http://farbe.li.tu-berlin.de/AET0/AET0L0NP.PDF /.PS; only vector graphic VG; start output
N: no 3D-linearization (OL) in file (F) or PS-startup (S)

see similar files: http://farbe.li.tu-berlin.de/AET0/AET0.HTM
technical information: http://farbe.li.tu-berlin.de or http://130.149.60.45/~farbmetrik

Weber-Fechner law in CIE 230:2019 for threshold colour differences of surface colours

The *Weber-Fechner* law describes the lightness L^*_r as ***logarithmic*** function of L_r.
The *Stevens* law describes the lightness L^*_{CIELAB} as ***potential*** function of $L_r=Y/5$.
IEC 61966-2-1 uses a similar potential function $L^*_{IEC} = m\,L_r^{1/2,4}$.
The *Weber-Fechner* law is equivalent to the equation: $\Delta L_r = c\,L_r$ [1]
Integration leads to the logarithmic equation: $L^*_r=k\log(L_r)$. [2]
Derivation for $\Delta L^*_r=1$ leads to the linear equation: $L_r/\Delta L_r=k=57$. [3]
For colours in offices the **standard contrast range** is **25:1**=90:3,6.

Table 1: CIE tristimulus value *Y*, luminance *L*, and lightnesses *L**

Colour (matte)	Tritimulus value	office luminance	relative luminance	CIE lightness	relative lightness
(contrast) (25:1=90:3,6)	Y	L [cd/m²]	L_r $=L/L_u$	L^*_{CIELAB} $\sim m\,L_r^{1/2,4}$	L^*_r $=k\log(L_r)$
White W (paper)	90 =18*5	142 =28,2*5	5	94 =50+44	40 $=k\log(5)$
Grey Z (paper)	18	28,2	1	50	0 $=k\log(1)$
Black N (paper)	3,6 =18/5	5,6 28,2/5	0,2	18 50−32	−40 $=k\log(0,2)$

For the lightness range between $L^*_r=-40$ and 40 the constant is: $k=40/\log(5)=57$

AET00−1N

Weber-Fechner law in CIE 230:2019 for threshold colour differences of surface colours and two ranges 0,2 <= L_r <=1 and 1 <= L_r <=5

The *Weber-Fechner* law describes the lightness L^*_r as ***logarithmic*** function of L_r.
The *Stevens* law describes the lightness L^*_{CIELAB} as ***potential*** function of $L_r=Y/5$.
IEC 61966-2-1 uses a similar potential function $L^*_{IEC} = m\,L_r^{1/2,4}$.
The *Weber-Fechner* law is equivalent to the linear equation: $\Delta L_r=c_i L_r$ $(i=0,1)$ [1]
Integration leads to the logarithmic equation: $L^*_r=k_i\log(L_r)$ $(i=0,1)$ [2]
Derivation leads for $\Delta L^*_r=1$ to the linear equation: $L_r/\Delta L_r=k_i$ ($k_0=46$, $k_1=63$) [3]
For colours in offices the **standard contrast range** is **25:1**=90:3,6.

Table 1: CIE tristimulus value *Y*, luminance *L*, and lightnesses *L**

Colour (matte)	Tritimulus value	office luminance	relative luminance	CIE lightness	relative lightness
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White W (paper)	90 =18*5	142 =28,2*5	5	94 =50+44	44 $=k_1\log(5)$
Grey Z (paper)	18	28,2	1	50	0 $=k_0\log(1)$
Black N (paper)	3,6 =18/5	5,6 28,2/5	0,2	18 50−32	−32 $=k_0\log(0,2)$

For the two lightness ranges it is $k_0=-32/\log(0,2)=46$ and $k_1=44/\log(5)=63$.

AET00−2N

line element of *Stiles* (1946) with „color values" L_P, M_D, S_T

three separate color signal functions

$$F(L_P)=i\ln(1+9L_P)$$
$$F(M_D)=j\ln(1+9M_D)$$
$$F(S_T)=k\ln(1+9S_T)$$

***Taylor*-derivations:**

$$\Delta F(L_P,M_D,S_T)=\frac{dF}{dL_P}\Delta L_P+\frac{dF}{dM_D}\Delta M_D+\frac{dF}{dS_T}\Delta S_T$$
$$=\frac{9i}{1+9L_P}\Delta L_P+\frac{9j}{1+9M_D}\Delta M_D+\frac{9k}{1+9S_T}\Delta S_T$$

AET01−1N

line element of *Vos&Walraven* (1972) with „color values" L_P, M_D, S_T

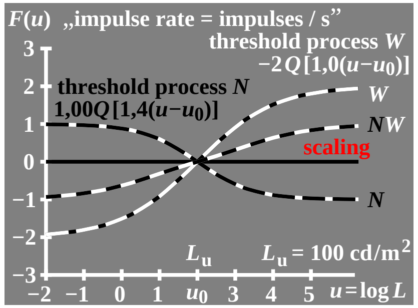
three separate color signal functions

$$F(L_P)=-2i\sqrt{L_P}$$
$$F(M_D)=-2j\sqrt{M_D}$$
$$F(S_T)=-2k\sqrt{S_T}$$

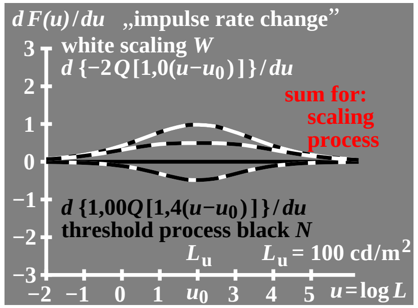
***Taylor*-derivations:**

$$\Delta F(L_P,M_D,S_T)=\frac{dF}{dL_P}\Delta L_P+\frac{dF}{dM_D}\Delta M_D+\frac{dF}{dS_T}\Delta S_T$$
$$\Delta F(L_P,M_D,S_T)=\frac{i}{\sqrt{L_P}}\Delta L_P+\frac{j}{\sqrt{M_D}}\Delta M_D+\frac{k}{\sqrt{S_T}}\Delta S_T$$

AET01−2N



AET00−3N



AET00−4N

functions $q[k(u-u_0)]$ „achromatic signal"-description

with $u=\log L$ (L = luminance)
$u_0=\log L_u$ (L_u = surround luminance)

$$q[k(u-u_0)]=1+1/[1+\sqrt{2}\,e^{k(u-u_0)}]$$

function values:

$q[k(u-u_0)\to+\infty]$ = 1
$q[k(u-u_0)=0]$ = $\sqrt{2}$
$q[k(u-u_0)\to-\infty]$ = 2

AET01−3N

„achromatic signal"-description functions $Q_{lm}[k(u-u_0)]$

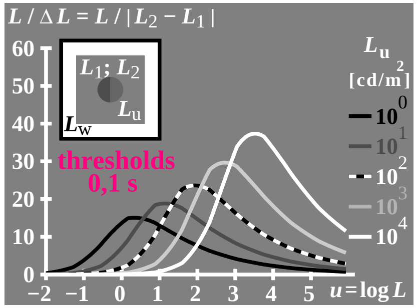
with $u=\log L$ (L = luminance)
$u_0=\log L_u$ (L_u = surround luminance)

$$Q_{lm}[k(u-u_0)]=\frac{l}{\ln\sqrt{2}}\ln q[k(u-u_0)]-m$$

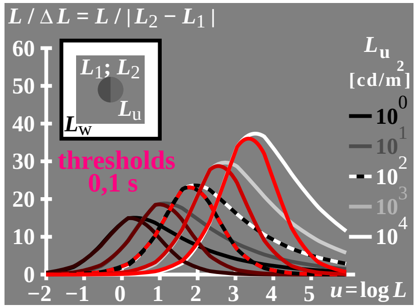
function values with $l = m = 1$:

$Q[k(u-u_0)\to+\infty]$ = 1
$Q[k(u-u_0)=0]$ = 0
$Q[k(u-u_0)\to-\infty]$ = −1

AET01−4N



AET00−5N



AET00−6N

„achromatic signal" discrimination as function of relative light density $h=\ln H=k(u-u_0)$, ln = natural log.

$$Q'=\frac{d}{dH}[\ln\{1+1/(1+\sqrt{2}H)\}]/\ln\sqrt{2}$$
$$=-\sqrt{2}/[\ln\sqrt{2}\,(1+\sqrt{2}H)(2+\sqrt{2}H)]$$

function values:

$Q'[k(u-u_0)\to+\infty]$ = 0
$Q'[k(u-u_0)=0]$ = −0,5
$Q'[k(u-u_0)\to-\infty]$ = 0

AET01−5N

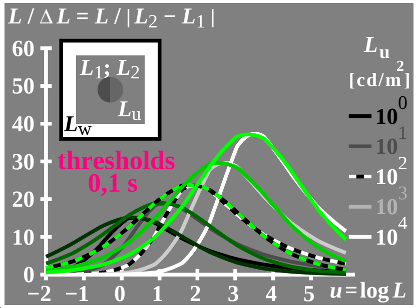
luminance discrimination possibility $L/\Delta L$ as function of H

with: $L=10^u$ $H=e^h=10^{\log e\,k(u-u_0)}$
$dL/du=\ln 10\,L$ $dH/du=kH$

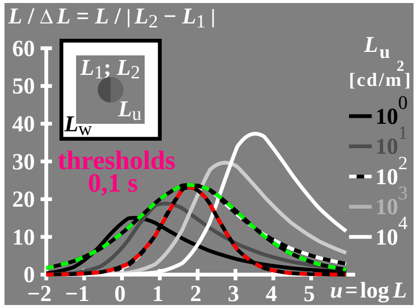
it follows: $L/\Delta L=[kH/(dH\ln 10)]$
$\frac{L}{dL}$ = const $H/[(1+\sqrt{2}H)(2+\sqrt{2}H)]$

$Q'[k(u-u_0)\to+\infty]$ = 0
$Q'[k(u-u_0)=0]$ = maximum
$Q'[k(u-u_0)\to-\infty]$ = 0

AET01−6N



AET00−7N



AET00−8N

double line element of *Richter* (1987) for the lighting technology with the luminance $L=f(L_P,M_D,S_T)$

$F(L)=\int_{-\infty}^{L}(L/\Delta L)\,dL$ (relative lightness?)

$$F(L)=iQ(H)=\begin{cases}\underline{i}\,Q(\underline{H}) & (u<u_0)\\ \bar{i}\,Q(\bar{H}) & (u\ge u_0)\end{cases}$$

with: $\underline{k}=1,4$ $\bar{k}=1$ $\underline{i}=1$ $\bar{i}=-2$
$u=\log L$ $u_0=\log L_u$
$H=e^{k(u-u_0)}$, $\underline{H}=e^{\underline{k}(u-u_0)}$, $\bar{H}=e^{\bar{k}(u-u_0)}$

AET01−7N

double line element of *Richter* (1987) for the lighting technology with the luminance $L=F(L_P,M_D,S_T)$

$F(L)=\int_{-\infty}^{L}(L/\Delta L)\,dL$ (relative lightness?)
$F(L)=iQ(H)$ $H=e^{k(u-u_0)}$
$Q(H)=[\ln\{1+1/(1+\sqrt{2}H)\}]/\ln\sqrt{2}-1$

Taylor-derivations:

$$\Delta F(L)=\frac{dF}{dL}\Delta L=i\,\frac{dQ}{dH}\Delta H$$
$$=-i\sqrt{2}\Delta H/[\ln\sqrt{2}\,(1+\sqrt{2}H)(2+\sqrt{2}H)]$$

AET01−8N

TUB registration: 20201101-AET0/AET0L0NP.PDF /.PS
application for evaluation and measurement of display or print output

TUB material: code=rha4ta

TUB-test chart AET0; Thresholds, contrast $(L/\Delta L)$, and lightness L^* input: *rgb/cmy0/000k/n*
Line element, contrast, and lightness according to *Weber-Fechner, Stiles, and Vos&Walraven*