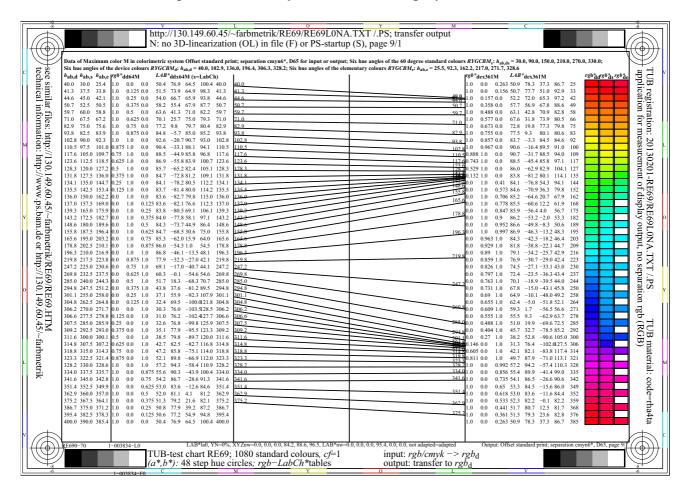
Table 7 shows an example PS code with three loops. A similar code is used to produce for example the output of many pages, see the file PS text (9 300 lines!) http://130.149.60.45/~farbmetrik/RE69/RE69L0FP.TXT

If one changes the extension from ".TXT" to ".PS" then for example the software *Mac Preview* produces a PDF file with 64 pages within a minute. This file includes according to line 5 of Fig. 23 the 1-Minus-Relation and calculates 1080 measurement data from the *rgb* data according to IEC 61966-2-1. This produces a table with a cloud of 729 *rgb*_d and corresponding $(L^*a^*b^*C^*_{ab}h_{ab})_d$ data. The CIELAB data fill a double cone with the $L^*C^*_{ab}$ data of a 48 step colour circle as basis.

On the pages 20 to 32 (first series) for the 1080 colours of the standard display the above file shows the tables $rgb_{d}^{*} - LCH_{d}^{*}$ (intended relation) and the tables $rgb_{d}^{*} - LCH_{d}^{*}$ (relation with dash-star coordinates for output linearization). The following two coordinates are identical: $rgb_{d}^{*} = rgb_{dd}$ (device to device output). The colour difference $\Delta E_{ab,d}^{*}$ between intended and real output is the difference between LCH_{d}^{*} and LCH_{d}^{*} .

On the pages 42 to 64 (second series) for the 1080 colours of the standard display the above file shows the tables rgb_{e}^{*} - LCH_{e}^{*} (intended relation) and the tables rgb_{e}^{*} - LCH_{e}^{*} (relation with dash-star coordinates for output linearization). The following two coordinates are identical: rgb_{e}^{*} = rgb_{de} (device to elementary output). The colour difference $\Delta E_{ab.e}^{*}$ between intended and real output is the difference between LCH_{e}^{*} and LCH_{e}^{*} .

Both tables are listed in Fig. 10 on page 14 (device output) and Fig. 11 on page 14 (elementary output).



7.5 Hue and colour output and accuracy for the sRGB display colours

Fig. 19 - rgb and CIELAB data of a 48 step hue circle for the device and elementary sRGB colours

Fig. 19 shows *rgb* and CIEAB data of a 48 step hue circle for the device and elementary colours. For the sRGB display near $h_{ab,e}$ =306 a large range of *rgb*_d data ($h_{ab,d}$ =300 to $h_{ab,d}$ =330) produce only a small change of the visual *rgb*_e data ($h_{ab,e}$ =300 to $h_{ab,e}$ =310).

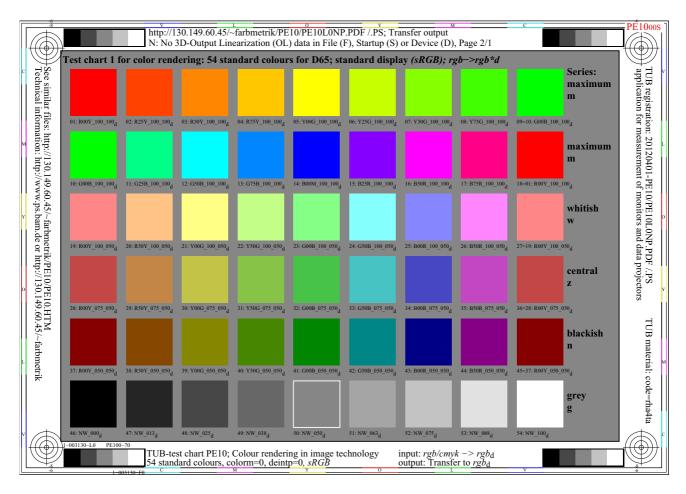


Fig. 20 - *HIC**_d data of a test chart 1 for colour rendering with a 16 step device hue circle

Fig. 20 shows the HIC_d^* data of a test chart 1 for colour rendering with a 16 step device hue circle. In addition there are three 8 step colour circles: whitish, greyish, and blackish. Finally ther is a 9 step grey scale.

The first and last colour of the 16 and 8 step colour circles are the same. This reduces difficulties for evaluations of the colour differences between the first and last step.

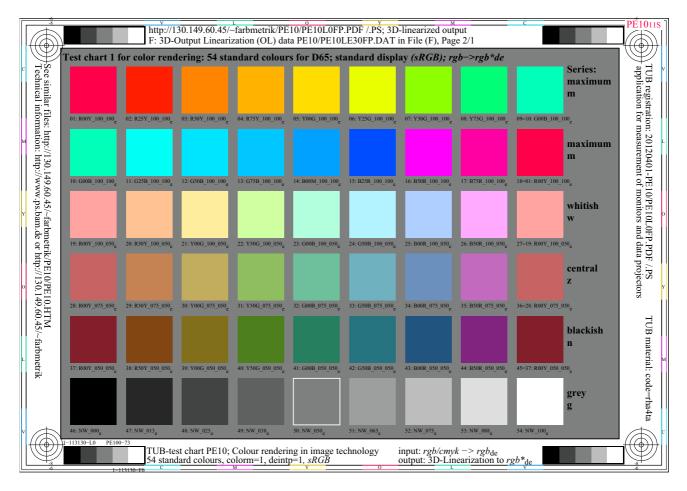


Fig. 21 - HIC_{e}^{*} data of a test chart 1 for colour rendering with a 16 step elementary hue circle Fig. 21 shows the HIC_{e}^{*} data of a test chart 1 for colour rendering with a 16 step elementary hue circle.

Table 8 - CIELAB colour differences ∆E* _{al}	b of start and linearized	output of the standard sRGB display
---	---------------------------	-------------------------------------

Calculation of disp files and series	Display output transfer and linearization of sRGB display according to IEC 61966–2–1							
files, colour amou	test colours	colour difference ΔE^*_{ab} (real–intended						
file and output colours pag		page, serie	content	hue trans	fer	3D-linearization		
code (d, e, dd, de)				d (de=0)	e (de=1)	dd (de=0)	de (de=1)	
RE69L0NP.PDF	57	18, 1 and 2	hue circle	0,9	26,3	0,1	0,4	
(output of d, e)	53	19, 1 and 2	test chart 1	6,5	21,3	0,8	0,8	
and	81	28, 1 and 2	plane $R-C$	7,3	11,2	0,8	0,7	
RE69L0FP.PDF	81	29, 1 and 2	plane <i>Y</i> – <i>B</i>	8,7	27,1	0,7	0,6	
(output of dd, de)	81	30, 1 and 2	plane <i>G</i> - <i>M</i>	11,4	22,0	0,6	0,6	

SE360-1

Table 8 shows the CIELAB colour differences between real and intended on a sRGB display for no room light reflection on the display (L_r =0). For the 48 steps of a hue circle and the 9 grey steps (57 colours) the CIELAB colour difference is $\Delta E^*_{ab,d}$ = 0,9 for the start output of the sRGB device colours and $\Delta E^*_{ab,d}$ = 26,3 for the start output of the sRGB elementary colours. This difference is reduced by output linearization to $\Delta E^*_{ab,dd}$ = 0,1 and $\Delta E^*_{ab,de}$ = 0,4. The remaining difference is therefore below threshold (ΔE^*_{ab} =1). This is similar for the colours of the test chart 1 for colour rendering. This test chart is shown in Fig. 20 on page 28 for the intended device colour output and in Fig. 21 for the intended elementary colour output. Again the mean difference is below

threshold and similar for the 81 colours in the hue planes *R*-*C*, *Y*-*B*, and *G*-*M* for the two intentions device colour and elementary colour output.

Compared to other output methods the accuracy is by a factor 10 higher, for example compared to ICC colour management according to ISO 15076-1. The reason is the different coding and use of the CIELAB output data of the sRGB colour space.

According to CIE 168 the sRGB colour space fills only 20% of the CIELAB coding space.

The standard sRGB space according to ISO 9241-306 with 2,5% room light reflection fills half of the space defined by no room light reflection.

Therefore the coding of the for example 729 measurement data between -128 to 127 (8 bit) for CIELAB a^* and b^* and between 0 and 100 for L^* produces at least coding errors of ΔE^*_{ab} =1. These errors are here avoided, because only the $L^*a^*b^*$ data of a 48 step colour circle are used with for example two digits after the comma for the three CIELAB data $L^*a^*b^*$.

Similar tables compared to Table 8 on page 29 with the colour differences ΔE^*_{ab} are available

- for different room light reflections on the screen or
- for different CMY and CMYK printers with only rgb input or
- for different CMY and CMYK printer with the additional cmyk input or

- for CMYK offset print with rgb or cymk input.

In these cases the standard deviation of the general colour output plays a larger role and increases the colour differences ΔE^*_{ab} between the intended and the real output.

For example the 6 basic colours *RYGCBM* are 3fold on the test chart with the 1080 colours (Fig. 17 on page 21).

A digital photo printer with rgb or cmy0 input data has shown a standard deviation near ΔE^*_{ab} =0,5.

For two laser printers no. 1 and 2, and offset print, all with *cmyk* input data in the file, the output colour depends often on the colours of the neighborhood and is between $\Delta E^*_{ab}=2$ and 5.

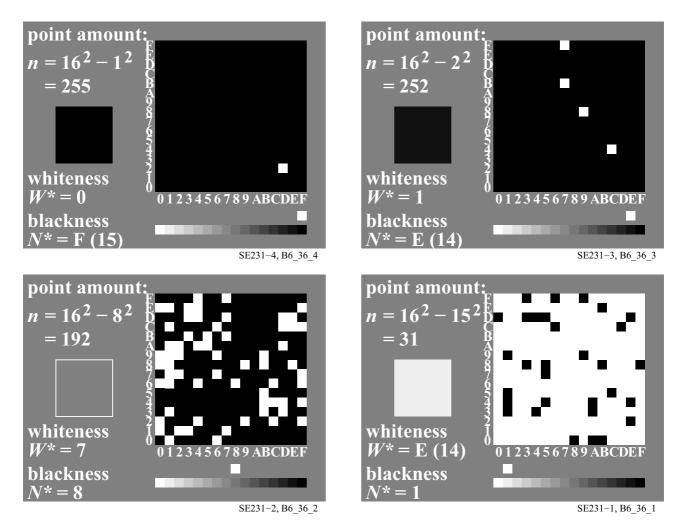
In addition for the laser printer no. 2 with only *rgb* data in the file the very irregular start output produces problems and irregular output, see Fig. 31 on page 42.

Therefore, and in addition, the colour differences ΔE^*_{ab} are dependent on device specific properties of printers and offset print.

The accuracy of the proposed method of output linearization of this paper is given in Table 8 and is below $\Delta E^*_{ab} \leq 1$. This is below the visual threshold.

For displays the value $\Delta E^*_{ab} \leq 1$ is only possible with 14 or 16 bit displays.

If the display output luminance is coded only with 8 bits, then only 16 equal steps are possible which differ by the value $\Delta L^*=6,7$ (=100/32), compare the relation between luminance and lightness in Fig. 22 on page 31. This is much higher compared to the threshold lightness $\Delta L^*=1$.



8.1 Equidistant grey scales for standard and different luminance contrast ratios

Fig. 22 - Equidistant grey scale with 16 steps

Fig. 22 describes one possibility to produce a visually equidistant grey scale. A square of the size 0,16 mm x 0,16mm is filled by 256 points. These points are again squares of the size 0,01 mm x 0,01 mm. Fig. 22 shows how to use a digital image setter with these properties to produce a grey scale with 16 visual equidistant steps. Black N is produced without any or one point in the black square. The large square has the size of the human visual resolution limit. This limit is often given as 60 lines/cm or 6 lines/mm which leads to a line width of 1/6 mm.

If the 16 step grey scale shall be equidistant, then no or one white point produces black. More points of the amounts 4, 9, 16, 25, ...225, and 256 produce the visual equidistant grey scale. The 16 steps may be described by the hexadecimal number 0,1,...9,A,...D,F, compare the figure. It is important to realize that

- for a grey near the middle (blackness N*=8) 192 (=256-64) points are still black and only 64 white,

- the first two steps near black N differ by an amount of 3 (=4-1) points (blackness F and E),

- the last two steps near white W differ by an amount of 31 (=256-225) points (blackness 1 and 0).

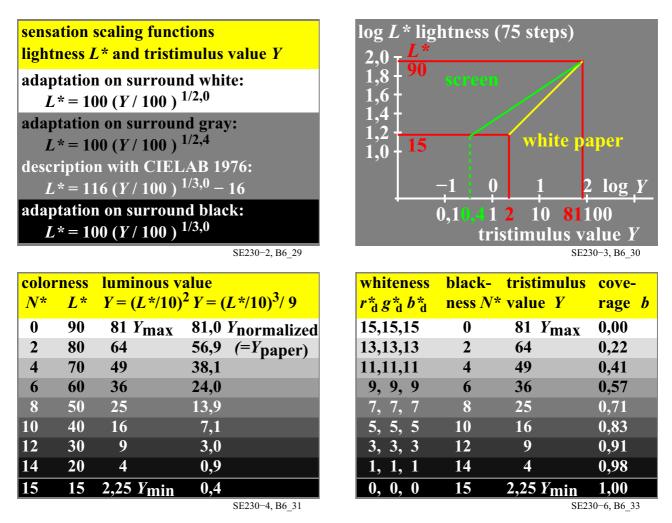
In the example the luminance L increase linear with the amount of points. However the lightness L^* which describes the equal visual spacing increase with the square root of the luminance L. It is valid

 $L^* = L^{1/2} - 1$ $L^*=0, 1, 2, ...5, 15$ (or in hex 0, 1, 2,...9,A,...D,F); L =1, 4, 9, 16, ...225, 256

In printing and other applications instead of the lightness L^* the blackness $N^* = 16 - L^*$ is used. In colorimetry the CIELAB lightness in the range between 0 and 100. The tristimulus value Y is linear related to the luminance L and the following CIELAB equation and two approximations are in use

$$L^* = 116 (Y/100)^{1/3} - 16$$
 with the approximation $L^* = 100 (Y/100)^{1/2,4}$ or roughly $L^* = 100 (Y/100)^{1/2}$

The last formula with the square root (exponent 1/2) is a good approximation for a white surround. The exponent (1/2,4) is used in the sRGB colour space according to IEC 61966-2-1 and more useful for a grey surround. The CIELAB formula produces for Y=2,5 the lightness L*=18 and for Y=88,6 (white standard offset paper) the lightness L*=95,4. Therefore the standard lightness range on standard paper is Δ L*=77,4 and the luminance contrast is $Y_W:Y_N = 88,6:2,5 = 36:1$. ISO 9142-306 defines this contrast as standard contrast range C_{Y5}. There are 8 luminance contrast ranges C_{Y8}, C_{Y7}, ... C_{Y1} with the luminance contrast ratios 288:1, 144:1, 72:1, 36:1, 9:1, 4.5:1, 2.25:1. The luminance contrast range C_{Y8} may appear with an emissive display in a dark room with no room light reflection on the display. The luminance contrast range C_{Y1} may appear on a data projector screen within a room illuminated by much daylight.



8.2 Tristimulus value Y, lightness L^* blackness N^* , and equidistant grey scale

Fig. 23 - Different sensation scaling functions for a white and black surround and example data

Fig. 23 shows different sensation scaling functions for a white and black surround (top left). In the case of output linearization the CIELAB correction below Y=0.8 is not necessary. For the standard sRGB display according to ISO 9241-306 and the standard offset print according to ISO/IEC 15775 the luminance factor has the value Y=2.5 for black. The CIELAB lightness is given in the top right and the bottom left figure. The corresponding value Y of the approximation equations are given as example.

Table 9 - Contrast steps C_{Y1} to C_{Y8} and luminances for offset paper and	data projector displays
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step C _{Yi} and Y- ratio (i=1 8)	lus values; Ratio	Range Y _{N1} Y _{N2}	lumi- nance ²⁾ ; Ratio [cd/m ²]	Display (P) lumi- nance ²⁾ ; Ratio [cd/m ²] L _{WP} : L _{NP}	application and colour mode at work place; illuminance on display 500 lux or 250/125/62 lux
C _{Y8} 288:1	88,9 : 0,31	0,00 <0,46	142 : 142/288	142*36 :018	display, only 062 lux
$C_{\rm Y7}$ 144:1	88,9 : 0,62	0,46 <0,93	142 : 142/144	142*36 : 035	display, only 125 lux
C _{Y6} 72:1	88,9 : 1,25	0,93 <1,87	142 : 142/72	142*36 : 071	display, only 250 lux
	88,9 : 2,50	1,87 <3,75	142 : 142/36	142*36 : 142	display & surface
	88,9 : 5,00	3,75 <7,50	142 : 142/18	142*18 : 142	display & surface
	88,9 : 10,0	7,50 <15,0	142 : 142/09	142*09 : 142	display & surface
$C_{y_2}^{13}$ 4,5:1	88,9 : 20,0	15,0 <30,0	142 : 142/4,5	142*4,5 : 142	display & surface
$C_{\rm V1}^{12}$,25:1 ³⁾	88,9 : 40,0	30,0 <60,0	142 : 142/2,25	142*2,25 : 142	display & surface

2) 500 lux corresponds to the viewing luminance L_v =142 cd/m² for a standard white paper with the tristimulues value Y_W =88,9. 3) For the contrast C_Y =2:1 the viewing luminances of both the black in the projection and the white standard offset paper are equal (!). Visual fatique caused by the adaptation luminance ratio 36:1 of the black at the screen and the black at the paper shall be reduced. If for example a grey screen with the CIE tristimulus value Y_Z = 22,2 (=0,25*88.9) is used the contrast step C_{Yi} remains constant. Then the luminance ratio of all colours at the screen and the paper has reduced to 9:1. This reduces visual fatique.

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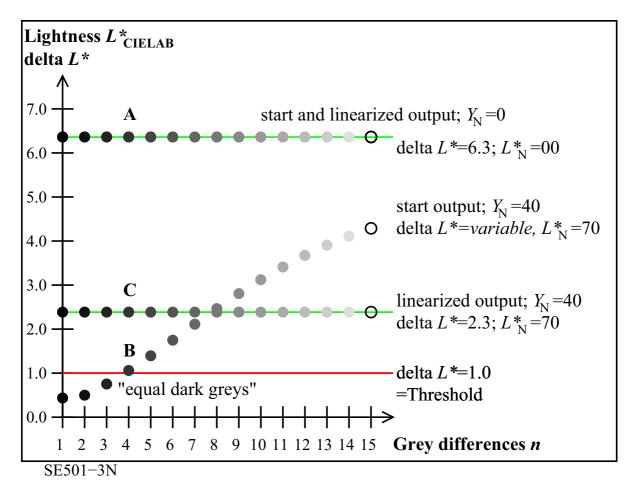
Table 9 shows in the first column the contrast steps C_{Y1} to C_{Y8} . According to ISO/IEC 15775 for offset print on standard offset paper the **standard** contrast step C_{Y5} is reached (see bold line). The standard output has the contrast value 36:1 which corresponds to the tristimulus value ratio $Y_W: Y_N = 88,6:2,5$ of White and Black. The offset **standard** contrast step C_{Y5} is accepted as a high quality contrast. The silky matte black of offset print has for the CIE 45/0 measuring and viewing geometry the luminance reflection 2,5% (Y_N =2,5). Usually all matte blacks of surface colours have a luminance reflection near 4%, so usually the contrast step C_{Y5} may be one step lower.

In offices and at many work places the **standard** illuminance is 500 lux, see ISO 8995-1:2002(E)/CIE S 008/ E:2001 — Lighting at Work Places

The standard illuminance 500 lux produces the luminance 142 cd/m² for the white offset paper with the tristimulus value 88,6. Therefore the printed offset black has the luminance 142 cd/m² divided by 36 which is about 4 cd/m².

In Table 9 it is assumed that the standard illuminance 500 lux produces the luminance 142 cd/m² on a white display screen of offset paper. Then for example a data projector must produce a 36 times larger luminance to reach the standard contrast step $C_{\rm Y5}$ of offset paper. At present no data projector reaches these luminances on the white screen. Therefore the visual change as function of contrast step has to be considered. For example the illuminance on the white screen may be reduced to 62 lux instead of 500 lux to reach the larger contrast step, for example by shutters.

Some more information about the eight contrast steps for displays is given in the following



8.4 Start and linearized output of displays for eight different contrast ratios



Fig. 24 shows the change of 15 sample differences by different luminance reflections at the emissive or data projector display.

In a dark room and for equal colour input values r=g=b of the *sRGB* colour space according to IEC 61966-2-1 the output produces equally spaced grey step with a lightness difference of delta $L^*=6,3$. The largest contrast step C_{Y8} is reached.

In Fig. 24 in an office with much daylight the ambient light reflection may produce the tristimulus value Y_N =40 for Black *N* and therefore the lowest contrast step C_{Y1} . In this case the illuminance of the data projector at the screen is about equal compared to the ambient illuminance. In this case four grey differences are below the threshold (ΔL *=1) and look black.

However, in Fig. 24 a *linearized output* produces 15 equal grey differences with delta $L^*=2,3$. Therefore again a 16 step equally spaced grey scale is visible. The grey difference is by about a factor three smaller compared to the dark room condition.

In general equally spaced grey and colour scales in a dark room are not any more equally spaced for different display reflections produced by the ambient light. It can be shown by colorimetry, that an appropriate "Gamma change" produces the intended linearized output for any display reflection.

Contrast steps C_{Yi} (i=1 to 8), and absolute and relative Gamma according to ISO 9241–306 ¹⁾								
step C _{Yi} and <i>Y-</i> ratio	Ratio	lus values; Range	Gamma G_{Pk} (k=0 to 7) for display (P) with G_{P0} =2,4 ²⁾	Gamma g_{Pk} (k=0 to 7) for display (P) with G_{P0} =2,4 ²⁾	application and colour mode at work place; illuminance on display 500 lux or 250/125/62 lux			
C_{Y5}^{10} 36:1 C_{Y4} 18:1	88,9 : 0,62 88,9 : 1,25 88,9 : 2,50 88,9 : 5,00 88,9 : 10,0 88,9 : 20,0	0,00 <0,46 0,46 <0,93 0,93 <1,87 1,87 <3,75 3,75 <7,50 7,50 <15,0 15,0 <30,0 30,0 <60,0	$G_{P1} = 2,22$ $G_{P2} = 2,04$ $G_{P3} = 1,86$ $G_{P4} = 1,68$ $G_{P5} = 1,50$ $G_{P6} = 1,32$	$g_{P0} = 1,000$ $g_{P1} = 0,925$ $g_{P2} = 0,850$ $g_{P3} = 0,775$ $g_{P4} = 0,700$ $g_{P5} = 0,625$ $g_{P6} = 0,550$ $g_{P7} = 0,475$	display, only 062 lux display, only 125 lux display, only 250 lux display & surface display & surface display & surface display & surface display & surface			

a for data projectors (P) with G_{p_0} =2,4. Compare IEC 61966–2–1: G_{p_0} =2,4.

2) The computer operating system Apple has used the value 1,8 until 2010. The change to 2,4 (= Windows) is in the wrong direction. 3) For the contrast $C_y = 2:1$ the viewing luminances of both the black in the projection and the white standard offset paper are equal (!). Visual fatique caused by the adaptation luminance ratio 36:1 of the black at the screen and the black at the paper shall be reduced. If for example a grey screen with the CIE tristimulus value $Y_Z = 22,2$ (=0,25*88.9) is used the contrast step C_{y_i} remains constant. Then the luminance ratio of all colours at the screen and the paper has reduced to 9:1. This reduces visual fatique.

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The eight contrast steps of Table 10 correspond to different absolute gamma values G_{Pk} (k=0 to 7). The absolute gamma value G_{P0} = 2,4 is defined for the rgb data in the sRGB colour space according to IEC 61966-2-1 for no screen reflection in the dark room. The nonlinear data of the sRGB colour space which may be named rgb* according to colorimetry are defined by the equations

 $r^* = r^{(1/2,4)}$ $g^* = g^{(1/2,4)}$ $g^* = g^{(1/2,4)}$

The value G_{P0} = 2,4 in the exponent is called the absolute gamma value. According to Table 10 the value shall be G_{P0} = 1,86 for the standard viewing condition of the contrast step C_{Y5} . Therefore in this case the modified rgb* data are defined by the equations

$$r^* = r^{(1/1,86)}$$
 $q^* = q^{(1/1,86)}$ $q^* = q^{(1/1,86)}$

It is assumed that the exponent G_{P0} = 2,4 of the sRGB colour space according to IEC 61966-2-1 is used by the hardware - software workflow. In Table 10 the relative gamma values g_{Pk} (k=0 to 7) are defined as

These values $g_{\rm P}$ are given at the bottom of any test chart. The graphs on page 3 show approximately the relative gamma values g_{Pk} and the inverse gamma values 1/ g_{Pk} . For example the relative gamma value g_{P3} =0,775 (=1,86 / 2,4) change the linearized output in a dark room (L_r =0,3) to a linearized output in the office room ($L_r=2,5$).

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8.6 Summary for display output

Table 8 on page 29 shows that the colour differences of the developed linearization method reach the value around ΔE^*_{ab} = 0,6 for both the device and the elementary hue output. This is below threshold defined by ΔE^*_{ab} = 1.

For eight display reflections of the room light a gamma change between 2,4 and 1,14 produces equal output spacing for eight contrast steps defined in Table 10 on page 35.

9 Methods of affine and minimum colour difference output for displays and prints

9.1 Definition of affine colour reproduction between displays and printers or offset print

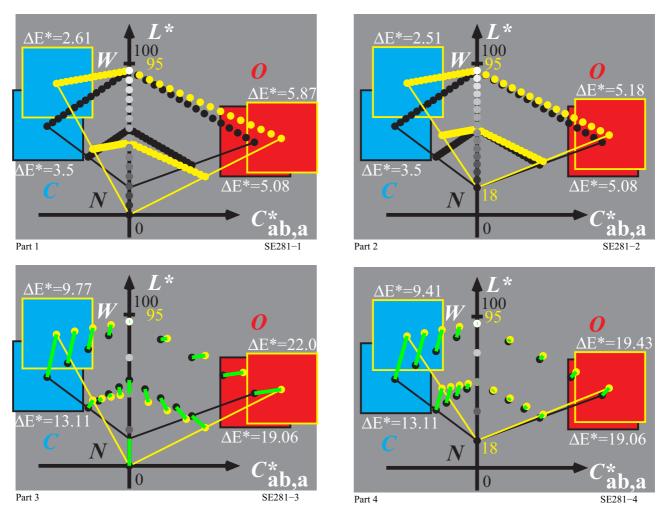
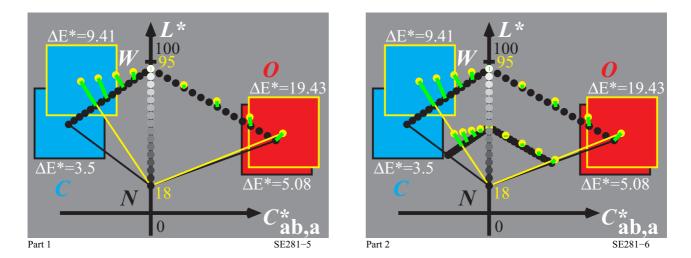




Fig. 25 shows the affine (linear) colour transfer between the standard linearized display and the offset output. In the top figure (left and right) 16 steps of the display (yellow balls) and printer (black balls) are shown. The display differs by the output of black with the lightness $L^*=0$ (left) and $L^*=18$ (right). The standard lightness $L^*=18$ is defined for standard offset output according to ISO/IEC 15775 and for standard display output according to ISO 9241-306.

The two bottom figures show a complex transfer on the left side and the more simple on the right side. Any colour of the yellow triangle is shifted to a colour of the black triangle. Therefore any colour on the display transfers to a reproducible colour on the printer. The whole triangle gamut of both the display and the printer is used.

However, the lightness L^* of all cyan colours on the printer is lower compared to the lightness of the display colours (bottom right).



9.2 Definition for minimum colour difference reproduction between displays and printers



Fig. 26 shows the "Minimum colour difference" transfer between linearized display and printer output. Again the 16 steps of the display (yellow balls) and printer (black balls) are shown. Both transfer s(left and right) have a shift of the light colours. In addition the darker colour series is shifted on the right side. The minimum colour difference ΔE^*_{ab} according to CIELAB is only reached on the left side. However, the "standard" ISO 15076-1 (ICC colour management) allows many proprietary solutions, which are to a high degree used. They are all called colour management according to ISO 15076-1.

In both cases of the colour transfer in Fig. 26 any colour of the yellow triangle is shifted to a colour of the black triangle. Therefore any colour on the display transfers to a reproducible colour on the printer.

However, the whole triangle gamut of the printer is **not** used, only about 70% for the cyan hue. Many colours which differ on the display are equal on the printer. There is loss of colour information for about 20% of the colours of the display for the cyan hue. Still up to now many printer companies seem to favor this kind of reproduction and use it especially for the so called RGB printers with the usual *rgb* input. These printers allow only *rgb* data in the files. In case of *cmyk* data in the file there is first a device-dependent and software-dependent change to rgb values and the again a change to *cmyk* within the printer.

In addition some companies produce the output according to company specific "user wishes or preferences" Usually companies produce more light colours compared to the affine reproduction. An example will be shown later in Fig. 31 on page 42

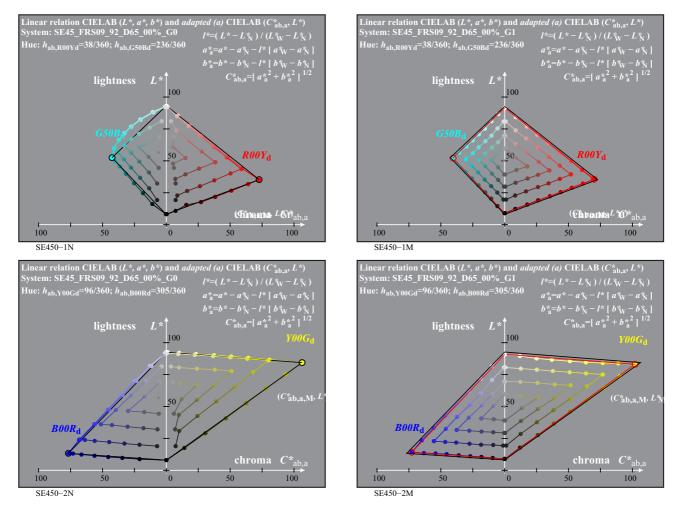
The different device colours, the "Minimum colour difference" criteria, and the company specific consider of user wishes produce equal colours on the printer for many very different colours on the screen. This may be called a colour chaos in the colour reproduction. Some colour differences of the 16 step series on the display with a value $\Delta E^*_{ab} = 5$ are often reduced below the threshold with $\Delta E^*_{ab} = 1$ and are not distinguishable. There is a large variety of outputs on the market.

However, for the affine transfer there is only one solution. The output properties can be evaluated visually without any measurement equipment, for example with the test charts of DIN 33872-2 to -6, see http://www.ps.bam.de/33872E

For the 16 step series the value $\Delta E^*_{ab} = 5$ may vary depending on the display or the printer. Fig. 25 on page 36 shows for the series between white and cyan and white and red the differences between $\Delta E^*_{ab} = 2,51$ and 5,18.

(right). Therefore all the steps are visible (ΔE^*_{ab} >1) on both devices and there is no loss of colour difference information.

10 Start and linearized output of printers with CMY and CMYK device colours



10.1 Linearization of a CMY photo printer with rgb data in the file

Fig. 27 - Start and linearized output in CIELAB hue planes R_{d} - C_{d} , and Y_{d} - B_{d}

Fig. 27 and many of the following figures show the start output on the left side and the linearized output on the right side. The examples in Fig. 27 and Fig. 28 on page 39 are for a photo printer which holds the 1-Minus-Relation. Either the PS operator *rgb setrgbcolor* or 1-r-1g 1-b 0 setcmykcolor produce the same output.

The 1-Minus-Relation is for example valid for *Adobe FrameMaker 8 on Windows*. It is for example usually valid for the operating system *Unix*. All the PS figures on the servers

http://www.ps.bam.de and http://130.149.60.45/~farbmetrik

have been developed with the software *Decwrite* on the operating system *Compac VMS* which holds the colorimetric 1-Minus-Relation. The 1-Minus-Relation was valid for the operating system Mac OSX until version 10.2 (about 2004). At that time the colour output switched to a colour output which is similar to the output of the software *Adobe Reader*. The output of this software differs according to the version. A larger change in the gamma function appeared between version 3 and 4 (about 2004).

In Fig. 27 the start output (left) of the photo printer produces a colorimetric tint (ΔE_{ab}^* about 5) for many grey steps. The grey axis is defined by the CIELAB data (a_W^* , b_W^*) of white and (a_N^* , b_N^*) of black and differs only slightly from the intended zero values for all these data.

In Fig. 27 the linearized output (right) of the photo printer produces a regular spacing within the hue planes R_d - C_d and Y_d - B_d . The grey scale is equally spaced in L^* . The grey scale is now achromatic and in that case printed by the CMY photo colorants. All the plots of Fig. 27 are based on real measurements of the start and linearized output. The colour difference between the intended and real colour is near the value ΔE^*_{ab} =0,5.

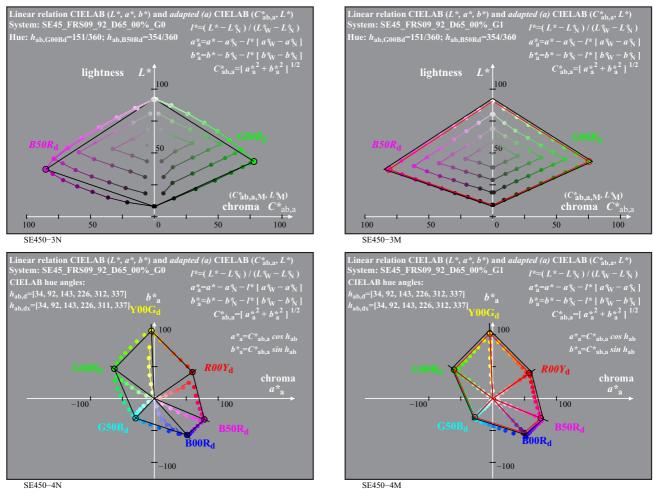
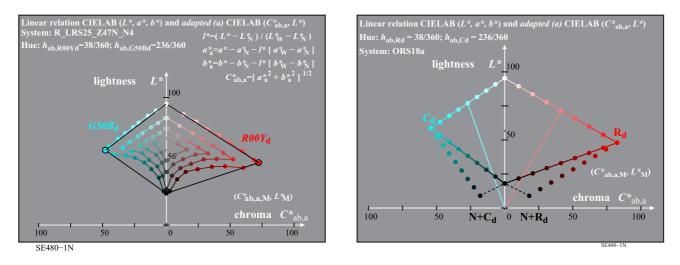


Fig. 28 - Start and linearized output in CIELAB hue planes G_d - M_d , and for hue circle

Fig. 28 shows again the start output on the left side and the linearized output on the right side for the photo printer. The two top figures for the hue plane $G_d - M_d$ show similar properties compared to Fig. 27 on page 38.

The two bottom figures show the six series between white and the most chromatic colours in a CIELAB (a^* , b^*) diagram. The start output shows some change of the CIELAB hue angle h_{ab} . The linearized output shows the samples on straight lines as intended.

NOTE: In Fig. 28 it was intended to produce the colours on a hexagon, for examples on a line between Y_d and G_d in the diagram (a^* , b^*). For the present software versions of the output linearization the possible maximum chroma is produced for any hue angle. Instead of 6 device hues a 48 step colour circle is used as reference for the colours of maximum chroma. For example this chroma is between Y_d and G_d larger compared to the black connecting line between Y_d and G_d .



10.2 Linearization of a CYMK laser printer no. 1 with two transfers rgb - cmyk in the file

Fig. 29 - Two start outputs with the separations cmyn4* and cmyn5* on a CMYK laser printer

Fig. 29 shows start outputs with the separation methods *cmyn4*^{*} and *cmyn5*^{*} for a *CMYK* laser printer with cmyk data in the file. There are many method to transfer *rgb* data in the file to *cmyk* data in the file. CIE colorimetry and PostScript define the 1-Minus-Relation which transfers

the PS operator *r g b setrgbcolor* to

the PS operator c m y k setcmykcolor.

For the most chromatic colours it is valid c=1-r, m=1-g, y=1-b, and k=0. For all colours it is valid w=min(r g b), c=1-r-w, m=1-g-w, y=1-b-w, and k=w.

The value *w* is subtracted from the original three values *cmy*. This method is called under colour removal and has the property that for all grey colours with r=g=b only black is used for the print. Therefore the printed black (for example in colour figures) is always printed only by the black colorant. This reduces the printing costs compared to the overprint of three colorants to produce black.

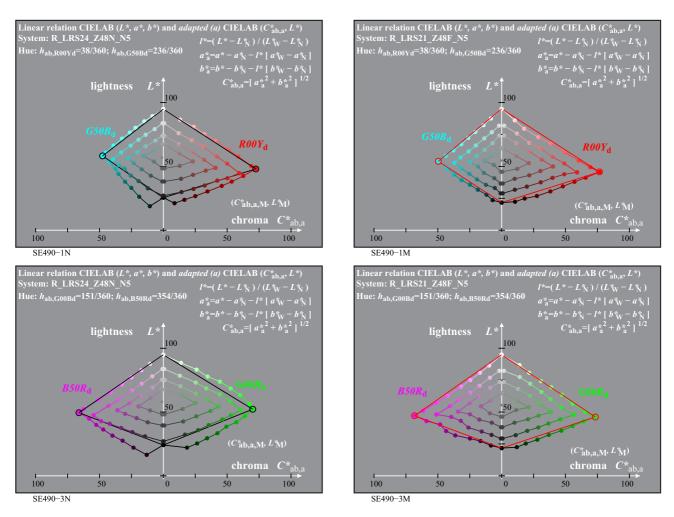
However, Fig. 29 (left) shows that many dark chromatic colours can not be not printed. This unwanted case is avoided in Fig. 29 (right). Here different amounts of black between 0 and 100% are printed on top of R_d or C_d . However this output produces a black with a reddish tint or cyan tint. Both colours have a lightness lower compared to the lightness of the black colorant and in addition there is a gap near black *N* produced by only the black colorant.

For the intention to produce all the colours up to the triangle line between black *N* (only) and R_d or C_d , there is the following solution. For example if 50% cyan and 50% black are overprinted the result is a whitish cyan. There explanation is as follows. If 50% cyan is printed then 50% of the white paper is now cyan. If in addition 50% of black is printed, then 25% is cyan, 25% is black, 25% is overprint cyan and black, and 25% is still white. The result is a shift of the output colour $0.5(C_d+N_d)$ towards the white point.

For example this shift towards white can be avoided if for example 50% cyan and 75% black are overprinted which reduces the shift towards white. According to Fig. 29 some shift towards white is allowed. For total overprint the colours are below the line R_{d} -N or C_{d} -N.

Instead of the colour separation $cmyn4^*$ defined by the 1-Minus-Relation the colour separations called $cmyn5^*$ and $cmyn6^*$ have been used for output separation in this report. The lines R_d -N and C_d -N are reached by the start output of the fixed transfer $rgb \rightarrow cmyn5^*$ of this laser printer with a cmyk input channel.

The start and linearized output properties of such a printer will be discussed in the following.



10.3 Linearization of a CYMK laser printer no. 1 with a special transfer rgb - cmyk in the file

Fig. 30 - Two start and linearized outputs R_d - C_d and G_d - M_d with the separation cmyn5*

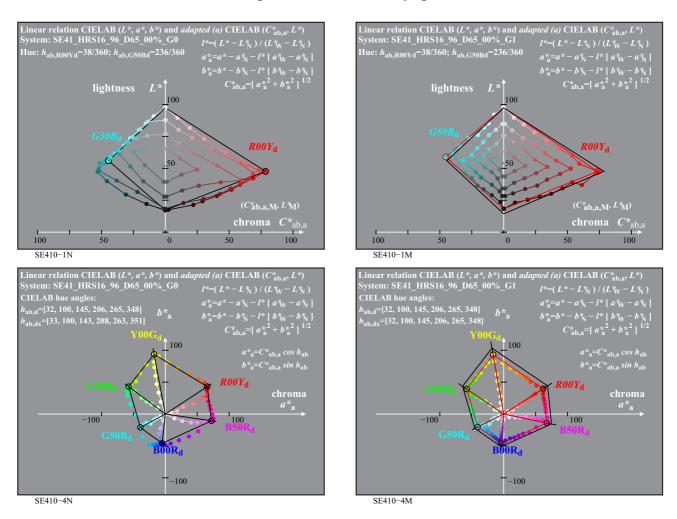
Fig. 30 shows two start and linearized outputs in the hue planes R_d - C_d and G_d - M_d on a CMYK laser printer with *cmyk* data in the file.

The cmyk data in the file are computed by a fixed separation equation called $cmyn5^*$. This equation transfers the *rgb* data in the file to *cmyk* data, and for example all data with r=g=b to only a k=w value.

This equation $cmyn5^*$ is different compared to the separation $cmyn4^*$ which can not produce the output colours on the line R_d -N and C_d -N, compare Fig. 29 on page 40 (left).

The output shows a reasonable spacing. However there is some more scatter compared to the photo printer in Fig. 27 on page 38 and Fig. 28 on page 39.

In addition the lightness L^* of black is near $L^*=24$ instead of $L^*=9$ for the photo printer.



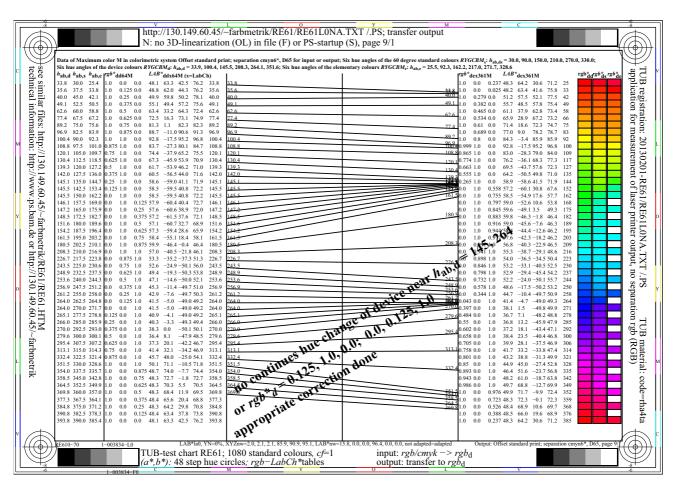
10.4 Linearization of a CMYK laser printer no. 2 with only rgb data in the file

Fig. 31 - Start and linearized output in hue plane R_d - C_d and in CIELAB diagram (a_a^*, b_a^*)

Fig. 31 shows the start and linearized output of a low cost *PostScript* laser printer of a leading printer company. This *Postscript* printer has two input channels for *rgb* and *cmyk* data in the file.

For equivalent *rgb* and *cmyk* data in the file the output is very different, see for example the output of page 1 of the test chart with 1080 colours in Fig. 17 on page 21.

In addition Fig. 31 shows an example output similar to the output of many RGB printers on the market. For many different *rgb* data in the test chart file with the 1080 colours the output colours appear equal, for example for the light cyan colours. This property is expected by the "minimim colour difference method" of Fig. 26 on page 37.



10.5 Hue transfer of a CMYK laser printer no. 2 with rgb data in the file

Fig. 32 - rgb and CIELAB data of a 48 step hue circle of a laser printer with only rgb data in the file

Fig. 32 shows the *rgb*- and CIELAB data for the standard 48 step hue circle of a *CMYK* laser printer no. 2. Only *rgb* data are used in the file. This is now the common method to describe colours in files, on the desktop and in the internet. Column 2 includes 48 different *rgb* input values in the file with a continues spacing of eight steps, for example between $rgb_{d,R}$ =(1 0 0)_d and $rgb_{d,Y}$ =(1 1 0)_d. The 48 steps are distributed in the standard file with the 1080 colours. For the position see for example the page 18 of the file http://130.149.60.45/~farbmetrik/RE69/RE69L0FP.PDF

In column 2 for any *rgb* data set one of the three *rgb* data has the value 0 and another the value 1. This indicates that the 48 steps produce the maximum (M) chroma which is possible with this printer. Real measurement data in CIELAB of the output are included in column 2. Usually there is a continues change of the CIELAB hue angle for a continues change of the *rgb* data. However, the laser printer 2 shows some hue changes backwards near $rgb_d=(0,125 \ 1 \ 0)_d$ and $rgb_d=(0 \ 0,125 \ 1)_d$. In addition a large range of *rgb* input values produce nearly the same hue output colours near $h_{ab}=152$ (roughly near G_e with $h_{ab,e}=162$), near $h_{ab}=264$ (roughly near B_e with $h_{ab,e}=271$), and near $h_{ab}=33$ (roughly near R_e with $h_{ab,e}=26$). Therefore many steps of the output circle look very similar and in addition near the elementary colours R_e , G_e , and B_e .

The intention of this report is to produce an equally spaced colour circle between the four elementary colours $RYGB_e$. The hue angles $h_{ab,e}$ of this circle are known, see the values in third column between $h_{ab,e}$ =25 towards $h_{ab,e}$ =385 (=25). The data in column 2 include a continues hue change $h_{ab,d}$ of the device colours and the corresponding rgb_d and $(L^*C^*_{ab})_d$ data. For the $h_{ab,e}$ data listed in column 3 the corresponding rgb_e and $(L^*C^*_{ab})_e$ data are calculated by linear interpolation. Pages 7 to 16 of the file http://130.149.60.45/~farbmetrik/RE69/RE69L0FP.PDF

include the corresponding data for habe between 0 and 360 degree which allow a fast calculation for any hue

angle of any *rgb* data. The indices *dd* (= device to device hue) and *de* (=device to elementary hue) and M (maximum chroma) are used for the *rgb* and $L^*a^*b^*C^*_{ab}h_{ab}$ data of the two colour circles in column 2 and 3.

10.6 Hue transfer of *CMYK* laser printer no. 2 with a transfer *rgb* -> *cmyk* data in the file

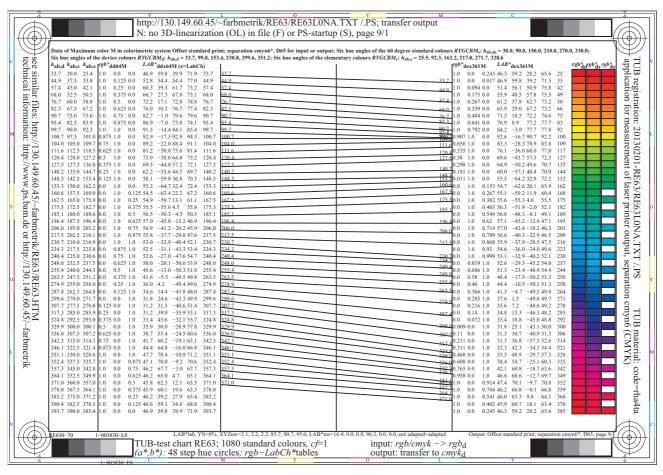


Fig. 33 - rgb and CIELAB data of a 48 step hue circle with cmyn6* separation

Fig. 33 shows the rgb- and CIELAB data of the *CMYK* laser printer no. 2 for the standard 48 step hue circle. Now the *rgb* data in the file have been changed by the separation method *cmyn6** to *cmyk* data. This method uses complete under colour removal and therefore the grey scale is only printed by the black colorant.

Fig. 32 on page 43 and Fig. 33 shows the hue circle output of the same laser printer no. 2 which look very different. Fig. 32 on page 43 is based on only rgb data in the file and Fig. 33 is based on the transfer of *rgb* to *cmyk* data in the file or by the *Frame File Linearization Method* (FF_LM), see Table 7. The hue output is much more regular except near $h_{ab,e}$ =100 (roughly near Y_e with $h_{ab,e}$ =92). The interpolation methods for the calculation of the *rgb*_{de} and (L*a*b*C*_{ab})_{de} data as function of $h_{ab,e}$ are the same in Fig. 32 on page 43 and Fig. 33. A higher accuracy of the intended hue is expected because of the much more regular spacing of the start output as function of $h_{ab,e}$.

The intended larger hue angle differences Δh_{ab} for the dark output area between green via blue towards red is indicated by producing only every second step in colour in this region, see the last vertical colour circle. The lines in Fig. 33 show a trend for the intended larger hue angle difference of the dark output area between green via blue towards red. This already helps to produce a colour circle similar to an elementary colour circle which is visually equally spaced.

10.7 Summary for start and linearized printer output

There are printer on the market with the same output for *rgb* and *cmyk* data according to the 1-Minus-Relation. It is hard to linearized at least some of the *CMYK* printers of the market with *rgb* input data in the file. However this is the usual use of many of the printers which usually have no *cmyk* input channel.

For any *PostScript* printer there is according to the PS Reference Manual a *cmyk* input channel. Here a user can change the *rgb* data in the file by different methods, for example by the Frame File Linearization Method (FF_LM). FF_LM changes the *rgb* data at least of any figure of this paper towards *cmyk* data usually at the moment of the device output. The result is a linearized output which fulfils all the user wishes of DIN 33872-2 to -6.

11 Start and linearized output for CMYK offset print

11.1 Hue transfer of CMYK offset print with transfer rgb -> cmyk in the file

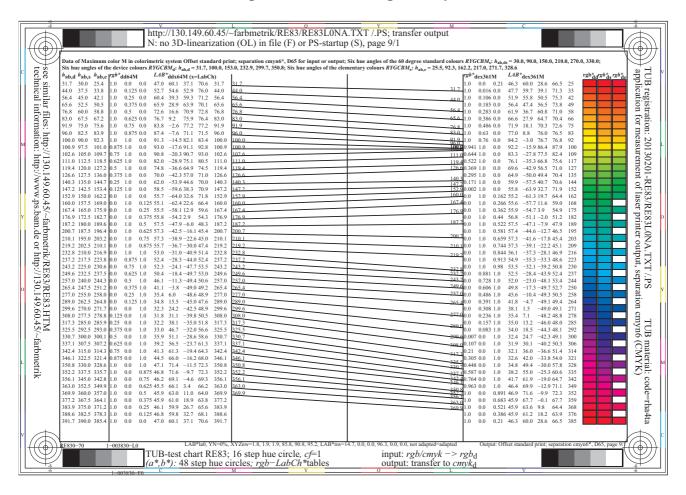


Fig. 34 - rgb and CIELAB data of a 48 step hue circle for the device and elementary offset colours

Fig. 34 shows the *rgb*- and CIELAB data of the *CMYK* offset print for the standard 48 step hue circle. Similar as in Fig. 33 on page 44 the *rgb* data in the file have been changed by the separation method *cmyn6** to *cmyk* data. This method uses complete under colour removal and therefore the grey scale is only printed by the black colorant.

Fig. 34 and Fig. 33 on page 44 look very similar. Many printer manufacturers use inks and toners which have roughly similar spectral reflection curves compared to the inks used in standard offset print. Therefore the conclusions for the laser printer no. 2 and offset with *rgb* data in the file and the separation method *cmyn6** in the file are similar. In most cases the user wishes according to DIN 33872-1 to -6 are fulfilled by output linearization and the use of the 1-Minus-relation. A visual user test with Yes/No criteria is sufficient and effective. No measuring equipment is needed.

The accuracy of the printer output, and of the standard offset output depends on different factors. Any output of the standard offset process is usually proofed at least by four 5 step colour scales. This visual evaluation or colorimetric specification uses equally spaced *cmyk* data between white and *CMYN*_d in the test file. If there are visual differences of the offset print output, then the offset machine is usually adjusted to reach this goal. Therefore to a high degree the start offset output of the 16 step series is already visually equally spaced. Fig. 20 on page 28 shows the 54 colours of the test chart 1 for colour rendering. For this test chart the colour differences between the intended and measured colours are $\Delta E^*_{ab,dd}=2,0$ and $\Delta E^*_{ab,de}=2,4$, see page 19 (series 1 and 2) of the file

http://130.149.60.45/~farbmetrik/RE83/RE83L0FA.PDF

11.2 Summary for offset print output and comparison with printer output

For offset print the linearization to fulfill to the user wishes according to DIN 33872-1 to -6 is successful. A visual user test with Yes/No criteria is sufficient and effective. No measuring equipment is needed.

The accuracy of the printer and standard offset output depends on different factors.

Any output of the standard offset process is usually proofed at least by four 5 step colour scales. The *cmyk* data between white and the colours $CMYN_d$ are equally spaced in the file and shall produce equal visual differences. If there are no equal visual differences for the offset print output, then the offset machine is usually adjusted to reach this goal.

Therefore to a high degree the start offset output of the 16 step series is already visually equally spaced. Fig. 20 on page 28 and Fig. 21 on page 29 shows the 54 colours of the test chart 1 for colour rendering. For this test chart the colour differences between the intended and measured colours are $\Delta E^*_{ab,dd}=2,0$ and $\Delta E^*_{ab,de}=2,4$, see page 19 (series 1 and 2) of the file http://130.149.60.45/~farbmetrik/RE83/RE83L0FA.PDF

We have measured the standard deviation, for example for the 6 colours RGB_d and CMY_d which are all three times at different places of the test chart with the 1080 colours.

Both *CMYK* laser printers no. 1 and 2 show a standard deviation around ΔE^*_{ab} =4, and similar to offset. This seems the main reason that for the *CMYK* laser printer no. 2 the colour differences between the intended and measured colours are similar to offset with the values $\Delta E^*_{ab,dd}$ =2,1 and $\Delta E^*_{ab,de}$ =2,4, see page 19 (series 1 and 2) of the file

http://130.149.60.45/~farbmetrik/RE63/RE63L0FA.PDF

12 Device output properties and linearization methods

12.1 Device output for printers and offset machines

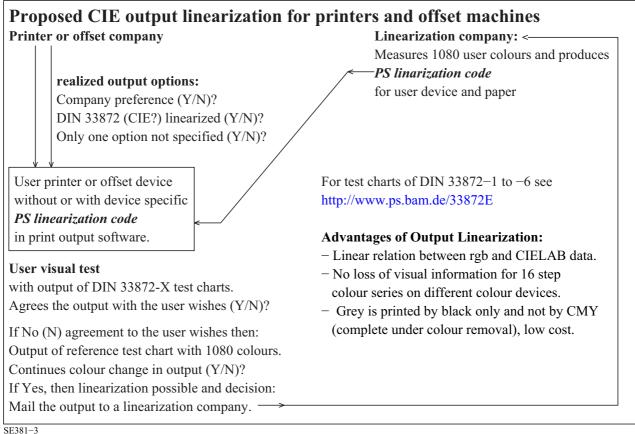


Fig. 35 - Proposed CIE output linearization for printers and offset machines

Fig. 35 shows one possible realization of a proposed CIE output linearization method. A user tests the output of the RGB or CMYK printer of a printer company, for example with the test charts according to DIN 33872-2 to -6. Usually the visual criteria will show if the user wishes of DIN 33872 are fulfilled or not. For the test charts and corresponding questions for the output see http://www.ps.bam.de/33872E

If there is no agreement to one or more user wishes the user may ask the printer or offset company for help.

If there is no help some user may have the possibility to measure the 1080 colours of the test chart output and may apply the Frame File Linearization Method (FF LM). Then the user has to copy the 1080 measurement data and the DIN 33872-X test file in PS format to the appropriate places in the Frame File, see Table 7 on page 26. An output of this file usually solves the user wish.

If the user has no possibility to measure the output color or has a low technical knowledge the user may send the paper output of the 1080 colours to a Linearization cCompany. He may get back a Frame File which includes the measurement data. The user or the Linearization company can include the test chart according to DIN 33872-X. An output of this file usually solves the user wish. If the user wish is solved then the user may pay for the help of the Linearization Company. He can use a Frame File to solve the problems for any user PS file. A PS file can be exported usually from any application.

However, there are limitations. Only the three operators r q b setrgbcolor, w setgray and c m y k setcmykcolor in the PS files are supported up to now. The output according to the user wish which includes the 1-Minus-Relation is expected for any PS files according to DIN 333872-X and any PS file of this paper.

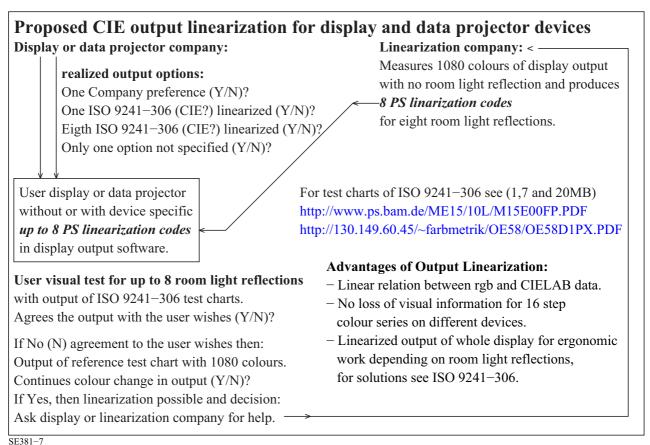


Fig. 36 - Proposed CIE output linearization for displays and data projector devices

Fig. 36 shows one possible realization of a proposed CIE output linearization method. A user tests the output of a display or data projector company, for example with the test charts according to DIN 33872-2 to -6. Usually the visual criteria will show if the user wishes according to DIN 33872-X are fulfilled or not. For the test charts and corresponding questions for the output see http://www.ps.bam.de/33872E

The procedure is similar compared to Fig. 35 on page 47.

In addition the user or the linearization company may produce a file according to the *Frame File Linearization Method* (*FF_LM*) which includes a loop for the eight standard room light reflections according to ISO 9142-306.

Depending on the reflection of the room light on the emissive display or the data projector display only one of the eight output pages shows the equal spacing of the 16 step series.

There are two files one for the black and white output and another for the colour output. There are Yes/No criteria for the visual evaluation of the output.

For a display output in black and white use the standard file according to ISO 9241-306, Annex D (16 pages, 1,7 MB)

http://www.ps.bam.de/ME15/10L/L16E00NP.PDF

For a display output in colour use the proposed standard file according to ISO 9241-306, Annex E (24 pages, 16 MB)

http://130.149.60.45/~farbmetrik/OE58/OE58D1PX.PDF

13 Summary

CIE R1-47:2009 Hue Angles of Elementary Colours defines the CIELAB hue angles $h_{ab,e}$ =26, 92, 162, and 272 with a standard deviation of about +/-4 for the four elementary (e) colours RYG_e , and +/-8 for Be.

According to *ISO TC159/SC4/WG2 Ergonomics* - *Visual Display Requirements* the four rgb_{e}^{*} -data sets $(1 \ 0 \ 0)_{e}$, $(1 \ 1 \ 0)_{e}$, $(0 \ 1 \ 0)_{e}$, and $(0 \ 0 \ 1)_{e}$ shall produce the four elementary hue angles $h_{ab,e}$.

Fig. 15 on page 19 shows a symmetric hue circle with this property. For example elementary red R_e is defined visually as neither yellowish nor bluish, and has the rgb_e^* data $(1 \ 0 \ 0)_e$. Red R_e is produced by the device to elementary (de) colour data $rgb_{de}=(1 \ 0 \ 0.26)_{de}$. There is only one well defined device-dependent transfer between any data rgb_e^* and rgb_{de} . The star (*) indicates that there is a linear relation between the hue angle $h_{ab,e}$ and the data rgb_e^* . Therefore for the intermediate colour between R_e and Y_e the hue angle has the value $h_{ab,R50Ye}$ =589 [=26+(26+92)/2], and is produced by the data rgb_e^* =(1 0,5 0)_e.

Fig. 27 on page 38 shows similar properties in a device hue plane red-cyan (R_d-C_d) for a start and the linearized output. For example there is a linear relation between $rgb_d^* = (0\ 0\ 0)_d$ for black *N* and $(1\ 0\ 0)_d$ for R_d and the CIELAB-data $(L^*C_{ab}^*)_d$ of both colours. In addition there is a linear relation between the CIELAB-data $(L^*C_{ab}^*)_{d1}$ and $(L^*C_{ab}^*)_{d2}$ of for example

- a display and a printer

- a device for two CIE standard illuminants

- a device for two CIE standard observers.

The transfer between two output possibilities is called an affine transfer. An example is given in Fig. 25 on page 36.

There are different output linearization methods, for example

- within a PS file
- with a PS frame file
- with a PS Startup Distiller directory
- with a PS In-Out Distiller directory
- with a device link profile

In any of these cases a transfer of the data rgb is calculated for example between the rgb data in a file and

- the rgb_{dd} data (dd=device to device colour) or
- the rgb_{de} (de=device to elementary colour)

in the same file for the output. The calculations are done within and during the workflow.

For example for the standard sRGB display with a display luminance reflection of L_r =2,5 the accuracy of the linearization method is usually 10 times higher compared to the method of ISO 15076-1 (ICC colour management). The table shows some results for two test charts and 81 colours of the three device hue planes R_d - C_d , Y_d - M_d , G_d - M_d and the elementary hue planes R_e - C_e , Y_e - M_e , G_e - M_e

For the standard sRGB display and **with output linearization** Table 8 on page 29 shows the mean colour difference $\Delta E^*_{ab}=0.6$ between the intended and real colours for any colour set. This value is below threshold $(\Delta E^*_{ab}=1)$.

For example, and for comparison, the colour difference **without output linearization** is ΔE^*_{ab} =11,4 for the 81 colours in the device hue plane G_d - M_d , and ΔE^*_{ab} =26,4 for the intended elementary hue circle of 48 steps together with a nine step grey scale.

The **device-independent elementary hue output** of this report is a step towards a visual human *RGB*^{*}_e colour space requested from *ISO/IEC JTC1/SC28 Office Equipment* to be developed within the CIE Division 1 and 8, see Fig. 6 on page 10.

The next research steps may be discussed together with the expected Reportership reports R8-09 and R1-57.

Annex A Definition and differences of *standard* and *relative* CIELAB data

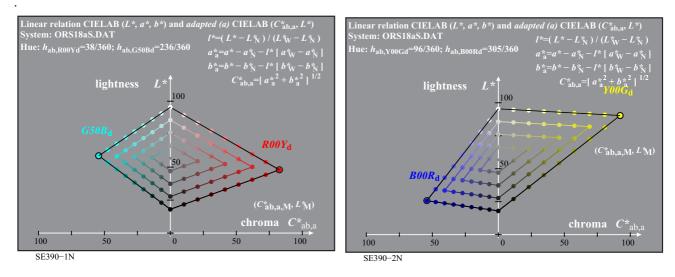


Fig. A.1 — Colour samples of ORS18a of hues R-C and Y-B in the adapted CIELAB diagram ($C^*_{ab.a}$, L^*)

Fig. A.1 shows examples for the calculation of colorimetric data from the standard CIELAB data and shows the colour samples of 9 step colour series at the border and the grey scale. The colours of the hue planes R_d - C_d and Y_d - B_d are shown in the cylindrical *adapted* CIELAB diagram ($C^*_{ab,a}$, L^*). The colorimetric *adapted* CIELAB data ($C^*_{ab,a}$, L^*) and h_{ab} are calculated from the *standard* CIELAB data L^* , C^*_{ab} , and h_{ab} or L^* , a^* , b^* . The coordinates relative lightness I^* , and adapted chroma a^*_a , b^*_a , and C^*_{ab} are defined in the figure.

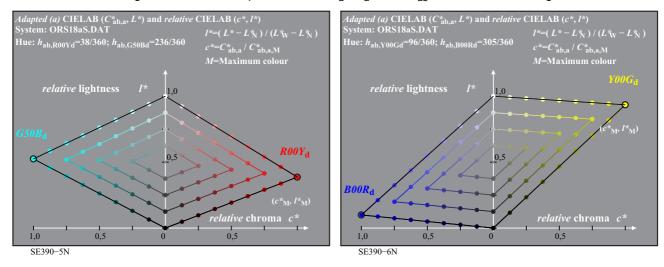




Fig. A.2 shows the same samples as in Fig. A.1. The colours of the hue planes R_d - C_d and Y_d - B_d are shown in the cylindrical relative CIELAB diagram (c^* , I^*). The coordinates relative chroma c^* and relative lightness I^* are defined in the figure. The calculation of the colorimetric *adapted* CIELAB data ($C^*_{ab,a}$, L^*) and h_{ab} is already given in Fig. A.1.

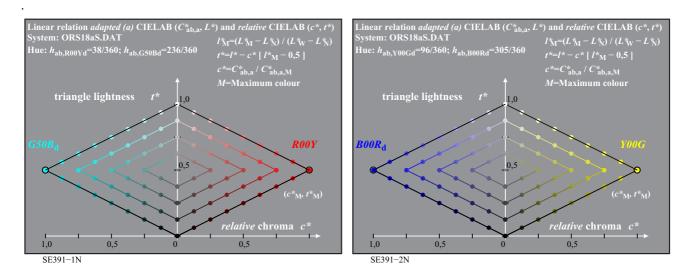


Fig. A.3 — Colour samples of ORS18a of the hues *R*-*C* and *Y*-*B* in the relative CIELAB diagram (c*, t*)

Fig. A.3 shows the same samples as in Fig. A.1 and A.2. The colours of the hue planes R_d - C_d and Y_d - B_d are shown in the cylindrical relative CIELAB diagram (c^* , t^*). The coordinates relative chroma c^* and triangle lightness t^* are defined in the figure. The calculation of the colorimetric *adapted* CIELAB data ($C^*_{ab,a}$, L^*) and h_{ab} is already given in Fig. A.1.

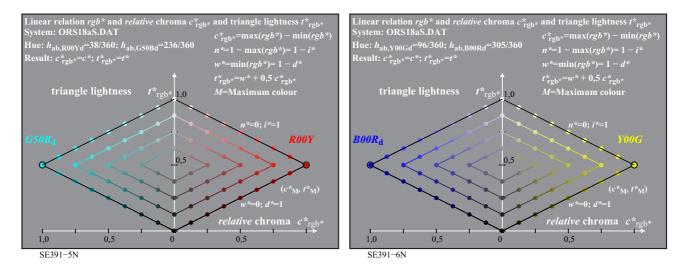


Fig. A.4— Colour samples of ORS18a of the hues R-C and Y-B in the relative CIELAB diagram (c*, t*)

Fig. A.4 shows the same samples as in Fig. A.1 to A.3. The colours of the hue planes R_d - C_d and Y_d - B_d are shown in the cylindrical relative CIELAB diagram (c^*_{rgb} , t^*_{rgb}). The coordinates relative chroma c^*_{rgb} and triangle lightness t^*_{rgb} are defined in the figure. The index *rgb* indicates that the calculation is done from the three *rgb* values and not from the CIELAB data.

The calculated the relative chroma c^* and the triangle lightness t^* which is calculated from the CIELAB data is identical to the relative chroma c^*_{rgb} and the triangle lightness t^*_{rgb} which is calculated from the *rgb*-input data for linearized output systems, for example according to ISO/IEC TR 19797:2004. For the hue angle here the CIELAB hue angle h_{ab} is given. However, the standard hue angles $h_{rgb} = 30$, 120 and 170 for red, green and blue and based on the *rgb* values are also possible. For the calculation of the hue angles h_{rgb} form the *rgb* data see DIN 33872-1.

Annex B

Standard and relative CIELAB data of the standard sRGB and offset device

Basic television colour or	chrom	aticity		ulus va				AB data <i>L</i>		
mixture colour for D65			(Y=100,	00 for wh	ite D65)	(L*=100,	00 for whit	e; L*=0,00		
CIE data for Y _W =100	xd	Уd	Xd	Yd	Zd	L*d	a*d	b*d	C*ab,d	hab,d
three additive mixture colours: t	elevision	colours a	cc. to ITU	J-R BT.7	09-3					
<i>C</i> _d cyan (cyan blue)	0,225	0,329	53,91	78,74	106.97	91,11	-48,08	-14,12	48,12	196
$M_{\rm d}$ magenta (magenta red)	0,321	0,154	59,29	28,48	96,99	60,32	98,23	-60,82	110,97	328
<i>Y</i> _d yellow	0,419	0,505	77,00	92,78	13,85	97,14	-21,56	94,48	93,07	103
three aditive basic colours: television colours acc. to ITU-R BT.709-3										
<i>R</i> _d red (orange red)	0,640	0,330	41,24	21,26	1,93	53,24	80,08	67,20	100,42	40
<i>G</i> ^d green (leaf green)	0,300	0,600	35,76	71,52	11,92	87,74	-86,18	83,18	115,04	136
$B_{\rm d}$ blue (violet blue)	0,150	0,060	18,05	7,22	95,05	32,30	79,19	-107,85	128,52	306
achromatic colours:										
W –	_	-	—	-	_	—	—	-	-	_
W1 (white monitor, 100%)	0,313	0,329	95,05	100,00	108,90	100,00	0,00	0,00	0,00	0
N (black monitor, 0,00%)	0,313	0,329	0,00	0,00	0,00	0,00	0,00	0,00	0,00	0
N0 -	-	-	-	_	_	_	_	_	_	_
	1	1	1 1			1	1	SI	E550-3	

Table B.1 — CIELAB data of 8 basic colours X = RYGCBM of the monitor TLS00 ($Y_N = 0$; $Y_W = 100$)

For the standard television monitor TLS00 with the lightness $L^* = 0$ for Black *N* and $L^*_W = 100$ for White W (see ISO/IEC 15775) table B.1 shows the CIE chromaticities *x* and *y*, and the CIE tristimulus values *X*, *Y*, and *Z*, and the standard CIELAB data $LAB^* = L^*$, a^* , b^* or $LCH^* = L^*$, C^*_{ab} , h_{ab} according to CIE 15. The chroma components a^*_N and b^*_N as well as a^*_W and b^*_W are all equal and zero. This is valid for the standard device.

Table B.2 shows the normalization to the lightness $L^*_W = 94,5$ for the White *W* of ORS18. Table B.1 shows the normalization $L^*_W = 100$ of White *W*. The normalization to $L^*_W = 94,5$ allows to compare the CIELAB data of White W for print and television colours and is equal to the normalization of ISO 9241-306 and ISO/IEC 15775. Part 1 of Table B.2 shows the lightness $L^*_N = 0$ for Black *N* for the standard television monitor TLS00. The Table B.1 includes the CIE chromaticities *x* and *y*, the CIE tristimulus values *X*, *Y*, and *Z*, and the CIELAB data $LAB^* = L^*$, a^* , b^* or $LCH^* = L^*$, C^*_{ab} , h_{ab} according to CIE 15. The chroma components a^*_N and b^*_N as well as a^*_W and b^*_W are all already equal to zero.

Part 1 of Table B.2 shows the lightness $L_N^* = 18$ for Black *N*. This standard lightness $L_N^* = 18$ may be produced by the luminance reflection of the room light on the monitor surface. Mate surfaces produce about 5% surface reflection, silk mate about 2,5%, and highly glossy about 1,5% for the 45/0 degree CIE measurement geometry. For the room illuminance *E*=500 lux according to ISO 8995 the luminance at the working area is 142 cd/m².

Table B.3 shows the standard and adapted CIELAB data for the standard offset system ORS18 according to ISO/IEC 15775. The tristimulus value of black N is Y=2,5 and for white W it is Y=88,6.

Many LCD monitors produce a luminance for white around 160 cd/m². If this display surface has the properties of a silky glossy surface then the reflection is around 2,5% and it may be valid Y=2,5 for the tristimulus value. For example in offices there are large differences of the luminance reflection and therefore ISO 9241-306 defines the standard reflection 2,5% and seven other reflections between 0% and 40% at work places. The last worst case appears for data projectors, and if the luminance reflection of the projector and the room light are approximately equal on the projection display.

Table B.2 — Standard and relative CIELAB data LAB* and lab* of television monitors TLS00	and TLS18

$\begin{array}{ c c c c c c c c c c c c c c c c c c c$		= standar	<i>adapted</i> = standard CIELAB data LAB^{*d} <i>relative</i> CIELAB data lab^{*d}	B data L	AB^*d	relative	CIEL	AB dat	a <i>lab*</i> d	_				
+2,5 xd yd Xd Xd Y lours: television colours acc. to ITU 0,228 0,329 48,71 1 red 0,321 0,162 53,43 2 1 1 $0,321$ 0,414 0,497 68,67 8 3		for white;	$(L^*=95, 4$ for white: $L^*=18, 01$ for black)	r black)		$(L^{*}=95, 4 \text{ for white: } L^{*}=18, 01 \text{ for black})$	for whii	$e; L^{*=I}$	8,01 for	black)				
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	1 L*d	а *d	$\mathbf{p}_* q$	$C^{*}_{ab,d}$	$h_{ab,d}$ r^*d	r*d	g^*d	$\mathbf{p}_{*}q$	<i>n</i> *	c^*	h^*	e*e	u*e	t^*
ed) $\begin{bmatrix} 0,228 & 0,329 & 48,71 \\ 0,321 & 0,162 & 53,43 \\ 0,414 & 0,497 & 68,67 \\ 0,414 & 0,497 & 68,67 \\ 1elevision colours acc. to ITU-RB \\ 0,600 & 0,330 & 37,89 \\ 0,161 & 0,581 & 33,18 \\ 0,161 & 0,079 & 17,93 \\ 0,1313 & 0,329 & 95,05 \\ 0,313 & 0,329 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,313 & 0,320 & 84,21 \\ 0,314 & 0,314 \\ 0$	-3													
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		-44,44	-13,14	46,32	196	0,00	1,00	1,00	0,00	1,00	0,546	0,578 0	331B	0,50
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		89,33	-55,69	105,26	328	1,00	0,00	1,00	0,00	1,00	0,911	0,875 E	350R	0,50
Sc. television colours acc. to ITU-RB 0,600 0,330 37,89 2 0,301 0,581 33,18 2 0,301 0,581 37,89 2 0,301 0,581 37,89 2 0,301 0,581 37,89 2 0,301 0,530 17,93 2 0,0161 0,079 17,93 2 0,0313 0,3229 95,05 10 0,0313 0,3229 84,21 1	4,67 92,74	-20,06	84,97	87,30	103	1,00	1,00	0,00	0,00	1,00	0,287	1,00 0,287 0,289 Y15G	715G	0,50
0,600 0,330 37,89 2 0,301 0,581 33,18 0 0,161 0,079 17,93 0 0,161 0,079 17,93 0 0,0313 0,329 95,05 10 0,0313 0,329 84,21 10						-						-		
0,301 0,581 33,18 0 0,161 0,079 17,93 0 0,313 0,329 95,05 10 0,313 0,329 84,21 8		71,63		87,29	35	1,00	0,00	0,00	0,00	1,00	0,097	0,036 F	(14Y	0,50
0,161 0,079 17,93 0,313 0,329 95,05 10 0,313 0,329 84,21 8	13,00 84,01	-79,02	73,94	108,20	137	0,00	1,00	0,00	0,00	1,00	0,380	0,411	764G	0,50
0,313 0,329 95,05 10 0,313 0,329 84,21 8		64,92		115,12	304	0,00	0,00	1,00	0,00	1,00	0,845	1,00 0,845 0,822 B28R	328R	0,50
0,313 0,329 95,05 10 0) 0,313 0,329 84,21 8														
0, 0,313 0,329 84,21 88,60 0,329 0	00,000 100,00	0,00	0,00	0,00	0	1,05		1,05	0,00	0,00	0,00	0,00		1,05
		0,00	0,00	0,00	0	1,00	1,00	1,00	0,00	0,00	0,00	0,00		1,00
	2,74 18,01	0,00	0,00	0,00	0	0,00		0,00	1,00	0,00	0,00	0,00		0,00
		0,00	0,00	0,00	0	-0,19	-0,19	-0,19	1,19	0,00	0,00	0,00		-0,19

Basic offset colour or	chrom	aticity	chromaticity tristimulus values	ulus val	ues	Standar	d CIEL	Standard CIELAB data LAB*	LAB*	
mixture colour for D65			(Y=88, 6)	(Y=88, 6 for white D65)		$(L^{*}=95,4)$	for white;	$(L^*=95, 4 for white; L^*-18, 01 for black)$	for black)	
ORS18 with <i>Y</i> _W =88,6	$\mathbf{p}_{\mathbf{X}}$	уд	$X_{\mathbf{d}}$ $Y_{\mathbf{d}}$	$Y_{\mathbf{d}}$	Ζd	P_*T	р <u>,</u> <i>р</i>	$\mathbf{p}_{*}q$	C*ab,d hab,d	hab,d
three subtractive basic colours: printing colours acc. to ISO 2846-1	printing o	colours ac	c. to ISO	2846-1						
Cd cyan (cyan blue)	0,165	0,165 0,234		26,62	68,54	18,74 26,62 68,54 58,62	-30,62 -42,74	-42,74	55,59	234
$M_{\rm d}$ magenta (magenta red) $0,459$ $0,235$	0,459	0,235	33,06	16,90	22,01	48,13	75,20	-6,79	75,51	355
Y _d yellow	0,441	0,441 0,500	68,06	77,10		90,37	-11,15	96,17	96,82	76
three subtractive mixture colours: # DIN 33866-colours, ISO reference paper	'S: # DIN	33866-co	lours; ISC	referenc	e paper					
$R_{\rm d}$ red (orange red)	0,608	0,608 0,338		30,13 16,75	2,28	2,28 47,94	65,31	52,07	83,53	39
Gd green (leaf green)	0,253	0,253 $0,556$	8,71	8,71 19,18	6,62	50,90	-62,96	36,71	72,89	150
B_{d} blue (violet blue)	0,216	0,216 0,140	7,17		21,41	25,72	31,45 -44,35	-44,35	54,38	305
achromatic colours: # calculated by linear chroma extrapolation in the CIELAB colour space	ed by lined	ar chrome	1 extrapolu	ation in th	he CIELA	B colour.	space			
<i>W1</i> (ideal white#, <i>D65</i>)	0,320	0,339	0,320 0,339 94,41 100,00 100,83 100,00	100,00	100,83	100,00	-1,07	5,06	5,17	0
W (ISO paper, $D65$)	0,320	0,320 0,339	83,68	83,68 88,60 89,47 95,41	89,47	95,41	-0.98	4,76	4,86	0
N (black printing colour)	0,312	0,325	2,42	2,52	2,81	18,01	0,50	-0,46	0,69	0
N0 (ideal black#, D65)	Ι	Ι	0,02	0,00	0,12	0,00	0,84	-1,68	1,89	0
								S	SE570-3	

Basic offset colour or mixture colour for D65	chrom	aticity	chromaticity tristimulus values $(Y = X + f_{or white DK})$	tristimulus values		adapted $\pi = 05 d$	adapted CIELAB data LAB [*] a,d (1 *=05 d for white 1 *=18 01 for black)	data <i>L</i> .	$\mathbf{1B}^{*}\mathbf{a},\mathbf{d}$		relative	relative CIELAB data <i>lab</i> *d /1 *=05 4 for white 1 *=18 01 for black)	AB dat $T_{P} \cdot I_{*} = I$	a <i>lab</i> *d	hlack)				
ORS18a with <i>Y</i> _W =88,6	xa,d	ya,d	$x_{a,d} \mid y_{a,d} \mid X_{a,d} \mid Y_{a,d} \mid$	Ya,d	-	<i>L</i> *a,d	<i>a</i> *a,d	<i>b</i> *a,d	b^* a,d C^* ab,a,d hab,a,d	<i>h</i> ab,a,d		g*d	P*d	<i>n*</i>	c*	* <i>u</i>	e*e	u*e	1*
three subtractive basic colours: printing colours acc. to ISO 2846-1	printing c	olours ac	c. to ISO	2846-1	1				-										
Cd cyan (cyan blue)	0,161	0,228	0,161 0,228 18,79	26,62		58,62	-30,34	-45,01	54,30	236	0,00	1,00	1,00	0,00	1,00 (0,656	0,669	G67B	
$M_{\rm d}$ magenta (magenta red) 0,454 0,232	0,454	0,232	33,08	16,90	22,90	48,13	75,28	-8,36	75,74	354	1,00	0,00	1,00	0,00	1,00 (0,982	0,931	B72R	0,50
Y _d yellow	0,439	0,439 0,494	68,47	68,47 77,10		90,37	-10,26	91,75	92,32	96	1,00	1,00	0,00	0,00	1,00 (0,268	0,264	0,268 0,264 Y05G	
three subtractive mixture colours: # DIN 33866-colours; ISO reference paper	s: # DIN .	33866-co	lours; ISC) referenc	e paper														
<i>R</i> _d red (orange red)	0,605	0,336	30,15	16,75	2,90	47,94	65,39	50,52	82,63	38	1,00	0,00	0,00		1,00 (0,105	0,047	R18Y	0,50
Gd green (leaf green)	0,249	0,548	8,72	19,18	7,07	50,90	-62,83	34,96	71,91	151	0,00	1,00	0,00	0,00	1,00 (0,419	0,461	Y84G	0,50
B_{d} blue (violet blue)	0,215	0,140	0,215 0,140 7,14 4,65	4,65	21,44	25,72	31,10	-44,40	54,22	305	0,00	0,00	1,00		1,00 0,847 0,822 B28R	0,847	0,822	B28R	0,50
achromatic colours: #calculated by linear chroma extrapolation in the CIELAB colour space	ed by linec	ur chroma	ı extrapolı	ation in th	ie CIELA	B colour s	pace												
W1 (ideal white#, D65)	0,313	0,329	0,313 0,329 95,05 100,00 108,92 100,00	100,00	108,92	100,00	0,00	0,00	0,00	0	1,05	1,05	1,05	0,00	0,00	0,00	0,00		1,05
W (ISO paper, $D65$)	0,313	0,313 0,329	84,21	88,60	96,48	95,41	0,00	0,00	0,00	0	1,00	1,00	1,00	0,00	0,00	0,00	0,00		1,00
N (black printing colour)	0,313 0,329		2,40	2,52	2,74	18,01	0,00	0,00	0,00	0		0,00	0,00	1,00	0,00	0,00	0,00		0,00
N0 (ideal black#, D65)	Ι	I	0,00 0,00 0,00	0,00	0,00	0,00	0,00	0,00	0,00	0	-0,19	-0,19	-0,19		0,00	0,00	0,00	I	-0,19
																		SE570-7	

Table B.3 — *Standard* and *relative* CIELAB data *LAB** and *lab** of offset ORS18 according to ISO/IEC 15775

C.1 Terms and definitions of special colorimetric data

In addition to the terms and the definitions of clause 3.1 Colorimetric data the maximum colours M of maximum chroma C^*_{ab} of a standard 48 step hue circle and their mixtures are defined. The families of the different colorimetric data of clause 3.1 are now given in Table C.1 and subdivided in Table C.2.

C.1.2

Colorimetric data of maximum colours *M* of a device system

Three colour data of a 48 step hue circle including the colorimetric linear mixture colours of two neighboring colours C.

NOTE 1: In the standard CIELAB-chroma diagram (a^*, b^*) and in the *adapted* CIELAB-chroma diagram (a^*_a, b^*_a) the maximum colours *M* create a closed figure by the 48 steps, and in the *relative* CIELAB-chroma diagram (a^*_r, b^*_r) a circle

NOTE 2: For many applications the adapted maximum colours M_a of a 256 step hue circle (8bit) are appropriate for fast colorimetric transfers. Such a table for 360 CIELAB hue angles h_{ab} usually includes the corresponding *rgb*-input data, the CIELAB *L**, *a**, *b**, *C**_{ab}, h_{ab} data and other data for fast transformations between device o device coordinates *rgb*_{dd} and device to elementary coordinates *rgb*_{de}.

C.2 Colorimetric data of Maximum colours *M* in table form

Table C.1 — Examples of colorimetric data of maximal colours *M* of a device system

Colorimetri	c data of	maximum colour	s M of a device (d) or	r elementary (e) system	
colori- metric name	family	family member	coordinate kind	coordinate (compare CIELAB <i>L*, C*</i> _{ab} , <i>h</i> _{ab} , <i>a*, b*</i>)	coordinate name
standard CIELAB adapted CIELAB (a)	LAB*	$LAB*LCH^*_{M}$ or $LAB*LAB^*_{M}$ $LAB*LAB^*_{M}$ or	cylindrical or kartesic cylindrical or	$L_{M}^{*} = LAB^{*}L_{M}^{*}$ $C_{M}^{*} = LAB^{*}C_{ab,M}^{*}$ $H_{M}^{*} = LAB^{*}h_{ab,M}$ $A_{M}^{*} = LAB^{*}a_{M}^{*}$ $B_{M}^{*} = LAB^{*}b_{M}^{*}$ $L_{a,M}^{*} = LAB^{*}L_{a,M}^{*}$ $C_{*}^{*} = LAB^{*}C^{*}$	lightness chroma hue angle red green chroma yellow blue chroma adapted lightness (= L_{M}^{*})
		LAB*LAB*	kartesic	$C_{a,M}^* = LAB_a^*C_{a,M}^*$ $H_{a,M}^* = LAB_a^*H_{a,M}^*$	adapted chroma adapted hue angle $(0 \le H^*_{a,M} \le 360)$
relative CIELAB (r)	lab*	<i>lab*lch</i> [*] _M or <i>lab*lab</i> [*] _M	cylindrical or kartesic	$l_{M}^{*} = lab*l_{M}^{*}$ $c_{M}^{*} = lab*c_{M}^{*}$ $h_{M}^{*} = lab*h_{M}^{*}$	relative lightness relative chroma relative hue $(0,00 \le h_{M}^{*} \le 1,00)$

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Colorimetri	c standar	d CIELAB data	and linearly related <i>a</i>	<i>dapted</i> and <i>relative</i> CII	ELAB data
colori- metric name	family	family member	coordinate kind	coordinate (compare CIELAB $L^*, C^*_{ab}, h_{ab}, a^*, b^*$)	coordinate name
standard	LAB*	LAB*LCH*	cylindrical	$L^* = LAB^*L^*$	lightness
CIELAB		or	or	$C^* = LAB^*C^*_{ab}$	chroma
		LAB*LAB*	kartesic	$H^* = LAB * h_{ab}$	hue angle
				$A^* = LAB^*a^*$	red green chroma
				$B^* = LAB^*b^*$	yellow blue chroma
adapted	LAB* a	LAB*LCH*	cylindrical	$L_{a}^{*} = LAB_{a}^{*}L_{a}^{*}$	adapted lightness (= L^*)
CIELAB (a)		or LAB*LAB*	or kartesic	$C_{a}^{*} = LAB_{a}^{*}C_{a}^{*}$	adapted chroma
		LAD aLAD a	Kartesie	$H_{a}^{*} = LAB_{a}^{*}H_{a}^{*}$	adapted hue angle $(0 \le H_a^* \le 360)$
relative	lab*	lab*lch*	cylindrical	$l^* = lab^*l^*$	relative lightness
CIELAB (r)		or		$c^* = lab^*c^*$	relative chroma
		lab*lab* or	kartesic	$h^* = lab^*h^*$	relative hue
		lab*tch*	cylindrical	$a_r^* = lab^*a_r^*$	relative a-red green chroma
		or	1	$b_r^* = lab^*b_r^*$	relative b-yellow blue chroma
		lab*tab*	kartesic	$t^* = lab^*t^*$	relative triangle lightness
		lab*nch*	triangle-cylindrical	$n^* = lab^*n^*$	relative blackness
		or <i>lab*nce*</i>	triangle-cylindrical	$c^* = lab^*c^*$	relative chroma
		or	u langie-cynnuncai	$h^* = lab^*h^*$	relative hue
		lab*ncu*	triangle-cylindrical	$e^* = lab^*e^*$	relative elementary hue text
		or <i>lab*tce*</i>	cylindrical	$u^* = lab^*u^*$	relative elementary hue
		or	cymuncar	$r^* = lab^*r^*$	relative r-red green chroma
		lab*try*	kartesic	$y^* = lab^*y^*$	relative j-yellow blue chroma
				$t^* = lab^*t^*$	relative triangle lightness
		lab*rgb*d	kartesic	$r_{\rm d}^* = lab * r_{\rm d}^*$	relative device red
				$g_{d}^{*} = lab_{g_{d}}^{*}$	relative device green
				$b*_{\rm d} = lab*b*_{\rm d}$	relative device blue
		lab*cmy*d	kartesic	$c_{d}^{*} = lab * c_{d}^{*}$	relative device cyan
				$m_{\rm d}^* = lab m_{\rm d}^*$	relative device magenta
				$y_{d}^{*} = lab^{*}y_{d}^{*}$	relative device yellow
		lab*rgb*e	kartesic	$r_{\rm e}^* = lab*r_{\rm e}^*$	relative elementary red
				$g_{e}^{*} = lab^{*}g_{e}^{*}$	relative elementary green
				$b*_{\rm e} = lab*b*_{\rm e}$	relative elementary blue
		lab*cmy _e	kartesic	$c_{e}^{*} = lab*c_{e}^{*}$	relative elementary cyan
				$m_{e}^{*} = lab * m_{e}^{*}$	relative elementary magenta
				$y_{e}^{*} = lab_{y_{e}^{*}}^{*}$	relative elementary yellow

Table C.2 — Examples of colorimetric data and linear relationship

Annex D Automatic colour measurement of output colours on displays

The standard test chart *G* with 1080 colours in Fig. 17 on page 21 needs to be measured automatically within less then one hour. For printer output this is possible with an *xy*-colour measuring equipment, for example of the companies *Gretag Macbeth or XRite*. In the paper case the output of the test chart *G* with 1080 colours on standard paper is used. For display output the following two *PDF* files produce 57 and 1080 colour pages for the display measurement. A file for the output of 48 hue steps and 9 grey steps produces the following output page no. 1

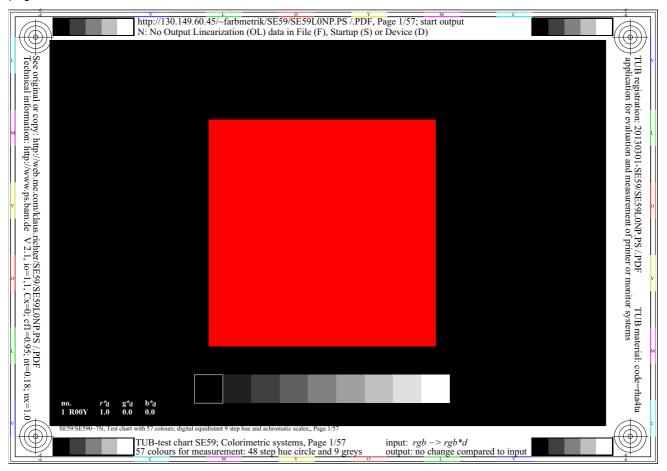


Fig D.1 — Display output for colour measurement of a 48 step hue circle and 9 grey steps

Fig. D.1 shows the first page of the display output for colour measurement of a 48 step hue circle and the 9 grey steps. A continuous number between 1 and 57, and for example the device hue text u_d^* (= $R00Y_d$ = o00y), and the *rgb*-input data (= 1 0 0)_d are given (bottom left). For the 57 colours see the following URL (57 pages, 60 KB):

http://130.149.60.45/~farbmetrik/SE59/SE59L0NP.PDF

For the 1080 standard colours see the following URL (1080 pages, 1,8 MB): http://130.149.60.45/~farbmetrik/SE60/SE60L0NP.PDF

Both files are useful for the separate measurement of colours and if no automatic measurement is available.

For automatic measurement the 1080 colours are produced one by one and measured. A computer program has been developed for the computer operating system *Windows (installed on a Macintosh computer)* by *J.*

Witt for the *high precision colorimeter C1210* of the company *LMT Lichtmesstechnik (Berlin)* at the *Federal Institute for Material Research and Testing (BAM, Berlin).*

Note: The computer program menu is in German, for example *Starte Messprogramm* is used instead of *start measurement program*.

LMT Colormeter C 1210 Gerätes	steuerung 🗆 🗆 🖾	3		
0.000 0.00	00 0.000			
0.333	0.333	Form3		
	0.555			
Gerätestatus:				
Mode:	Bereich:			
Status:	Eingabezustand:			
Fehlercode:	Kalibrierfaktor:			
Format:	Warnung:			
Gerätesteuerung: serielle Schnittste	elle:			
COM1 💽	Messintervall x (ms): 4000 Stufenzahl: 9	-		
Befehlsübersicht: Gerätemodus:	Messprogramme:			
Messwertspeicherung: Dezimaltrennzeichen:	, Dateilname: LMT.log			
Beende Messprogramm Abbr	rechen RGB			
1000 0000 0000 %orange red 0 0000 1000 0000 %leaf green L 0000 0000 1000 %violett blue V		·		
		-		
Error:0 Zeichen #1 0) bytes gelesei () bytes waiting	<i>///</i>		

Fig. D.2 — Automatic colour measurement of 1080 standard colours with a colorimeter

Fig. D.2 shows an example output for the automatic colour measurement of 57 or 1080 standard colours with a colorimeter. The colour measurement produces the CIE chromaticity coordinates x, y and the illuminance E in lux (proportional to the tristimulus value Y). It takes about 5s for one colour measurement and therefore it takes about 1,5 hours to measure the 1080 standard colours of Fig. 17 on page 21 (Test chart Grid G).

The program menu allows to measure for example 9x9x9 steps automatically (as indicated by the number 9). If by the technology *copy and paste* the *rgb*-input data (for example 57, or 1080 data) are included in the rectangle at the bottom, then this *rgb*-input data are used to produce and measure the colours in the right window. In the example the device colour R_d (Orange red O) with the *rgb*-input data sequence 1000 0000 0000%Red R_d (Orange red O) is measured.

If an external data projector, for example a VGA device, is connected to the computer, then the colours in the projection can be measured.

The measurement data of for example 1080 colours appear in a file *LMT.log*. These data are included for example in lines 672 to 1753 of the *PS* file (download the *PostScript* file with ".TXT" instead of ".PS")

http://130.149.60.45/~farbmetrik/SE61/SE61L0NP.PDF

The output pages 1 and 2 of the corresponding *PDF* file shows the *rgb*-input data (slightly changed by the 8bit *rgb*-input coding which are necessary for output on most displays). In addition the CIE chromaticities *x*, *y* and

The eight last colours in Fig. 17 on page 21 are the achromatic colours Black *N* (no. 1073) and White *W* (no. 1074) and the six colours $RCYBGM_d$ produced for the input values $(1 \ 0 \ 0)_d$, $(0 \ 1 \ 1)_d$, $(1 \ 1 \ 0)_d$, $(0 \ 0 \ 1)_d$, $(0 \ 1 \ 0)_d$, $(1 \ 0 \ 1)_d$, $(0 \ 0 \ 1)_d$, $(0 \ 1 \ 0)_d$, $(0 \ 0 \ 1)_d$, $(0 \ 0 \ 1)_d$, $(0 \ 0 \ 0)_d$, $(0 \ 1 \ 0)_d$, $(0 \ 0 \ 0)_$

On page 1 and 2 the *rgb*-input data and the measured *x*, *y*, Y_m (measured in lux) data are shown. On page 3 and 4 the *rgb*-input data and the measured *x*, *y*, Y_n data are shown. The tristimulus value Y_n is normalized to 100 for white W (colour no. 1074).

In a similar file the CIE XYZ and $L^*C^*_{ab}h_{ab}$ are calculated (4 pages, 225 KB)

http://130.149.60.45/~farbmetrik/SE62/SE62L0NP.PDF

The pages 1 and 2 of the file output show the CIE data with the standard normalization Y=88,6. The output of the pages 3 and 4 show the data $rgb'^*=rgb_{dd}$ which are necessary to produce the intended CIE data $(L^*C^*_{ab}h_{ab})_{d}$. These data have been calculated by the 3D output linearization method.