

LABJND modifications of the colour space and the colour-difference formula by line elements for different applications

Example line element in lightness direction of *Stiles* (1946), who uses the luminance L instead of the tristimulus value Y .

$$L^*(Y) = s \ln[1+9Y] \quad s=\text{scaling factor} \quad [1a]$$

$$d(L^*(Y)) / dY = 9s / [1+9Y] \quad [2a]$$

For this derivation, and for the lightness threshold $d(L^*(Y))=1$ it is valid:

$$dY = [1+9Y] / 9s \quad [3a]$$

For the normalization with the surround values $Y_u=18$, dY_u and $L^*(Y_u)$:

$$dY/dY_u = [1+9Y] / [1+9Y_u] \quad [4a]$$

$$L^*(Y) / L^*(Y_u) = \ln[1+9Y] / \ln[1+9Y_u] \quad [5a]$$

For the LABJND colour-difference formula according to CIE 230:2019:

$$dY/dY_u = [A_1+A_2Y] / [A_1+A_2Y_u] \quad A_1=0,0170, A_2=0,0058 \quad [1b]$$

It is valid with the definition $A_{2u}=A_2Y_u/A_1=6,141$

$$dY/dY_u = [1+A_{2u}(Y/Y_u)] / [1+A_{2u}] \quad [2b]$$

$$L^*(Y) / L^*(Y_u) = \ln[1+A_{2u}(Y/Y_u)] / \ln[1+A_{2u}] \quad [3b]$$

Line elements for the LABJND-colour space are NOT included in CIE 230. The value of A_{2u} is known for many applications, for example as function of the distance, the presentation time and the luminance of the samples.