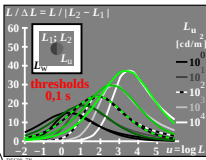
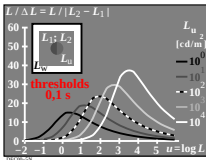
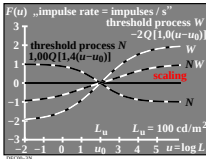


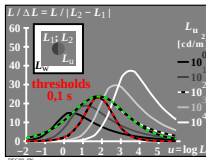
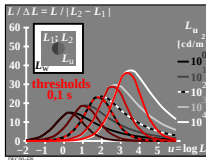
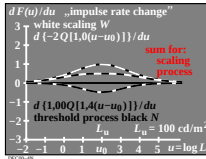
http://farbe.li.tu-berlin.de/DECO/DECOL0N1.TXT /PS; only vector graphic VG; start output
N: no 3D-linearization (OL) in file (F) or PS-startup (S)

Weber-Fechner law in CIE 200-2013 for threshold colour difference of surface colours
The Weber-Fechner law describes the lightness L^* as logarithmic function of L . The Stevens law describes the lightness L^* as potential function of L .
BIE 1992-2001 uses a similar potential function $L^*_{90} = a + b \cdot L^a$.
The Weber-Fechner law is equivalent to the equation: $\Delta L^* = c \cdot L$.
Integration leads to the logarithmic equation: $L^* = 4.5 \log(L)$.
Differentiation leads for $\Delta L^* = 1$ leads to the linear equation: $L = 10 \cdot \Delta L^* - 57$.
For the values of the standard contrast range is 25-90-135.
Table 1: CIE estimations value L^* , luminance L and lightness L^* .

Colour (name)	Tristimulus value	Relative luminance	CIE lightness	Relative lightness
(contrast)	L	L_c	L^*	L^*_c
(25-100-34)	L_c	L_c	L^*_c	L^*_c
White W	100	1.0	100	1.0
Black B	0.0001	0.0001	0.0001	0.0001
Grey Z (neutral)	18	0.018	18	0.018
Black N	0.0	0.0	0.0	0.0
White N	100	1.0	100	1.0



Weber-Fechner law in CIE 200-2013 for threshold colour difference of surface colours and two ranges $0.2 \leq L_c \leq 1$ and $1 \leq L_c \leq 10$.
The Weber-Fechner law describes the lightness L^* as logarithmic function of L . The Stevens law describes the lightness L^* as potential function of L .
BIE 1992-2001 uses a similar potential function $L^*_{90} = a + b \cdot L^a$.
The Weber-Fechner law is equivalent to the linear equation: $\Delta L^* = c \cdot L$.
Integration leads to the logarithmic equation: $L^* = 4.5 \log(L)$.
Differentiation leads for $\Delta L^* = 1$ leads to the linear equation: $L = 10 \cdot \Delta L^* - 57$.
For the values of the standard contrast range is 25-90-135.
Table 1: CIE estimations value L^* , luminance L and lightness L^* .



line element of Stiles (1946) with „color values“ L_p, M_D, S_T
three separate color signal functions
 $F(L_p) = i \ln(1 + 9 L_p)$
 $F(M_D) = j \ln(1 + 9 M_D)$
 $F(S_T) = k \ln(1 + 9 S_T)$
Taylor-derivations:
 $\Delta F(L_p, M_D, S_T) = \frac{dF}{dL_p} \Delta L_p + \frac{dF}{dM_D} \Delta M_D + \frac{dF}{dS_T} \Delta S_T$
 $= \frac{9i}{1+9L_p} \Delta L_p + \frac{9j}{1+9M_D} \Delta M_D + \frac{9k}{1+9S_T} \Delta S_T$

functions $q[k(u-u_0)]$
„achromatic signal“-description
with $u = \log L$ (L = luminance)
 $u_0 = \log L_u$ (L_u = surround luminance)
 $q[k(u-u_0)] = 1 + 1/(1 + \sqrt{2} e^{k(u-u_0)})$
function values:
 $q[k(u-u_0) \rightarrow +\infty] = 1$
 $q[k(u-u_0) = 0] = \sqrt{2}$
 $q[k(u-u_0) \rightarrow -\infty] = 2$

„achromatic signal“ discrimination as function of relative light density
 $h = \ln H = k(u-u_0)$, $\ln =$ natural log.
 $Q' = \frac{d}{dH} \{ \ln(1 + 1/(1 + \sqrt{2} H)) \} / \ln \sqrt{2}$
 $= -\sqrt{2} / (\ln \sqrt{2} (1 + \sqrt{2} H) (2 + \sqrt{2} H))$
function values:
 $Q'[k(u-u_0) \rightarrow +\infty] = 0$
 $Q'[k(u-u_0) = 0] = -0,5$
 $Q'[k(u-u_0) \rightarrow -\infty] = 0$

double line element of Richter (1987) for the lighting technology with the luminance $L = F(L_p, M_D, S_T)$
 $F(L) = \int_{-\infty}^L (L/\Delta L) dL$ (relative L, M, S)
 $F(L) = i Q(H) = \int_{-\infty}^L Q(H) dH$ ($u < u_0$)
 $F(L) = i Q(H) = \int_{-\infty}^L Q(H) dH$ ($u \geq u_0$)
with: $k=1, 4$ $k=1$ $i=1$ $i=2$
 $u = \log L$ $u_0 = \log L_u$ $u = \log L$
 $H = e^{k(u-u_0)}$ $H = e^{k(u-u_0)}$ $H = e^{k(u-u_0)}$

line element of Vos&Walraven (1972) with „color values“ L_p, M_D, S_T
three separate color signal functions
 $F(L_p) = 2i \sqrt{L_p}$
 $F(M_D) = 2j \sqrt{M_D}$
 $F(S_T) = 2k \sqrt{S_T}$
Taylor-derivations:
 $\Delta F(L_p, M_D, S_T) = \frac{dF}{dL_p} \Delta L_p + \frac{dF}{dM_D} \Delta M_D + \frac{dF}{dS_T} \Delta S_T$
 $\Delta F(L_p, M_D, S_T) = \frac{i}{\sqrt{L_p}} \Delta L_p + \frac{j}{\sqrt{M_D}} \Delta M_D + \frac{k}{\sqrt{S_T}} \Delta S_T$

„achromatic signal“-description functions $Q_{lm}[k(u-u_0)]$
with $u = \log L$ (L = luminance)
 $u_0 = \log L_u$ (L_u = surround luminance)
 $Q_{lm}[k(u-u_0)] = \frac{1}{\ln \sqrt{2}} \ln q[k(u-u_0)] - m$
function values with $l = m = 1$:
 $Q[k(u-u_0) \rightarrow +\infty] = -1$
 $Q[k(u-u_0) = 0] = 0$
 $Q[k(u-u_0) \rightarrow -\infty] = 1$

luminance discrimination possibility $L/\Delta L$ as function of H
with: $L = 10^u$ $H = e^{\frac{1}{\ln 10} \log e k(u-u_0)}$
 $dL/dH = \ln 10 L$ $dH/dH = k H$
it follows: $L/\Delta L = [k H / (dH \ln 10)]$
 $\frac{L}{\Delta L} = \text{const } H / ((1 + \sqrt{2} H) (2 + \sqrt{2} H))$
 $Q'[k(u-u_0) \rightarrow +\infty] = 0$
 $Q'[k(u-u_0) = 0] = \text{maximum}$
 $Q'[k(u-u_0) \rightarrow -\infty] = 0$

double line element of Richter (1987) for the lighting technology with the luminance $L = F(L_p, M_D, S_T)$
 $F(L) = \int_{-\infty}^L (L/\Delta L) dL$ (relative L, M, S)
 $F(L) = i Q(H) = \int_{-\infty}^L Q(H) dH$ ($u < u_0$)
 $F(L) = i Q(H) = \int_{-\infty}^L Q(H) dH$ ($u \geq u_0$)
with: $k=1, 4$ $k=1$ $i=1$ $i=2$
 $u = \log L$ $u_0 = \log L_u$ $u = \log L$
 $H = e^{k(u-u_0)}$ $H = e^{k(u-u_0)}$ $H = e^{k(u-u_0)}$

TUB-test chart DECO; Thresholds, contrast ($L/\Delta L$), and lightness L^* input: rgb/cmy0/000k/n
Line element, contrast, and lightness according to Weber-Fechner, Stiles, and Vos&Walraven