

## Weber-Fechner law in CIE 230:2019 for threshold colour differences of surface colours

The Weber-Fechner law describes the lightness  $L^*$ , as *logarithmic* function of  $L_r$ .  
 For local adaptation to *Adjacent* colours there is a *visible contrast* 100:1.

The Stevens law describes the lightness  $L^*_{\text{CIELAB}}$  as *potential* function of  $L_r = Y/5$ .  
 IEC 61966-2-1 uses a similar potential function  $L^*_{\text{IEC}} = m L_r^{1/2,4}$ .

For *separate* colours on a grey surround there is a *visible contrast* 25:1=90:3,6.  
*see K. Richter, 2006, Relation of Weber and Stevens law at achromatic threshold.*  
<http://farbe.tu-berlin.de/A/BAMAT.PDF>

Table 1: CIE tristimulus value  $Y$ , luminance  $L$ , and lightnesses  $L^*$

Colour (matte)	Tritimulus value	office luminance	relative luminance	CIE lightness	relative lightness
(contrast) (25:1=90:3,6)	$Y$	$L$ [cd/m <sup>2</sup> ]	$L_r$ $=L/L_Z$	$L^*_{\text{CIELAB}}$ $\sim m L_r^{1/2,4}$	$L^*_r$ $=k \log(L_r)$
White W (paper)	90 $=18*5$	142 $=28,2*5$	5	94 $=50+44$	40 $=k \log(5)$
Grey Z (paper)	18	28,2	1	50	0 $=k \log(1)$
Black N (paper)	3,6 $=18/5$	5,6 $=28,2/5$	0,2	18 $=50-32$	-40 $=k \log(0,2)$

For the lightness range between  $L^*_r = -40$  and 40 the constant is:  $k = 40/\log(5) = 57$